

# Package ‘clmplus’

December 14, 2022

**Type** Package

**Title** Tool-Box of Chain Ladder Plus Models

**Version** 0.1.0

**Description** Implementation of the chain ladder model under the reverse time framework introduced in Hiabu (2017) <[doi:10.1080/03461238.2016.1240709](https://doi.org/10.1080/03461238.2016.1240709)>.

It also implements extensions that add flexibility to the individual development factors modeling by allowing practitioners to set their own hazard rate model.

**URL** <https://github.com/gpitt71/clmplus>

**BugReports** <https://github.com/gpitt71/clmplus/issues>

**License** GPL (>= 2)

**Imports** StMoMo, ChainLadder, stats, ggplot2, forecast, gridExtra,  
reshape2

**Encoding** UTF-8

**LazyData** true

**Suggests** knitr, rmarkdown, apc, dplyr, tidyverse

**VignetteBuilder** knitr, rmarkdown

**RoxygenNote** 7.2.2

**NeedsCompilation** no

**Author** Gabriele Pittarello [aut, cre, cph]  
(<<https://orcid.org/0000-0003-3360-5826>>),  
Munir Hiabu [aut, cph] (<<https://orcid.org/0000-0001-5846-667X>>),  
Andres Villegas [aut, cph]

**Maintainer** Gabriele Pittarello <[gabriele.pittarello@uniroma1.it](mailto:gabriele.pittarello@uniroma1.it)>

**Repository** CRAN

**Date/Publication** 2022-12-14 16:20:06 UTC

## R topics documented:

amases.gtpl	2
amases.mod	3
amases.mtpl	3
clmplus	4
clmplus.default	6
clmplus.RtTriangle	8
plot.clmplusmodel	10
plot.RtTriangle	11
plotresiduals	12
plotresiduals.clmplusmodel	12
plotresiduals.default	13
RtTriangle	14
sifa.gtpl	15
sifa.mod	15
sifa.mtpl	16

<b>Index</b>	<b>17</b>
--------------	-----------

**amases.gtpl**

*Amases GTPL*

### Description

Dataset of cumulative paid claims for a small italian company in the line of business: general third party liability.

### Usage

`amases.gtpl`

### Format

Run-off triangle with 12 development periods.

### References

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

---

`amases.mod`*Amases MOD*

---

**Description**

Dataset of cumulative paid claims for a small italian company in the line of business: motor or damage.

**Usage**`amases.mod`**Format**

Run-off triangle with 12 development periods.

**References**

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

---

`amases.mtpl`*Amases MTPL*

---

**Description**

Dataset of cumulative paid claims for a small italian company in the line of business: motor third party liability.

**Usage**`amases.mtpl`**Format**

Run-off triangle with 12 development periods.

**References**

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

clmplus

*Fit chain-ladder+ to reverse time triangles.*

## Description

Generic method to fit the chain ladder +.

## Usage

```
clmplus(
  RtTriangle,
  hazard.model = NULL,
  xc = NULL,
  iter.max = 10000,
  tolerance.max = 1e-06,
  link = c("log", "logit"),
  staticAgeFun = TRUE,
  periodAgeFun = "NP",
  cohortAgeFun = NULL,
  constFun = function(ax, bx, kt, b0x, gc, wxt, ages) list(ax = ax, bx = bx, kt = kt, b0x
    = b0x, gc = gc),
  gk.fc.model = "a",
  ckj.fc.model = "a",
  gk.order = c(1, 1, 0),
  ckj.order = c(0, 1, 0),
  ...
)
```

## Arguments

RtTriangle	RtTriangle object to be fitted.
hazard.model	hazard model supported from our package, must be provided as a string. The model can be chosen from: <ul style="list-style-type: none"> <li>• 'a': Age model, this is equivalent to the Mack chain-ladder.</li> <li>• 'ac': Age and cohort effects.</li> <li>• 'ap': Age and cohort effects.</li> <li>• 'apc': Age cohort and period effects.</li> <li>• 'lc': Lee-Carter parameters: age and age-period interaction effects.</li> <li>• 'cbd': Cairns-Blake-Dowd mortality model (CBD).</li> <li>• 'm6': CBD with cohorts.</li> <li>• 'm7': CBD m7 extension.</li> <li>• 'm8': CBD m7 extension.</li> </ul>
xc	xc constant parameter to be set for the m8 model. Default to NULL.
iter.max	maximum number of iterations for the Newton-Raphson algorithm. It will be ignored for other fitting procedures.

tolerance.max	maximum tolerance of parameters difference for convergence for the Newton-Rhapson algorithm implementation. Ignored for other fitting procedures.
link	defines the link function and random component associated with the mortality model. "log" would assume that deaths follow a Poisson distribution and use a log link while "logit" would assume that deaths follow a Binomial distribution and a logit link. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
staticAgeFun	logical value indicating if a static age function $\alpha_x$ is to be included. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
periodAgeFun	a list of length $N$ with the definitions of the period age modulating parameters $\beta_x^{(i)}$ . Each entry can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(i)} = 1$ or a predefined parametric function of age (see details). Set this to NULL if there are no period terms in the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
cohortAgeFun	defines the cohort age modulating parameter $\beta_x^{(0)}$ . It can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(0)} = 1$ , a predefined parametric function of age (see details) or NULL if there is no cohort effect. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
constFun	function defining the identifiability constraints of the model. It must be a function of the form constFun <- function(ax, bx, kt, b0x, gc, wxt, ages) taking a set of fitted model parameters and returning a list list(ax = ax, bx = bx, kt = kt, b0x = b0x, gc = gc) of the model parameters with the identifiability constraints applied. If omitted no identifiability constraints are applied to the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
gk.fc.model	model to forecast the cohort component for the last accident period. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a cohort effect.
ckj.fc.model	model to forecast the calendar period effect. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a period effect.
gk.order	order of the arima model with drift for the accident year effect extrapolation. Default to (1,1,0).
ckj.order	order of the arima model with drift for the calendar year effect extrapolation. Default to (0,1,0).
...	parameters to be passed to clmplus.

### Value

No return value, called to pass method clmplus.

### References

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

## Examples

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl=clmplus(sifa.mtpl.rtt, 'a')
```

**clmplus.default**      *Fit chain-ladder+ to reverse time triangles.*

## Description

This function allows to fit chain-ladder+ models to cumulative payments run-off triangles.

## Usage

```
## Default S3 method:
clmplus(
  RtTriangle,
  hazard.model = NULL,
  xc = NULL,
  iter.max = 10000,
  tolerance.max = 1e-06,
  link = c("log", "logit"),
  staticAgeFun = TRUE,
  periodAgeFun = "NP",
  cohortAgeFun = NULL,
  constFun = function(ax, bx, kt, b0x, gc, wxt, ages) list(ax = ax, bx = bx, kt = kt, b0x
    = b0x, gc = gc),
  gk.fc.model = "a",
  ckj.fc.model = "a",
  gk.order = c(1, 1, 0),
  ckj.order = c(0, 1, 0),
  ...
)
```

## Arguments

- |              |   |
|--------------|---|
| RtTriangle   | RtTriangle object to be fitted.   |
| hazard.model | hazard model supported from our package, must be provided as a string. The model can be choosen from: |
- 'a': Age model, this is equivalent to the Mack chain-ladder.
  - 'ac': Age and cohort effects.
  - 'ap': Age and cohort effects.
  - 'apc': Age cohort and period effects.
  - 'cbd': Cairns-Blake-Dowd mortality model (CBD).

	<ul style="list-style-type: none"> <li>• 'lc': Lee-Carter parameters: age and age-period interaction effects.</li> <li>• 'm6': CBD with cohorts.</li> <li>• 'm7': CBD m7 extension.</li> <li>• 'm8': CBD m7 extension.</li> </ul>
xc	xc constant parameter to be set for the m8 model. Default to NULL.
iter.max	maximum number of iterations for the Newton-Rhapson algorithm. It will be ignored for other fitting procedures.
tolerance.max	maximum tolerance of parameters difference for convergence for the Newton-Rhapson algorithm implementation. Ignored for other fitting procedures.
link	defines the link function and random component associated with the mortality model. "log" would assume that deaths follow a Poisson distribution and use a log link while "logit" would assume that deaths follow a Binomial distribution and a logit link. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
staticAgeFun	logical value indicating if a static age function $\alpha_x$ is to be included. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
periodAgeFun	a list of length $N$ with the definitions of the period age modulating parameters $\beta_x^{(i)}$ . Each entry can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(i)} = 1$ or a predefined parametric function of age (see details). Set this to NULL if there are no period terms in the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
cohortAgeFun	defines the cohort age modulating parameter $\beta_x^{(0)}$ . It can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(0)} = 1$ , a predefined parametric function of age (see details) or NULL if there is no cohort effect. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
constFun	function defining the identifiability constraints of the model. It must be a function of the form constFun <- function(ax, bx, kt, b0x, gc, wxt, ages) taking a set of fitted model parameters and returning a list list(ax = ax, bx = bx, kt = kt, b0x = b0x, gc = gc) of the model parameters with the identifiability constraints applied. If omitted no identifiability constraints are applied to the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
gk.fc.model	model to forecast the cohort component for the last accident period. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a cohort effect.
ckj.fc.model	model to forecast the calendar period effect. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a period effect.
gk.order	order of the arima model with drift for the accident year effect extrapolation. Default to (1,1,0).
ckj.order	order of the arima model with drift for the calendar year effect extrapolation. Default to (0,1,0).
...	parameters to be passed to clmplus.

## Value

No return value, called as clmplus method default.

## References

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

`clmplus.RtTriangle`     *Fit chain-ladder+ to reverse time triangles.*

## Description

This function allows to fit chain-ladder+ models to cumulative payments run-off triangles.

## Usage

```
## S3 method for class 'RtTriangle'
clmplus(
  RtTriangle,
  hazard.model = NULL,
  xc = NULL,
  iter.max = 10000,
  tolerance.max = 1e-06,
  link = c("log", "logit"),
  staticAgeFun = TRUE,
  periodAgeFun = "NP",
  cohortAgeFun = NULL,
  constFun = function(ax, bx, kt, b0x, gc, wxt, ages) list(ax = ax, bx = bx, kt = kt, b0x
    = b0x, gc = gc),
  gk.fc.model = "a",
  ckj.fc.model = "a",
  gk.order = c(1, 1, 0),
  ckj.order = c(0, 1, 0),
  ...
)
```

## Arguments

- |                           |  |
|---------------------------|--|
| <code>RtTriangle</code>   | RtTriangle object to be fitted.  |
| <code>hazard.model</code> | hazard model supported from our package, must be provided as a string. The model can be chosen from: <ul style="list-style-type: none"> <li>• 'a': Age model, this is equivalent to the Mack chain-ladder.</li> <li>• 'ac': Age and cohort effects.</li> <li>• 'ap': Age and cohort effects.</li> <li>• 'apc': Age cohort and period effects.</li> </ul> |

	<ul style="list-style-type: none"> <li>• 'lc': Lee-Carter parameters: age and age-period interaction effects.</li> <li>• 'cbd': Cairns-Blake-Dowd mortality model (CBD).</li> <li>• 'm6': CBD with cohorts.</li> <li>• 'm7': CBD m7 extension.</li> <li>• 'm8': CBD m7 extension.</li> </ul>
xc	xc constant parameter to be set for the m8 model. Default to NULL.
iter.max	maximum number of iterations for the Newton-Rhapson algorithm. It will be ignored for other fitting procedures.
tolerance.max	maximum tolerance of parameters difference for convergence for the Newton-Rhapson algorithm implementation. Ignored for other fitting procedures.
link	defines the link function and random component associated with the mortality model. "log" would assume that deaths follow a Poisson distribution and use a log link while "logit" would assume that deaths follow a Binomial distribution and a logit link. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
staticAgeFun	logical value indicating if a static age function $\alpha_x$ is to be included. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
periodAgeFun	a list of length $N$ with the definitions of the period age modulating parameters $\beta_x^{(i)}$ . Each entry can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(i)} = 1$ or a predefined parametric function of age (see details). Set this to NULL if there are no period terms in the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
cohortAgeFun	defines the cohort age modulating parameter $\beta_x^{(0)}$ . It can take values: "NP" for non-parametric age terms, "1" for $\beta_x^{(0)} = 1$ , a predefined parametric function of age (see details) or NULL if there is no cohort effect. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
constFun	function defining the identifiability constraints of the model. It must be a function of the form constFun <- function(ax, bx, kt, b0x, gc, wxt, ages) taking a set of fitted model parameters and returning a list list(ax = ax, bx = bx, kt = kt, b0x = b0x, gc = gc) of the model parameters with the identifiability constraints applied. If omitted no identifiability constraints are applied to the model. To be disregarded unless the practitioner specifies his own hazard model in StMoMo.
gk.fc.model	model to forecast the cohort component for the last accident period. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a cohort effect.
ckj.fc.model	model to forecast the calendar period effect. It can be either arima ('a') or linear model ('l'). Disregarded for models that do not have a period effect.
gk.order	order of the arima model with drift for the accident year effect extrapolation. Default to (1,1,0).
ckj.order	order of the arima model with drift for the calendar year effect extrapolation. Default to (0,1,0).
...	parameters to be passed to clmplus.

**Value**

An object of class "clmplusmodel". A list with the following elements:

<code>model.fit</code>	Hazard model fit from StMoMo.
<code>hazard.model</code>	Hazard model chosen.
<code>exposure</code>	Matrix that contains the exposure derived from the input triangle, under the uniform claims arrival assumption.
<code>ultimate.cost</code>	Ultimate costs vector.
<code>model.fcst</code>	Hazard forecasts.
<code>converged</code>	logical value. Whether the fit converged.
<code>citer</code>	Number of Netwon-Rhapson iterations in case a lee-carter hazard-model was chosen.

**References**

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

**Examples**

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl=clmplus(sifa.mtpl.rtt, 'a')
```

`plot.clmplusmodel`      *Plot the hazard model fitted and forecasted parameters*

**Description**

This function allows to define the behavior of the triangle payments.

**Usage**

```
## S3 method for class 'clmplusmodel'
plot(x, cy.type = "fe", ...)
```

**Arguments**

<code>x</code>	clmplus model to be plotted.
<code>cy.type</code>	whether to show fitted period effect with or without extrapolatio Default is "fe", standing for fitted and extrapolated. Alternative is to specify "f" for fitted effect.
<code>...</code>	Arguments to be passed to plot.

**Value**

No return value, plots coefficients of the hazard models.

**References**

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

**Examples**

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl<-clmplus(sifa.mtpl.rtt, 'a')
plot(hz.chl)
```

plot.RtTriangle	<i>Plot the payments behavior</i>
-----------------	-----------------------------------

**Description**

This function allows to define the behavior of the triangle payments.

**Usage**

```
## S3 method for class 'RtTriangle'
plot(x, ...)
```

**Arguments**

x	RtTriangle to be plotted.
...	Arguments to be passed to plot.

**Value**

No return value, plots the run-off triangle cumulative payments and incremental payments.

**References**

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

**Examples**

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
plot(sifa.mtpl.rtt)
```

**plotresiduals**      *Plot the hazard model residuals*

### Description

This function allows to plot the hazard model residuals on the triangle payments.

### Usage

```
plotresiduals(clmplusmodel, heat.lim = c(-2.5, 2.5))
```

### Arguments

clmplusmodel	clmplusmodel object to be plotted.
heat.lim	limits in the residuals plot.

### Value

No return value, called to pass method plotresiduals.

### References

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

### Examples

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl<-clmplus(sifa.mtpl.rtt, 'a')
plotresiduals(hz.chl)
```

**plotresiduals.clmplusmodel**      *Plot the hazard model residuals*

### Description

This function allows to plot the hazard model residuals on the triangle payments.

### Usage

```
## S3 method for class 'clmplusmodel'
plotresiduals(clmplusmodel, heat.lim = c(-2.5, 2.5))
```

**Arguments**

`clmplusmodel`    clmplusmodel object to be plotted.  
`heat.lim`        limits in the residuals plot.

**Value**

No return value, plots the hazard model residuals in triangular form.

**References**

Hiabu, Munir. “On the relationship between classical chain ladder and granular reserving.” Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

**Examples**

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl<-clmplus(sifa.mtpl.rtt, 'a')
plotresiduals(hz.chl)
```

`plotresiduals.default` *Plot the hazard model residuals*

**Description**

This function allows to plot the hazard model residuals on the triangle payments.

**Usage**

```
## Default S3 method:
plotresiduals(clmplusmodel, heat.lim = c(-2.5, 2.5))
```

**Arguments**

`clmplusmodel`    clmplusmodel object to be plotted.  
`heat.lim`        limits in the residuals plot.

**Value**

No return value, called as `plotresiduals` method default.

**References**

Hiabu, Munir. “On the relationship between classical chain ladder and granular reserving.” Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

## Examples

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
hz.chl<-clmpplus(sifa.mtpl.rtt, 'a')
plotresiduals(hz.chl)
```

**RtTriangle**

*Reverse time triangles*

## Description

This function allows to define the class of triangles for reverse time models.

## Usage

```
RtTriangle(cumulative.payments.triangle, k = 1/2)
```

## Arguments

cumulative.payments.triangle	Input triangle of cumulative payments.
k	Claims exposure in the cell, also known as lost exposure.

## Value

An object of class "RtTriangle". Lists the following elements:

cumulative.payments.triangle	Input triangle of cumulative payments.
occurrence	Matrix that contains the occurrence derived from the input triangle.
exposure	Matrix that contains the exposure derived from the input triangle, under the uniform claims arrival assumption.
incremental.payments.triangle	Triangle of incremental payments derived from the input.
J	Run-off triangle dimension.
diagonal	Cumulatives payments last diagonal.

## References

Hiabu, Munir. "On the relationship between classical chain ladder and granular reserving." Scandinavian Actuarial Journal 2017 (2017): 708 - 729.

## Examples

```
data(sifa.mtpl)
sifa.mtpl.rtt <- RtTriangle(cumulative.payments.triangle=sifa.mtpl)
```

---

`sifa.gtpl`*Sifa GTPL*

---

**Description**

Dataset of cumulative paid claims for a medium italian company in the line of business: general third party liability.

**Usage**`sifa.gtpl`**Format**

Run-off triangle with 12 development periods.

**References**

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

---

`sifa.mod`*Sifa MOD*

---

**Description**

Dataset of cumulative paid claims for a medium italian company in the line of business: motor or damage.

**Usage**`sifa.mod`**Format**

Run-off triangle with 12 development periods.

**References**

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

---

`sifa.mtpl`

---

*Sifa MTPL*

---

### Description

Dataset of cumulative paid claims for a medium italian company in the line of business: motor third party liability.

### Usage

`sifa.mtpl`

### Format

Run-off triangle with 12 development periods.

### References

Savelli, Nino, and Clemente, Gian Paolo. "Lezioni di matematica attuariale delle assicurazioni danni." EDUCatt-Ente per il diritto allo studio universitario dell'Università Cattolica, 2014

# Index

## \* datasets

  amases.gtpl, 2  
  amases.mod, 3  
  amases.mtpl, 3  
  sifa.gtpl, 15  
  sifa.mod, 15  
  sifa.mtpl, 16

amases.gtpl, 2  
amases.mod, 3  
amases.mtpl, 3

clmplus, 4  
clmplus.default, 6  
clmplus.RtTriangle, 8

plot.clmplusmodel, 10  
plot.RtTriangle, 11  
plotresiduals, 12  
plotresiduals.clmplusmodel, 12  
plotresiduals.default, 13

RtTriangle, 14

sifa.gtpl, 15  
sifa.mod, 15  
sifa.mtpl, 16