# Package 'DtD'

October 12, 2022

## R topics documented:

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BS_call                              *European Call Option Price and the Inverse*

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### Description

Computes the European call option and the inverse. All vectors with length greater than one needs to have the same length.

### Usage

```
BS_call(V, D, T., r, vol)

get_underlying(S, D, T., r, vol, tol = 1e-12)
```

### Arguments

| | |
|---|---|
| V | numeric vector or scalar with price of the underlying asset. |
| D | numeric vector or scalar with debt due in T.. |
| T. | numeric vector or scalar with time to maturity. |
| r | numeric vector or scalar with risk free rates. |
| vol | numeric vector or scalar with volatilities, $\sigma$s. |
| S | numeric vector with observed stock prices. |
| tol | numeric scalar with tolerance to get_underlying. The difference is scaled if the absolute of S is large than tol as in the tolerance argument to all.equal.numeric. |

### Value

Numeric vector or scalar with price of the underlying asset or equity price.

### See Also

BS_fit

### Examples

```
library(DtD)
set.seed(58661382)
sims <- BS_sim(
  vol = .2, mu = .03, dt = .1, V_0 = 100, T. = 1, D = rep(80, 20), r = .01)

stopifnot(with(
```

```
    sims, isTRUE(all.equal(V, get_underlying(S, D, T, r, vol)))))
  stopifnot(with(
    sims, isTRUE(all.equal(S, BS_call(V, D, T, r, vol)))))
```

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BS_fit                    *Fit Black-Scholes Parameters*

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### Description

Function to estimate the volatility, $\sigma$, and drift, $\mu$. See vignette("Distance-to-default", package = "DtD") for details. All vectors with length greater than one needs to have the same length. The Nelder-Mead method from [optim](optim) is used when method = "mle". Either time or dt should be passed.

### Usage

```
BS_fit(
  S,
  D,
  T.,
  r,
  time,
  dt,
  vol_start,
  method = c("iterative", "mle"),
  tol = 1e-12,
  eps = 1e-08
)
```

### Arguments

| | |
|---|---|
| S | numeric vector with observed stock prices. |
| D | numeric vector or scalar with debt due in T.. |
| T. | numeric vector or scalar with time to maturity. |
| r | numeric vector or scalar with risk free rates. |
| time | numeric vector with the observation times. |
| dt | numeric scalar with time increments between observations. |
| vol_start | numeric scalar with starting value for $\sigma$. |
| method | string to specify which estimation method to use. |
| tol | numeric scalar with tolerance to [get_underlying](get_underlying). The difference is scaled if the absolute of S is large than tol as in the tolerance argument to [all.equal.numeric](all.equal.numeric). |
| eps | numeric scalar with convergence threshold. |

## Value

A list with the following components

| | |
|---|---|
| ests | estimates of $\sigma$, and drift, $\mu$. |
| n_iter | number of iterations when `method = "iterative"` and number of log likelihood evaluations when `method = "mle"`. |
| success | logical for whether the estimation method converged. |

## Warning

Choosing `tol >= eps` or roughly equal may make the method alternate between two solutions for some data sets.

## Examples

```
library(DtD)
set.seed(83486778)
sims <- BS_sim(
  vol = .1, mu = .05, dt = .1, V_0 = 100, T. = 1, D = rep(80, 20), r = .01)

with(sims,
     BS_fit(S = S, D = D, T. = T, r = r, time = time, method = "mle"))
```

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| BS_fit_rolling | *Fit Black-Scholes Parameters Over Rolling Window* |
|---|---|

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## Description

Function to estimate the volatility, $\sigma$, and drift, $\mu$. E.g., the window can be over a given number of months. See `vignette("Distance-to-default", package = "DtD")` for details.

## Usage

```
BS_fit_rolling(
  S,
  D,
  T.,
  r,
  time,
  dt,
  vol_start,
  method = c("iterative", "mle"),
  tol = 1e-12,
  eps = 1e-08,
  grp,
  width,
  min_obs
)
```

## Arguments

| | |
|---|---|
| S | numeric vector with observed stock prices. |
| D | numeric vector or scalar with debt due in `T.`. |
| T. | numeric vector or scalar with time to maturity. |
| r | numeric vector or scalar with risk free rates. |
| time | numeric vector with the observation times. |
| dt | numeric scalar with time increments between observations. |
| vol_start | numeric scalar with starting value for $\sigma$. |
| method | string to specify which estimation method to use. |
| tol | numeric scalar with tolerance to `get_underlying`. The difference is scaled if the absolute of S is large than `tol` as in the `tolerance` argument to `all.equal.numeric`. |
| eps | numeric scalar with convergence threshold. |
| grp | integer vector with the group identifier (e.g., units of months). |
| width | integer scalar with the units of `grp` to include in the rolling window. |
| min_obs | integer scalar for the minimum number of observation required in each window. |

## Value

Matrix with the `grp`, number of observation in the window, parameter estimates, and 'n_iter' as in `BS_fit`, and whether the estimation method was successful.

An `error` attribute is added in case other code than `optim` fails. It is a list of lists with the `grp` index where the method failed and the output from `try`.

## See Also

`BS_fit`

## Examples

```
# Simulate data
set.seed(55770945)
n <- 21L * 3L * 12L # 21 trading days for 3 years w/ 12 months
sims <- BS_sim(
  vol = .1, mu = .05, dt = .1, V_0 = 100, T. = 1,
  D = runif(n, 80, 90), r = runif(n, 0, .01))
sims$month <- (1:nrow(sims) - 1L) %/% 21L + 1L

# throw out some months
sims <- subset(sims, !month %in% 15:24)

# assign parameters
grp <- sims$month
width <- 12L        # window w/ 12 month width
min_obs <- 21L * 3L # require 3 months of data

# estimate results with R loop which is slightly simpler then the
```

```
# implementation
grps <- unique(grp)
out <- matrix(
  NA_real_, nrow = length(grps), ncol = 6,
  dimnames = list(NULL, c("mu", "vol", "n_iter", "success", "n_obs", "grp")))
for(g in grps){
  idx <- which(grps == g)
  keep <- which(grp %in% (g - width + 1L):g)
  out[idx, c("n_obs", "grp")] <- c(length(keep), g)
  if(length(keep) < min_obs)
    next
  res <- with(
    sims[keep, ],
    BS_fit(S = S, D = D, T. = T, r = r, time = time, method = "iterative",
           vol_start = 1))
  out[idx, c("mu", "vol", "n_iter", "success")] <- rep(
    do.call(c, res[c("ests", "n_iter", "success")]), each = length(idx))
}

# we get the same with the R function
out_func <- with(sims, BS_fit_rolling(
  S = S, D = D, T. = T, r = r, time = time, method = "iterative",
  grp = month, width = width, min_obs = min_obs))

all.equal(out[, names(out) != "n_iter"],
          out_func[, names(out_func) != "n_iter"])
```

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BS_sim                          *Simulate Stock Price and Price of Underlying Asset*

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### Description

At least one of D, r, or T. needs to have the desired length of the simulated series. All vectors with length greater than one needs to have the same length.

### Usage

```
BS_sim(vol, mu, dt, V_0, D, r, T.)
```

### Arguments

| | |
|---|---|
| vol | numeric scalar with $\sigma$ value. |
| mu | numeric scalar with $\mu$ value. |
| dt | numeric scalar with time increments between observations. |
| V_0 | numeric scalar with starting value of the underlying asset, $S_0$. |
| D | numeric vector or scalar with debt due in T.. |
| r | numeric vector or scalar with risk free rates. |
| T. | numeric vector or scalar with time to maturity. |

## See Also

BS_fit

## Examples

```
library(DtD)
set.seed(79156879)
sims <- BS_sim(
  vol = .1, mu = .05, dt = .2, V_0 = 100, T. = 1, D = rep(80, 20), r = .01)

# plot underlying
plot(sims$V)

# plot stock
plot(sims$S)
```

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| merton_ll | *Compute Log-Likelihood of Merton Model* |
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## Description

Computes the log-likelihood for a given values of $\mu$ and $\sigma$.

## Usage

```
merton_ll(S, D, T., r, time, dt, vol, mu, tol = 1e-12)
```

## Arguments

| | |
|---|---|
| S | numeric vector with observed stock prices. |
| D | numeric vector or scalar with debt due in T.. |
| T. | numeric vector or scalar with time to maturity. |
| r | numeric vector or scalar with risk free rates. |
| time | numeric vector with the observation times. |
| dt | numeric scalar with time increments between observations. |
| vol | numeric scalar with the $\sigma$ value. |
| mu | numeric scalar with the $\mu$ value. |
| tol | numeric scalar with tolerance to get_underlying. The difference is scaled if the absolute of S is large than tol as in the tolerance argument to all.equal.numeric. |

## See Also

BS_fit

## Examples

```
# we get the same if we call `optim` as follows. The former is faster and is
# recommended
set.seed(4648394)
sims <- BS_sim(
  vol = .1, mu = .05, dt = .1, V_0 = 100, T. = 1, D = rep(80, 20), r = .01)

r1 <- with(
  sims, BS_fit(S = S, D = D, T. = T, r = r, time = time, method = "mle",
               eps = 1e-8, vol_start = .2))

r2 <- optim(c(mu = 0, log_vol = log(.2)), function(par)
  -with(
    sims, merton_ll(S = S, D = D, T. = T, r = r, time = time,
                    mu = par["mu"], vol = exp(par["log_vol"]))))

all.equal(r1$n_iter, unname(r2$counts[1]))
all.equal(r1$ests[1], r2$par[1])
all.equal(r1$ests[2], exp(r2$par[2]), check.attributes = FALSE)

# the log-likelihood integrates to one as it should though likely not the
# most stable way to test this
ll <- integrate(
  function(x) sapply(x, function(S)
    exp(merton_ll(
      S = c(1, S), D = .8, T. = 3, r = .01, dt = 1/250, vol = .2,
      mu = .05))),
  lower = 1e-4, upper = 6)
stopifnot(isTRUE(all.equal(ll$value, 1, tolerance = 1e-5)))
```

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