

Working with dbarts Saved Trees

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When a `dbarts` model is fit with the `keepTrees` option set to `TRUE`, the sampler will return those trees in a “flat” format that corresponds to a depth-first, left-hand traversal. Recursion can be used to map functions the nodes in this structure, aggregating statistics of interest.

Simulation

To illustrate, we generate a fake dataset according to the “Friedman 1” model (Friedman 1991).

```
f <- function(x)
  10 * sin(pi * x[,1] * x[,2]) + 20 * (x[,3] - 0.5)^2 +
  10 * x[,4] + 5 * x[,5]

set.seed(99)
sigma <- 1.0
n <- 100

x <- matrix(runif(n * 10), n, 10)
y <- rnorm(n, f(x), sigma)

data <- data.frame(x, y)
```

Model Fitting

In order to interrogate the trees, they must be saved when the model is fit. This is accomplished by setting:

- For `bart`: `keeptrees = TRUE`
- For `bart2`: `keepTrees = TRUE`
- For a custom `dbartsSampler`, `control = dbartsControl(keepTrees = TRUE)`

In the context of our fake data, with small sample numbers for illustrative purposes, a model can be fit thusly:

```
library(dbarts, quietly = TRUE)

bartFit <- bart(
  y ~ ., data,
  ndpost = 4, # number of posterior samples
  nskip = 1000, # number of "warmup" samples to discard
  nchain = 2, # number of independent, parallel chains
  nthread = 1, # units of parallel execution
  ntrees = 3, # number of trees per chain
  seed = 2, # chosen to generate a deep tree
  keeptrees = TRUE,
  verbose = FALSE)
```

Extracting Trees

The `extract` function accepts as a `type` the value `"trees"`. If present, the arguments `chainNums`, `sampleNums`, and/or `treeNums` can be used to extract only a subset of trees.

```
trees <- extract(bartFit, "trees")
```

Flattened Trees

The `trees` data frame corresponds to a depth-first, left-hand-side tree traversal.

```
print(head(trees, n = 10))
```

##	chain	sample	tree	n	var	value
## 1	1	1	1	100	2	0.22796229
## 2	1	1	1	18	1	0.28581841
## 3	1	1	1	7	-1	-0.02959142
## 4	1	1	1	11	-1	-0.20336110
## 5	1	1	1	82	5	0.10434842
## 6	1	1	1	8	-1	-0.02468813
## 7	1	1	1	74	2	0.77999259
## 8	1	1	1	56	-1	0.09481149
## 9	1	1	1	18	4	0.76320697
## 10	1	1	1	9	-1	0.02619319

The columns refer to:

- `chain`, `sample`, `tree` - index variables
- `n` - number of observations in node (from the training data, or from `newdata` when it is supplied; see “Counts for New Data” below)
- `var` - either the index of the variable used for splitting or -1 if the node is a leaf
- `value` - either the value such that observations less than or equal to it are sent down the left path of the tree or the predicted value for a leaf node

The mapping between the values of `var` and the variable names can be looked up in the internal copy of the data that the sampler stores. This can be found in a fitted model as the element `fit$data@x`, as seen below.

Tree Traversal

A useful technique for processing trees is [recursion](#). By having the function return the number of nodes it has processed, it is possible to advance from the left-hand-side to the right by skipping ahead the appropriate number of rows. For example:

```
# Turns a flattened tree data frame into a list of lists, or a "natural" tree structure.
rebuildTree <- function(tree, object) {
  # Define a worker function that will be recursively called on every node.
  rebuildTreeRecurse <- function(tree) {
    node <- list(
      value = tree$value[1],
      n     = tree$n[1]
    )
    # Check node if is a leaf, and if so return early.
    if (tree$var[1] == -1) {
      node$n_nodes <- 1
      return(node)
    }
  }
```

```

node$var <- variableNames[tree$var[1]]

# By removing the current row, we can recurse down the left branch.
headOfLeftBranch <- tree[-1,]
left <- rebuildTreeRecurse(headOfLeftBranch)
n_nodes.left <- left$n_nodes
left$n_nodes <- NULL
node$left <- left

# The right branch is obtained by advancing past the left nodes.
headOfRightBranch <- tree[seq.int(2 + n_nodes.left, nrow(tree)),]
right <- rebuildTreeRecurse(headOfRightBranch)
n_nodes.right <- right$n_nodes
right$n_nodes <- NULL
node$right <- right

node$n_nodes <- 1L + n_nodes.left + n_nodes.right

return(node)
}
variableNames <- colnames(object$fit$data@x)

result <- rebuildTreeRecurse(tree)
result$n_nodes <- NULL
return(result)
}

treeOfInterest <- subset(trees, chain == 1 & sample == 3 & tree == 1)
print(rebuildTree(treeOfInterest, bartFit))

## $value
## [1] 0.2279623
##
## $n
## [1] 100
##
## $var
## [1] "X2"
##
## $left
## $left$value
## [1] 0.2858184
##
## $left$n
## [1] 18
##
## $left$var
## [1] "X1"
##
## $left$left
## $left$left$value
## [1] -0.03007205
##
## $left$left$n

```

```

## [1] 7
##
##
## $left$right
## $left$right$value
## [1] 0.7964085
##
## $left$right$n
## [1] 11
##
## $left$right$var
## [1] "X10"
##
## $left$right$left
## $left$right$left$value
## [1] -0.2228073
##
## $left$right$left$n
## [1] 9
##
##
##
## $left$right$right
## $left$right$right$value
## [1] -0.2207859
##
## $left$right$right$n
## [1] 2
##
##
##
## $right
## $right$value
## [1] 0.1043484
##
## $right$n
## [1] 82
##
## $right$var
## [1] "X5"
##
## $right$left
## $right$left$value
## [1] -0.0003996113
##
## $right$left$n
## [1] 8
##
##
## $right$right
## $right$right$value
## [1] 0.7799926
##
## $right$right$n

```

```
## [1] 74
##
## $right$right$var
## [1] "X2"
##
## $right$right$left
## $right$right$left$value
## [1] 0.1331738
##
## $right$right$left$n
## [1] 56
##
##
## $right$right$right
## $right$right$right$value
## [1] 0.763207
##
## $right$right$right$n
## [1] 18
##
## $right$right$right$var
## [1] "X4"
##
## $right$right$right$left
## $right$right$right$left$value
## [1] 0.03938565
##
## $right$right$right$left$n
## [1] 9
##
##
## $right$right$right$right
## $right$right$right$right$value
## [1] 0.2617129
##
## $right$right$right$right$n
## [1] 9
```

Using a `by` statement, it is possible to “rebuild” all trees at once:

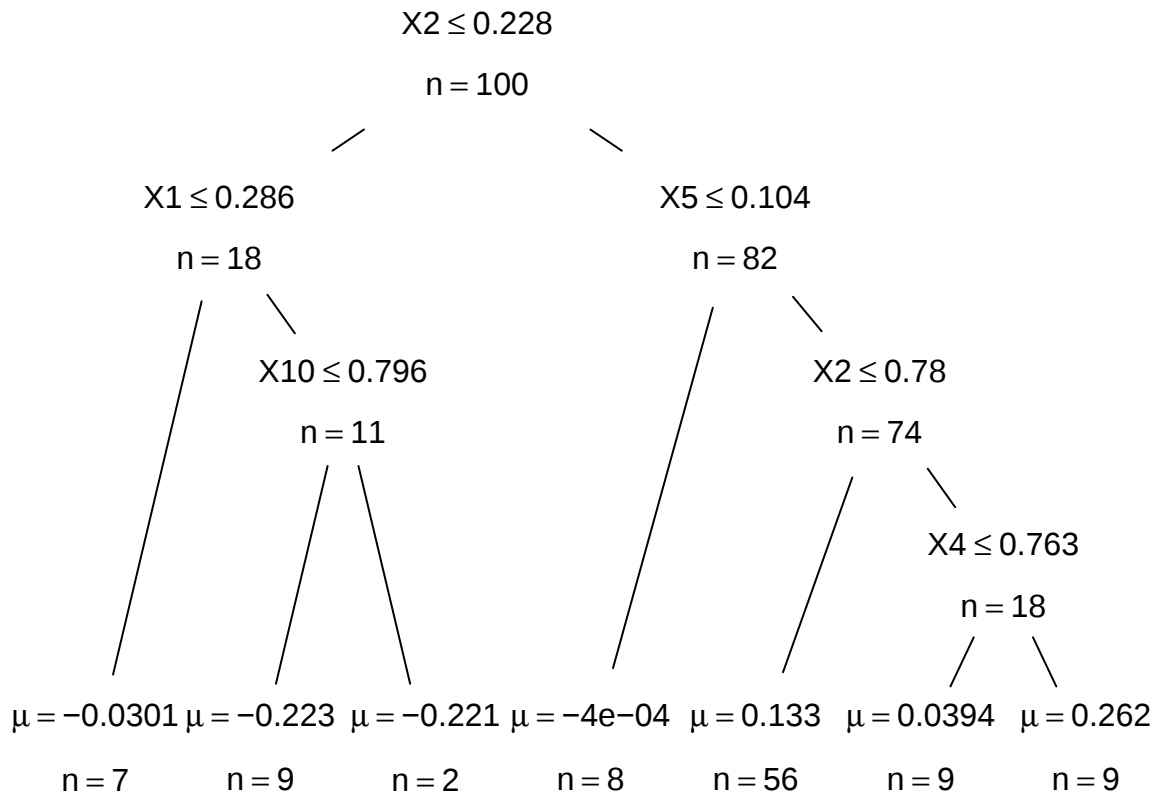
```
allTrees <- by(
  data      = trees,
  INDICES   = trees[,c("chain", "sample", "tree")],
  FUN       = rebuildTree,
  object    = bartFit)

# One way to index the result of this:
#   allTrees[chain = "1", sample = "2", tree = "3"]
```

Plotting Trees

`dbartsSampler` objects have a `plotTree` method that can be used to visualize single trees:

```
bartFit$fit$plotTree(chainNum = 1, sampleNum = 3, treeNum = 1)
```



Getting Tree Predictions

The following function traverses a flattened tree, splits observations while going the branches, and populates a vector giving the predicted value of that tree on input data. It requires a data in the same format as the fitted bart model so that it can evaluate the splits.

```

getPredictionsForTree <- function(tree, x) {
  predictions <- rep(NA_real_, nrow(x))

  getPredictionsForTreeRecursive <- function(tree, indices) {
    if (tree$var[1] == -1) {
      # Assigns in the calling environment by using <<-
      predictions[indices] <<- tree$value[1]
      return(1)
    }

    goesLeft <- x[indices, tree$var[1]] <= tree$value[1]
    headOfLeftBranch <- tree[-1,]
    n_nodes.left <- getPredictionsForTreeRecursive(
      headOfLeftBranch, indices[goesLeft])

    headOfRightBranch <- tree[seq.int(2 + n_nodes.left, nrow(tree)),]
    n_nodes.right <- getPredictionsForTreeRecursive(
      headOfRightBranch, indices[!goesLeft])

    return(1 + n_nodes.left + n_nodes.right)
  }

  getPredictionsForTreeRecursive(tree, seq_len(nrow(x)))
}

```

```

    return(predictions)
}

getPredictionsForTree(treeOfInterest, bartFit$fit$data@x[1:5,])

## [1] -0.2228073037  0.2617128852  0.1331738132 -0.2228073037 -0.0003996113

```

A `by` statement can be used to obtain all predictions for all trees.

Counts for New Data

The recursion above routes new data through the trees by hand. To simply count how a new dataset distributes across the (frozen) partition, pass `newdata` to `extract`: the tree structure, split rules, and leaf predictions are unchanged, and only the `n` column is recomputed by routing that data through each tree. The predictors are supplied in the same form as for `predict`.

```

newData <- x[1:5,]
newTrees <- extract(bartFit, "trees", newdata = newData, sampleNums = 3, treeNums = 1)
print(subset(newTrees, chain == 1))

```

##	chain	sample	tree	n	var	value
## 1	1	3	1 5	2	0.2279622898	
## 2	1	3	1 2	1	0.2858184060	
## 3	1	3	1 0	-1	-0.0300720511	
## 4	1	3	1 2	10	0.7964084761	
## 5	1	3	1 2	-1	-0.2228073037	
## 6	1	3	1 0	-1	-0.2207858507	
## 7	1	3	1 3	5	0.1043484238	
## 8	1	3	1 1	-1	-0.0003996113	
## 9	1	3	1 2	2	0.7799925941	
## 10	1	3	1 1	-1	0.1331738132	
## 11	1	3	1 1	4	0.7632069662	
## 12	1	3	1 0	-1	0.0393856545	
## 13	1	3	1 1	-1	0.2617128852	

Advanced Traversal

The following function can be used to map an arbitrary function over a tree.

```

mapOverNodes <- function(tree, f, ...) {
  mapOverNodesRecurse <- function(tree, depth, f, ...) {
    node <- list(
      value = tree$value[1],
      n = tree$n[1],
      depth = depth
    )
    if (tree$var[1] == -1) {
      node$n_nodes <- 1
      node$f.x <- f(node, ...)
      return(node)
    }
    node$var <- tree$var[1]
    node$f.x <- f(node, ...)

    headOfLeftBranch <- tree[-1,]

```

```

    left <- mapOverNodesRecurse(headOfLeftBranch, depth + 1, f, ...)
    n_nodes.left <- left$n_nodes
    left$n_nodes <- NULL
    node$left <- left

    headOfRightBranch <- tree[seq.int(2 + n_nodes.left, nrow(tree)),]
    right <- mapOverNodesRecurse(headOfRightBranch, depth + 1, f, ...)
    n_nodes.right <- right$n_nodes
    right$n_nodes <- NULL
    node$right <- right

    node$n_nodes <- 1 + n_nodes.left + n_nodes.right
    return(node)
  }
  result <- mapOverNodesRecurse(tree, 1, f, ...)
  result$n_nodes <- NULL
  return(result)
}

```

As an example of its usage, the following function aggregates all ancestor/descendant relationships in a tree. In a data object - here an R environment - it keeps track of the current state of traversal. This includes the variables that have been used for splits above the current node and also includes the current node's depth, which is used to detect backtracking.

```

observeInteractions <- function(node, ...) {
  if (is.null(node$var)) return(NULL)

  interactionData <- list(...)$interactionData
  # Make the current node visible inside the environment.
  interactionData$node <- node
  with(interactionData, {
    if (node$depth <= currentDepth) {
      # If true, we have backtracked to go down the right branch, so we
      # remove the variables from the left branch.
      currentVariables <- currentVariables[seq_len(node$depth - 1)]
    }
    if (length(interactionData$currentVariables) > 0) {
      # This is a brute-force way of updating the following indices,
      # relying on the column-major storage order that R uses:
      # hasInteraction[currentVariables,,drop = FALSE][,node$var]
      updateIndices <- currentVariables +
        (node$var - 1) * nrow(hasInteraction)
      hasInteraction[updateIndices] <- TRUE
    }
    currentVariables <- c(currentVariables, node$var)
    currentDepth <- node$depth
  })
  rm("node", envir = interactionData)

  # Since the function is used for its side effects, there isn't a return
  # value.
  return(NULL)
}

```

```

numVariables <- ncol(bartFit$fit$data@x)
variableNames <- colnames(bartFit$fit$data@x)

# Define this as an environment as they are mutable
interactionData <- list2env(list(
  currentDepth = 0,
  currentVariables = integer(),
  hasInteraction = matrix(
    data = FALSE,
    ncol = numVariables, nrow = numVariables,
    dimnames = list(ancestor = variableNames, descendant = variableNames)
  )
))

invisible(mapOverNodes(
  treeOfInterest,
  observeInteractions,
  interactionData = interactionData
))

```

After execution, the boolean matrix in the interaction data environment will contain all ancestor/descendant relationships in this tree.

```
print(interactionData$hasInteraction)
```

```
##           descendant
## ancestor   X1    X2    X3    X4    X5    X6    X7    X8    X9   X10
##   X1 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  TRUE
##   X2  TRUE  TRUE FALSE  TRUE  TRUE FALSE FALSE FALSE FALSE  TRUE
##   X3 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##   X4 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##   X5 FALSE  TRUE FALSE  TRUE  FALSE FALSE FALSE FALSE FALSE  FALSE
##   X6 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##   X7 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##   X8 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##   X9 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
##  X10 FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE FALSE  FALSE
```

Finally, the entire process can be wrapped in a `by` statement and the results aggregated across all trees in order to count the number of times variables have specific relationships.

References

Friedman, Jerome H. 1991. “Multivariate Adaptive Regression Splines.” *The Annals of Statistics* 19 (1): 1–67. <https://doi.org/10.1214/aos/1176347963>.