

Testing hierarchical pathway kinetics with residue data on cyantraniliprole

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Introduction

The purpose of this document is to test demonstrate how nonlinear hierarchical models (NLHM) based on the parent degradation models SFO, FOMC, DFOP and HS, with serial formation of two or more metabolites can be fitted with the `mkln` package.

It was assembled in the course of work package 1.2 of Project Number 173340 (Application of nonlinear hierarchical models to the kinetic evaluation of chemical degradation data) of the German Environment Agency carried out in 2022 and 2023.

The `mkln` package is used in version 1.2.2 which is currently under development. The newly introduced functionality that is used here is a simplification of excluding random effects for a set of fits based on a related set of fits with a reduced model, and the documentation of the starting parameters of the fit, so that all starting parameters of `saem` fits are now listed in the summary. The `saemix` package is used as a backend for fitting the NLHM, but is also loaded to make the convergence plot function available.

This document is processed with the `knitr` package, which also provides the `kable` function that is used to improve the display of tabular data in R markdown documents. For parallel processing, the `parallel` package is used.

```
library(mkin)
library(knitr)
library(saemix)
library(parallel)
n_cores <- detectCores()
if (Sys.info()["sysname"] == "Windows") {
  cl <- makePSOCKcluster(n_cores)
} else {
  cl <- makeForkCluster(n_cores)
}
```

Test data

The example data are taken from the final addendum to the DAR from 2014 and are distributed with the mkin package. Residue data and time step normalisation factors are read in using the function `read_spreadsheet` from the mkin package. This function also performs the time step normalisation.

```
data_file <- system.file(
  "testdata", "cyantraniliprole_soil_efsa_2014.xlsx",
  package = "mkin")
cyan_ds <- read_spreadsheet(data_file, parent_only = FALSE)
```

The following tables show the covariate data and the 5 datasets that were read in from the spreadsheet file.

```
pH <- attr(cyan_ds, "covariates")
kable(pH, caption = "Covariate data")
```

Table 1: Covariate data

	pH
Nambsheim	7.90
Tama	6.20
Gross-Umstadt	7.04
Sassafras	4.62
Lleida	8.05

```

for (ds_name in names(cyan_ds)) {
  print(
    kable(mkin_long_to_wide(cyan_ds[[ds_name]]),
      caption = paste("Dataset", ds_name),
      booktabs = TRUE, row.names = FALSE))
  cat("\n\\clearpage\n")
}

```

Table 2: Dataset Nambsheim

time	cyan	JCZ38	J9C38	JSE76	J9Z38
0.000000	105.79	NA	NA	NA	NA
3.210424	77.26	7.92	11.94	5.58	9.12
7.490988	57.13	15.46	16.58	12.59	11.74
17.122259	37.74	15.98	13.36	26.05	10.77
23.543105	31.47	6.05	14.49	34.71	4.96
43.875788	16.74	6.07	7.57	40.38	6.52
67.418893	8.85	10.34	6.39	30.71	8.90
107.014116	5.19	9.61	1.95	20.41	12.93
129.487080	3.45	6.18	1.36	21.78	6.99
195.835832	2.15	9.13	0.95	16.29	7.69
254.693596	1.92	6.92	0.20	13.57	7.16
321.042348	2.26	7.02	NA	11.12	8.66
383.110535	NA	5.05	NA	10.64	5.56
0.000000	105.57	NA	NA	NA	NA
3.210424	78.88	12.77	11.94	5.47	9.12
7.490988	59.94	15.27	16.58	13.60	11.74
17.122259	39.67	14.26	13.36	29.44	10.77
23.543105	30.21	16.07	14.49	35.90	4.96
43.875788	18.06	9.44	7.57	42.30	6.52
67.418893	8.54	5.78	6.39	34.70	8.90
107.014116	7.26	4.54	1.95	23.33	12.93
129.487080	3.60	4.22	1.36	23.56	6.99
195.835832	2.84	3.05	0.95	16.21	7.69
254.693596	2.00	2.90	0.20	15.53	7.16
321.042348	1.79	0.94	NA	9.80	8.66
383.110535	NA	1.82	NA	9.49	5.56

Table 3: Dataset Tama

time	cyan	JCZ38	J9Z38	JSE76
0.000000	106.14	NA	NA	NA
2.400833	93.47	6.46	2.85	NA
5.601943	88.39	10.86	4.65	3.85
12.804442	72.29	11.97	4.91	11.24
17.606108	65.79	13.11	6.63	13.79
32.811382	53.16	11.24	8.90	23.40
50.417490	44.01	11.34	9.98	29.56
80.027761	33.23	8.82	11.31	35.63
96.833591	40.68	5.94	8.32	29.09
146.450803	20.65	4.49	8.72	36.88
190.466072	17.71	4.66	11.10	40.97
240.083284	14.86	2.27	11.62	40.11
286.499386	12.02	NA	10.73	42.58
0.000000	109.11	NA	NA	NA
2.400833	96.84	5.52	2.04	2.02
5.601943	85.29	9.65	2.99	4.39
12.804442	73.68	12.48	5.05	11.47
17.606108	64.89	12.44	6.29	15.00
32.811382	52.27	10.86	7.65	23.30
50.417490	42.61	10.54	9.37	31.06
80.027761	34.29	10.02	9.04	37.87
96.833591	30.50	6.34	8.14	33.97
146.450803	19.21	6.29	8.52	26.15
190.466072	17.55	5.81	9.89	32.08
240.083284	13.22	5.99	10.79	40.66
286.499386	11.09	6.05	8.82	42.90

Table 4: Dataset Gross-Umstadt

time	cyan	JCZ38	J9Z38	JSE76
0.0000000	103.03	NA	NA	NA
2.1014681	87.85	4.79	3.26	0.62
4.9034255	77.35	8.05	9.89	1.32
10.5073404	69.33	9.74	12.32	4.74
21.0146807	55.65	14.57	13.59	9.84
31.5220211	49.03	14.66	16.71	12.32
42.0293615	41.86	15.97	13.64	15.53
63.0440422	34.88	18.20	14.12	22.02
84.0587230	28.26	15.64	14.06	25.60
0.0000000	104.05	NA	NA	NA
2.1014681	85.25	2.68	7.32	0.69
4.9034255	77.22	7.28	8.37	1.45
10.5073404	65.23	10.73	10.93	4.74
21.0146807	57.78	12.29	14.80	9.05
31.5220211	54.83	14.05	12.01	11.05
42.0293615	45.17	12.12	17.89	15.71
63.0440422	34.83	12.90	15.86	22.52
84.0587230	26.59	14.28	14.91	28.48
0.0000000	104.62	NA	NA	NA
0.8145225	97.21	NA	4.00	NA
1.9005525	89.64	3.59	5.24	NA
4.0726125	87.90	4.10	9.58	NA
8.1452251	86.90	5.96	9.45	NA
12.2178376	74.74	7.83	15.03	5.33
16.2904502	74.13	8.84	14.41	5.10
24.4356753	65.26	11.84	18.33	6.71
32.5809004	57.70	12.74	19.93	9.74
0.0000000	101.94	NA	NA	NA
0.8145225	99.94	NA	NA	NA
1.9005525	94.87	NA	4.56	NA
4.0726125	86.96	6.75	6.90	NA
8.1452251	80.51	10.68	7.43	2.58
12.2178376	78.38	10.35	9.46	3.69
16.2904502	70.05	13.73	9.27	7.18
24.4356753	61.28	12.57	13.28	13.19
32.5809004	52.85	12.67	12.95	13.69

Table 5: Dataset Sassafras

time	cyan	JCZ38	J9Z38	JSE76
0.000000	102.17	NA	NA	NA
2.216719	95.49	1.11	0.10	0.83
5.172343	83.35	6.43	2.89	3.30
11.083593	78.18	10.00	5.59	0.81
22.167186	70.44	17.21	4.23	1.09
33.250779	68.00	20.45	5.86	1.17
44.334371	59.64	24.64	3.17	2.72
66.501557	50.73	27.50	6.19	1.27
88.668742	45.65	32.77	5.69	4.54
0.000000	100.43	NA	NA	NA
2.216719	95.34	3.21	0.14	0.46
5.172343	84.38	5.73	4.75	0.62
11.083593	78.50	11.89	3.99	0.73
22.167186	71.17	17.28	4.39	0.66
33.250779	59.41	18.73	11.85	2.65
44.334371	64.57	22.93	5.13	2.01
66.501557	49.08	33.39	5.67	3.63
88.668742	40.41	39.60	5.93	6.17

Table 6: Dataset Lleida

time	cyan	JCZ38	J9Z38	JSE76
0.000000	102.71	NA	NA	NA
2.821051	79.11	5.70	8.07	0.97
6.582451	70.03	7.17	11.31	4.72
14.105253	50.93	10.25	14.84	9.95
28.210505	33.43	10.40	14.82	24.06
42.315758	24.69	9.75	16.38	29.38
56.421010	22.99	10.06	15.51	29.25
84.631516	14.63	5.63	14.74	31.04
112.842021	12.43	4.17	13.53	33.28
0.000000	99.31	NA	NA	NA
2.821051	82.07	6.55	5.60	1.12
6.582451	70.65	7.61	8.01	3.21
14.105253	53.52	11.48	10.82	12.24
28.210505	35.60	11.19	15.43	23.53
42.315758	34.26	11.09	13.26	27.42
56.421010	21.79	4.80	18.30	30.20
84.631516	14.06	6.30	16.35	32.32
112.842021	11.51	5.57	12.64	32.51

Parent only evaluations

As the pathway fits have very long run times, evaluations of the parent data are performed first, in order to determine for each hierarchical parent degradation model which random effects on the degradation model parameters are ill-defined.

```
cyan_sep_const <- mmkin(c("SFO", "FOMC", "DFOP", "SFORB", "HS"),
  cyan_ds, quiet = TRUE, cores = n_cores)
cyan_sep_tc <- update(cyan_sep_const, error_model = "tc")
cyan_saem_full <- mhmkin(list(cyan_sep_const, cyan_sep_tc))
status(cyan_saem_full) |> kable()
```

	const	tc
SFO	OK	OK
FOMC	OK	OK
DFOP	OK	OK
SFORB	OK	OK
HS	OK	OK

All fits converged successfully.

```
illparms(cyan_saem_full) |> kable()
```

	const	tc
SFO	sd(cyan_0)	sd(cyan_0)
FOMC	sd(log_beta)	sd(cyan_0)
DFOP	sd(cyan_0)	sd(cyan_0), sd(log_k1)
SFORB	sd(cyan_free_0)	sd(cyan_free_0), sd(log_k_cyan_free_bound)
HS	sd(cyan_0)	sd(cyan_0)

In almost all models, the random effect for the initial concentration of the parent compound is ill-defined. For the biexponential models DFOP and SFORB, the random effect of one additional parameter is ill-defined when the two-component error model is used.

```
anova(cyan_saem_full) |> kable(digits = 1)
```

	npars	AIC	BIC	Lik
SFO const	5	833.9	832.0	-412.0
SFO tc	6	831.6	829.3	-409.8
FOMC const	7	709.1	706.4	-347.6
FOMC tc	8	689.2	686.1	-336.6
DFOP const	9	703.0	699.5	-342.5
SFORB const	9	701.3	697.8	-341.7
HS const	9	718.6	715.1	-350.3
DFOP tc	10	703.1	699.2	-341.6
SFORB tc	10	700.1	696.2	-340.1
HS tc	10	716.7	712.8	-348.3

Model comparison based on AIC and BIC indicates that the two-component error model is preferable for all parent models with the exception of DFOP. The lowest AIC and BIC values are obtained with the FOMC model, followed by SFORB and DFOP.

Pathway fits

Evaluations with pathway established previously

To test the technical feasibility of coupling the relevant parent degradation models with different transformation pathway models, a list of `mkkinmod` models is set up below. As in the EU evaluation, parallel formation of metabolites JCZ38 and J9Z38 and secondary formation of metabolite JSE76 from JCZ38 is used.

```
if (!dir.exists("cyan_dlls")) dir.create("cyan_dlls")
cyan_path_1 <- list(
  sfo_path_1 = mkinmod(
    cyan = mkinsub("SF0", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0"), quiet = TRUE,
    name = "sfo_path_1", dll_dir = "cyan_dlls", overwrite = TRUE),
  fomc_path_1 = mkinmod(
    cyan = mkinsub("FOMC", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0"), quiet = TRUE,
    name = "fomc_path_1", dll_dir = "cyan_dlls", overwrite = TRUE),
  dfop_path_1 = mkinmod(
    cyan = mkinsub("DFOP", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0"), quiet = TRUE,
    name = "dfop_path_1", dll_dir = "cyan_dlls", overwrite = TRUE),
  sforb_path_1 = mkinmod(
    cyan = mkinsub("SFORB", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0"), quiet = TRUE,
    name = "sforb_path_1", dll_dir = "cyan_dlls", overwrite = TRUE),
  hs_path_1 = mkinmod(
    cyan = mkinsub("HS", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0"), quiet = TRUE,
    name = "hs_path_1", dll_dir = "cyan_dlls", overwrite = TRUE)
)
```

To obtain suitable starting values for the NLHM fits, separate pathway fits are performed for all datasets.

```
f_sep_1_const <- mmkin(
  cyan_path_1,
  cyan_ds,
  error_model = "const",
  cluster = cl,
  quiet = TRUE)
status(f_sep_1_const) |> kable()
```

	Nambsheim	Tama	Gross-Umstadt	Sassafras	Lleida
sfo_path_1	OK	OK	OK	OK	OK
fomc_path_1	OK	OK	OK	OK	OK
dfop_path_1	OK	OK	OK	OK	OK
sforb_path_1	OK	OK	OK	OK	OK

	Nambsheim	Tama	Gross-Umstadt	Sassafras	Lleida
hs_path_1	C	C	C	C	C

```
f_sep_1_tc <- update(f_sep_1_const, error_model = "tc")
status(f_sep_1_tc) |> kable()
```

	Nambsheim	Tama	Gross-Umstadt	Sassafras	Lleida
sfo_path_1	OK	OK	OK	OK	OK
fomc_path_1	OK	OK	OK	OK	C
dfop_path_1	OK	OK	OK	OK	OK
sforb_path_1	OK	C	OK	OK	OK
hs_path_1	C	OK	C	OK	OK

Most separate fits converged successfully. The biggest convergence problems are seen when using the HS model with constant variance.

For the hierarchical pathway fits, those random effects that could not be quantified in the corresponding parent data analyses are excluded.

In the code below, the output of the `illparms` function for the parent only fits is used as an argument `no_random_effect` to the `mhmkin` function. The possibility to do so was introduced in `mkim` version 1.2.2 which is currently under development.

```
f_saem_1 <- mhmkin(list(f_sep_1_const, f_sep_1_tc),
  no_random_effect = illparms(cyan_saem_full),
  cluster = c1)
```

```
status(f_saem_1) |> kable()
```

	const	tc
sfo_path_1	Fth, FO	Fth, FO
fomc_path_1	OK	Fth, FO
dfop_path_1	Fth, FO	Fth, FO
sforb_path_1	Fth, FO	Fth, FO
hs_path_1	Fth, FO	Fth, FO

The status information from the individual fits shows that all fits completed successfully. The matrix entries Fth and FO indicate that the Fisher Information Matrix could not be inverted for the fixed effects (theta) and the random effects (Omega), respectively. For the affected fits, ill-defined parameters cannot be determined using the `illparms` function, because it relies on the Fisher Information Matrix.

```
illparms(f_saem_1) |> kable()
```

	const	tc
sfo_path_1	NA	NA
fomc_path_1	sd(log_k_J9Z38), sd(f_cyan_ilr_2), sd(f_JCZ38_qlogis)	NA
dfop_path_1	NA	NA
sforb_path_1	NA	NA
hs_path_1	NA	NA

The model comparison below suggests that the pathway fits using DFOP or SFORB for the parent compound provide the best fit.

```
anova(f_saem_1) |> kable(digits = 1)
```

	npar	AIC	BIC	Lik
sfo_path_1 const	16	2692.8	2686.6	-1330.4
sfo_path_1 tc	17	2657.7	2651.1	-1311.9
fomc_path_1 const	18	2427.8	2420.8	-1195.9
fomc_path_1 tc	19	2423.4	2416.0	-1192.7
dfop_path_1 const	20	2403.2	2395.4	-1181.6
sforb_path_1 const	20	2401.4	2393.6	-1180.7
hs_path_1 const	20	2427.3	2419.5	-1193.7
dfop_path_1 tc	20	2398.0	2390.2	-1179.0
sforb_path_1 tc	20	2399.8	2392.0	-1179.9
hs_path_1 tc	21	2422.3	2414.1	-1190.2

For these two parent model, successful fits are shown below. Plots of the fits with the other parent models are shown in the Appendix.

```
plot(f_saem_1[["dfop_path_1", "tc"]])
```

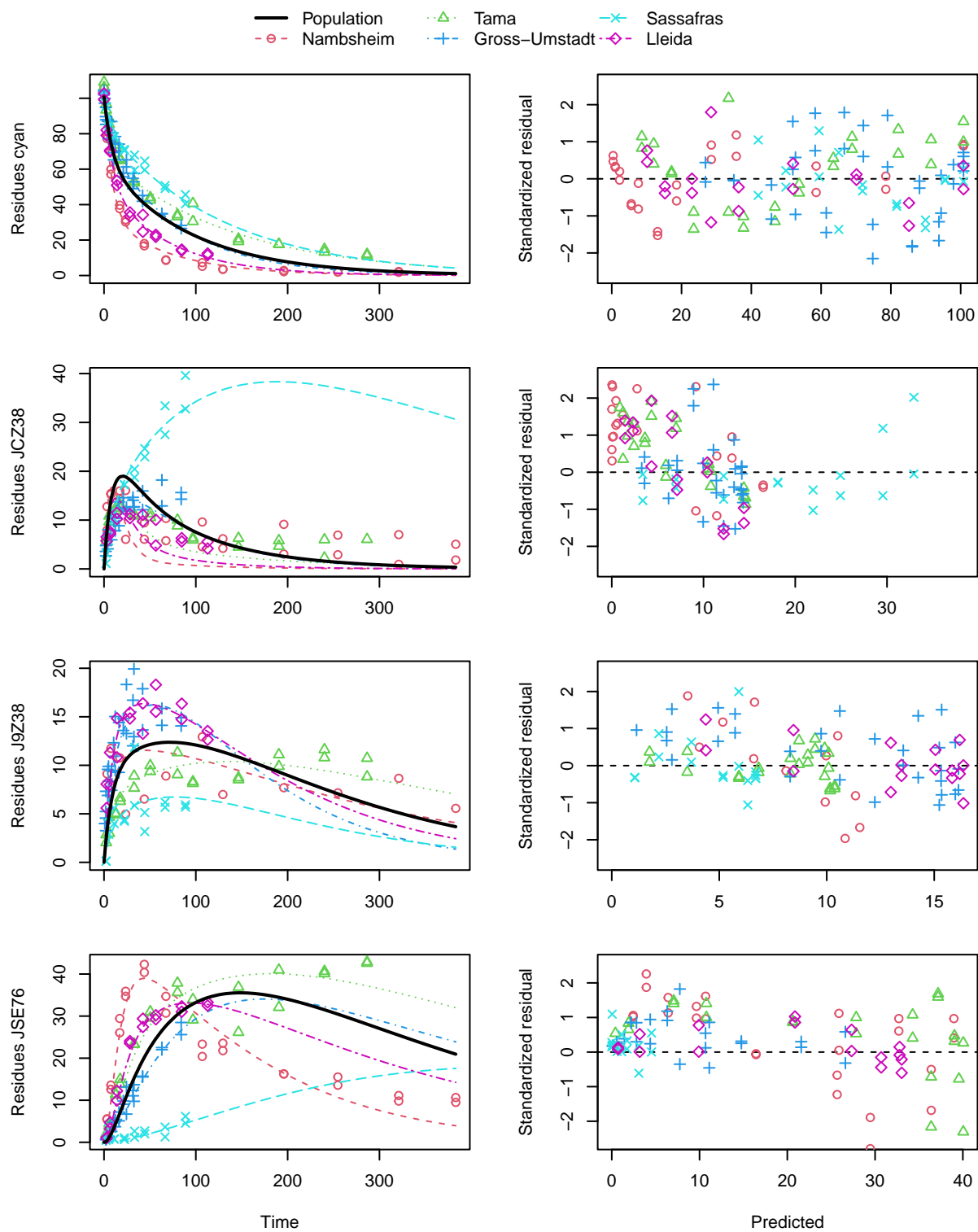


Figure 1: DFOP pathway fit with two-component error

```
plot(f_saem_1[["sforb_path_1", "tc"]])
```

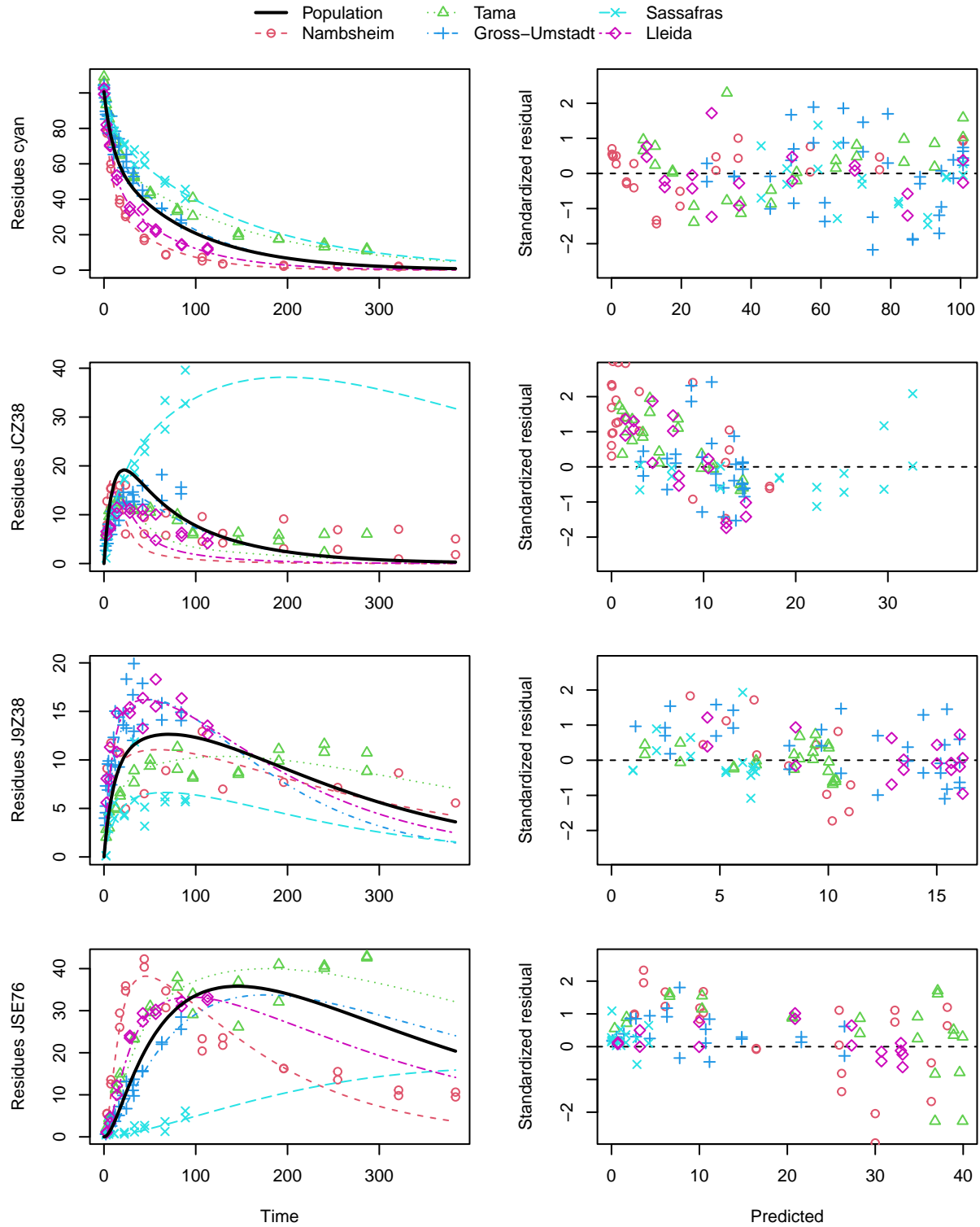


Figure 2: SFORB pathway fit with two-component error

A closer graphical analysis of these Figures shows that the residues of transformation product JCZ38 in the soils Tama and Nambshiem observed at later time points are strongly and systematically underestimated.

Alternative pathway fits

To improve the fit for JCZ38, a back-reaction from JSE76 to JCZ38 was introduced in an alternative version of the transformation pathway, in analogy to the back-reaction from K5A78 to K5A77. Both pairs of transformation products are pairs of an organic acid with its corresponding amide (Addendum 2014, p. 109). As FOMC provided the best fit for the parent, and the biexponential models DFOP and SFORB provided the best initial pathway fits, these three parent models are used in the alternative pathway fits.

```
cyan_path_2 <- list(
  fomc_path_2 = mkinmod(
    cyan = mkinsub("FOMC", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0", "JCZ38"),
    name = "fomc_path_2", quiet = TRUE,
    dll_dir = "cyan_dlls",
    overwrite = TRUE
  ),
  dfop_path_2 = mkinmod(
    cyan = mkinsub("DFOP", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0", "JCZ38"),
    name = "dfop_path_2", quiet = TRUE,
    dll_dir = "cyan_dlls",
    overwrite = TRUE
  ),
  sforb_path_2 = mkinmod(
    cyan = mkinsub("SFORB", c("JCZ38", "J9Z38")),
    JCZ38 = mkinsub("SF0", "JSE76"),
    J9Z38 = mkinsub("SF0"),
    JSE76 = mkinsub("SF0", "JCZ38"),
    name = "sforb_path_2", quiet = TRUE,
    dll_dir = "cyan_dlls",
    overwrite = TRUE
  )
)
f_sep_2_const <- mmkin(
  cyan_path_2,
  cyan_ds,
  error_model = "const",
  cluster = cl,
  quiet = TRUE)

status(f_sep_2_const) |> kable()
```

	Nambsheim	Tama	Gross-Umstadt	Sassafras	Lleida
fomc_path_2	OK	OK	OK	C	OK
dfop_path_2	OK	OK	OK	C	OK
sforb_path_2	OK	OK	OK	C	OK

Using constant variance, separate fits converge with the exception of the fits to the Sassafras soil data.

```
f_sep_2_tc <- update(f_sep_2_const, error_model = "tc")
status(f_sep_2_tc) |> kable()
```

	Nambsheim	Tama	Gross-Umstadt	Sassafras	Lleida
fomc_path_2	OK	C	OK	C	OK
dfop_path_2	OK	OK	OK	C	OK
sforb_path_2	OK	OK	OK	OK	OK

Using the two-component error model, all separate fits converge with the exception of the alternative pathway fit with DFOP used for the parent and the Sassafras dataset.

```
f_saem_2 <- mhmkin(list(f_sep_2_const, f_sep_2_tc),
  no_random_effect = illparms(cyan_saem_full[2:4, ]),
  cluster = cl)
```

```
status(f_saem_2) |> kable()
```

	const	tc
fomc_path_2	OK	FO
dfop_path_2	OK	OK
sforb_path_2	OK	OK

The hierarchical fits for the alternative pathway completed successfully.

```
illparms(f_saem_2) |> kable()
```

	const	tc
fomc_path_2	sd(f_JCZ38_qlogis), sd(f_JSE76_qlogis)	NA
dfop_path_2	sd(f_JCZ38_qlogis), sd(f_JSE76_qlogis)	sd(f_JCZ38_qlogis), sd(f_JSE76_qlogis)
sforb_path_2	sd(f_JCZ38_qlogis), sd(f_JSE76_qlogis)	sd(f_JCZ38_qlogis), sd(f_JSE76_qlogis)

In both fits, the random effects for the formation fractions for the pathways from JCZ38 to JSE76, and for the reverse pathway from JSE76 to JCZ38 are ill-defined.

```
anova(f_saem_2) |> kable(digits = 1)
```

	npar	AIC	BIC	Lik
fomc_path_2 const	20	2308.3	2300.5	-1134.2
fomc_path_2 tc	21	2248.3	2240.1	-1103.2
dfop_path_2 const	22	2289.6	2281.0	-1122.8
sforb_path_2 const	22	2284.1	2275.5	-1120.0
dfop_path_2 tc	22	2234.4	2225.8	-1095.2
sforb_path_2 tc	22	2240.4	2231.8	-1098.2

The variants using the biexponential models DFOP and SFORB for the parent compound and the two-component error model give the lowest AIC and BIC values and are plotted below. Compared with the original pathway, the AIC and BIC values indicate a large improvement. This is confirmed by the plots, which show that the metabolite JCZ38 is fitted much better with this model.


```
plot(f_saem_2[["fomc_path_2", "tc"]])
```

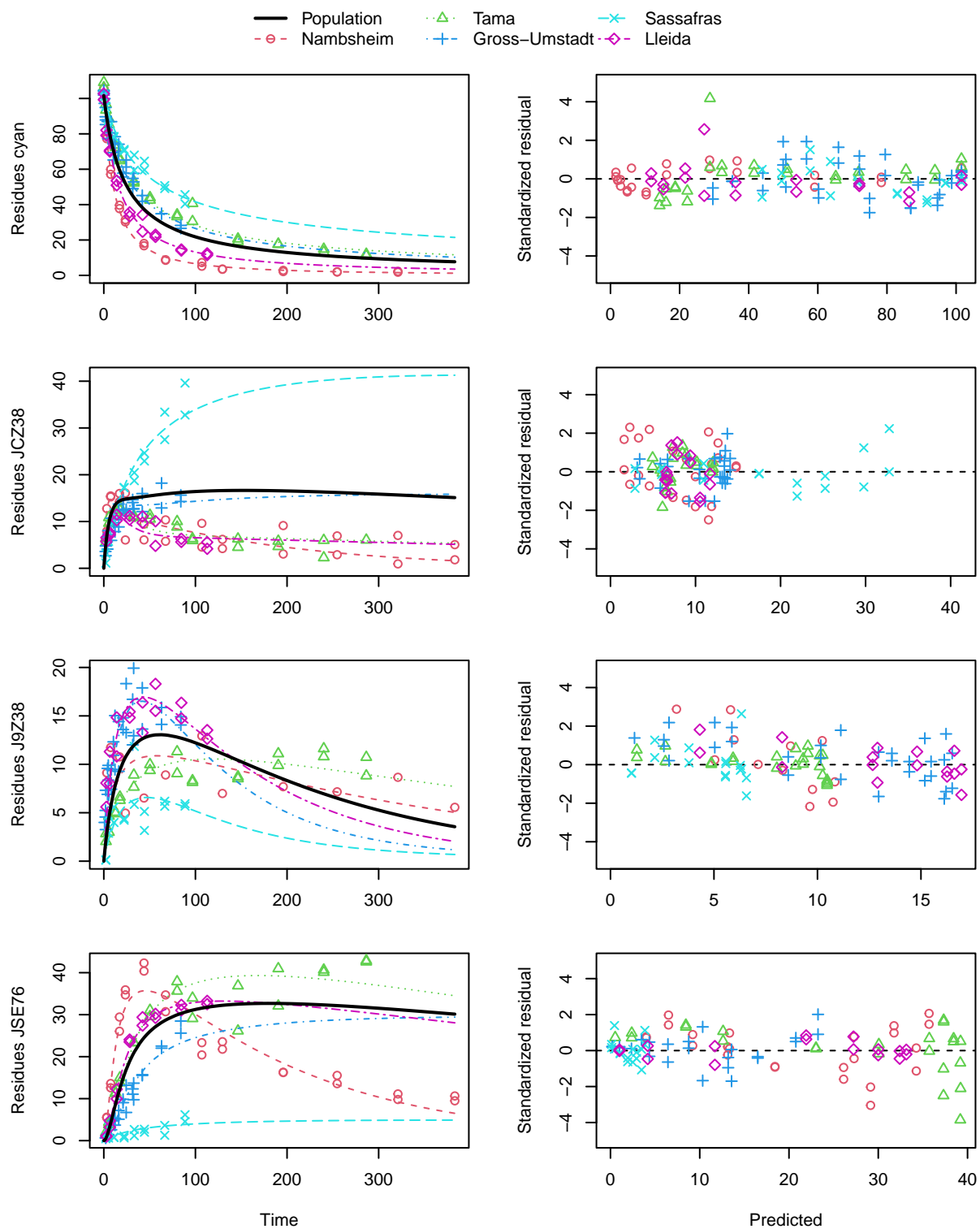


Figure 3: FOMC pathway fit with two-component error, alternative pathway

```
plot(f_saem_2[["dfop_path_2", "tc"]])
```

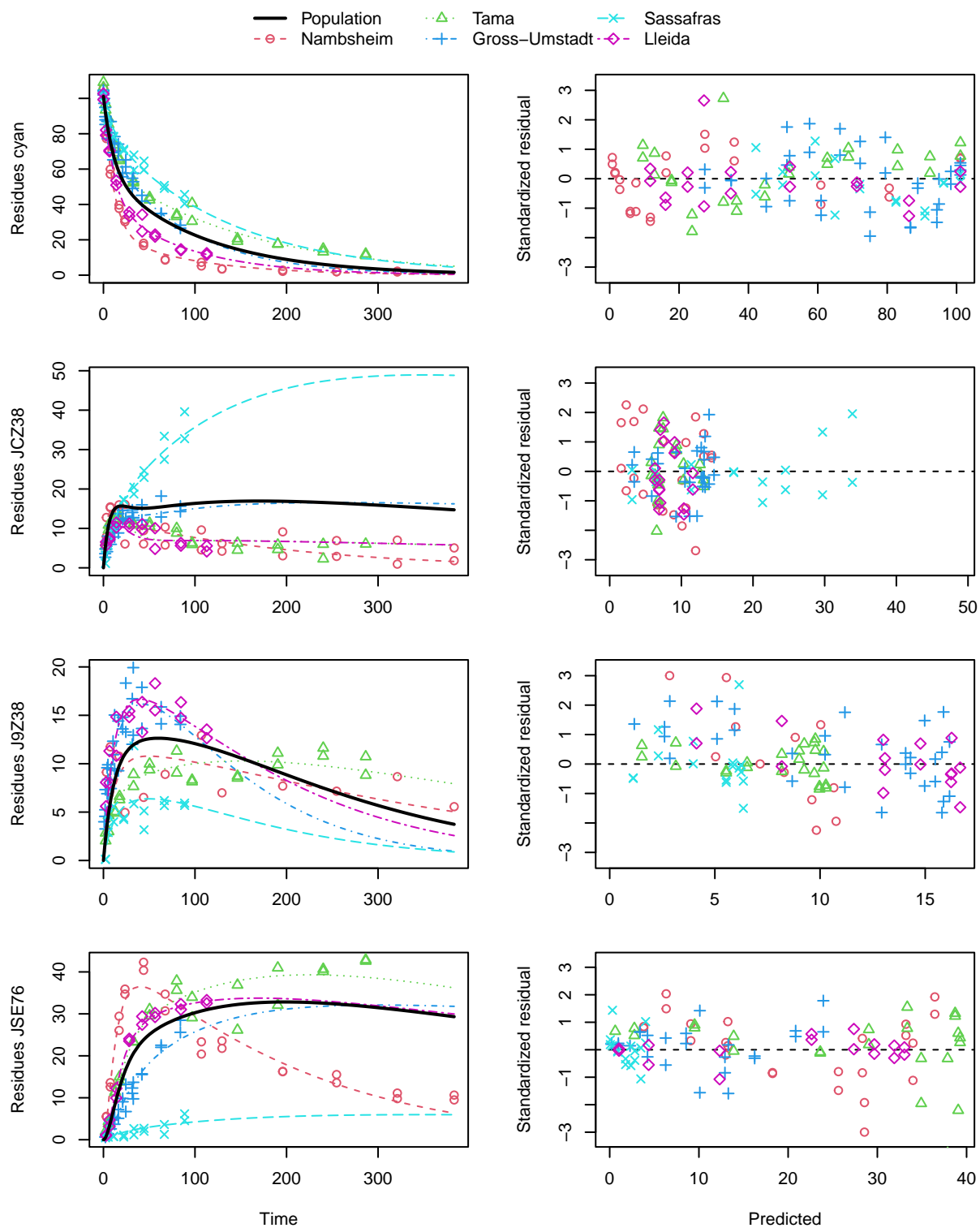


Figure 4: DFOP pathway fit with two-component error, alternative pathway

```
plot(f_saem_2[["sforb_path_2", "tc"]])
```

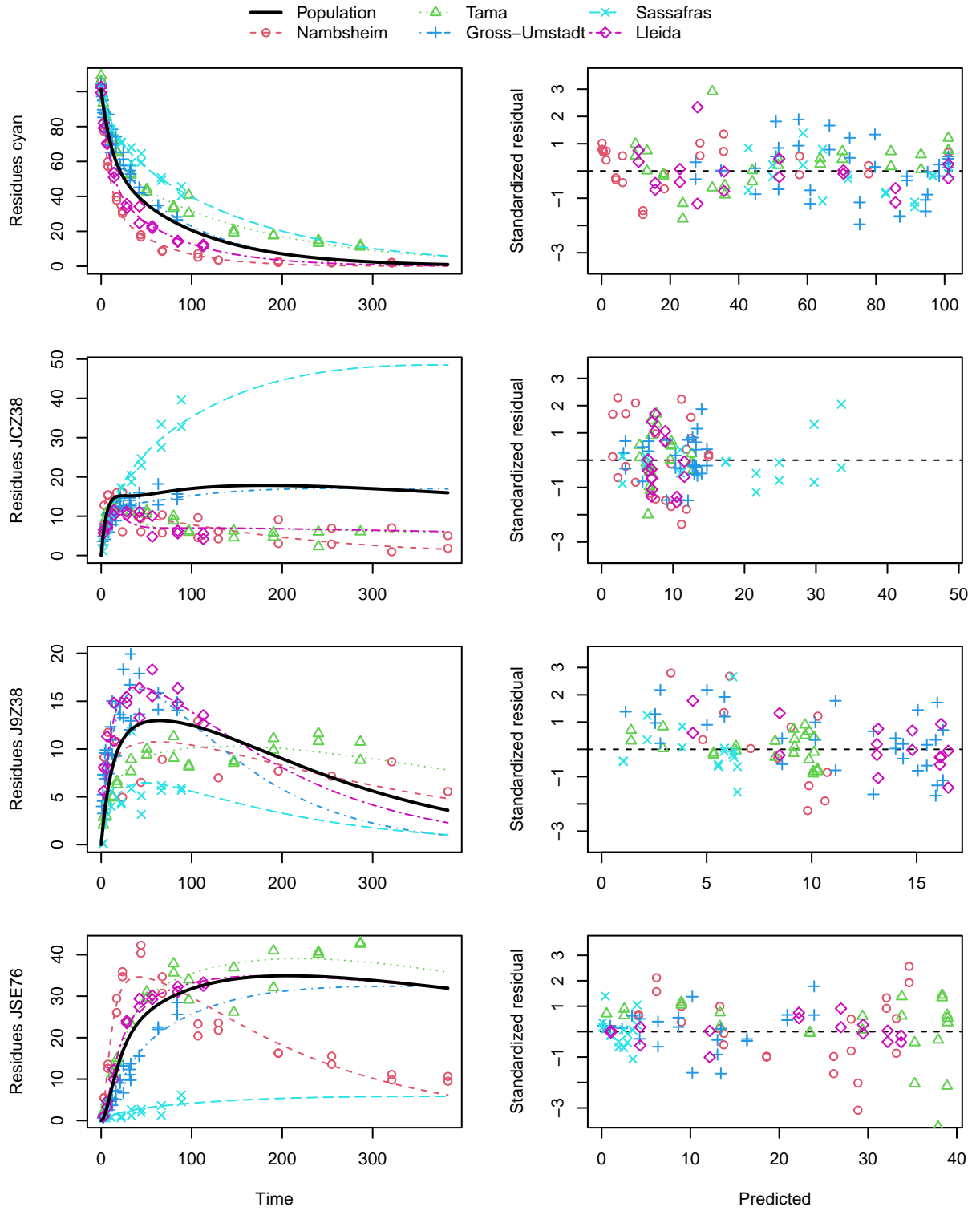


Figure 5: SFORB pathway fit with two-component error, alternative pathway

Refinement of alternative pathway fits

All ill-defined random effects that were identified in the parent only fits and in the above pathway fits, are excluded for the final evaluations below. For this purpose, a list of character vectors is created below that can be indexed by row and column indices, and which contains the degradation parameter names for which random effects should be excluded for each of the hierarchical fits contained in `f_saem_2`.

```
no_ranef <- matrix(list(), nrow = 3, ncol = 2, dimnames = dimnames(f_saem_2))
no_ranef[["fomc_path_2", "const"]] <- c("log_beta", "f_JCZ38_qlogis", "f_JSE76_qlogis")
no_ranef[["fomc_path_2", "tc"]] <- c("cyan_0", "f_JCZ38_qlogis", "f_JSE76_qlogis")
no_ranef[["dfop_path_2", "const"]] <- c("cyan_0", "f_JCZ38_qlogis", "f_JSE76_qlogis")
no_ranef[["dfop_path_2", "tc"]] <- c("cyan_0", "log_k1", "f_JCZ38_qlogis", "f_JSE76_qlogis")
no_ranef[["sforb_path_2", "const"]] <- c("cyan_free_0",
    "f_JCZ38_qlogis", "f_JSE76_qlogis")
no_ranef[["sforb_path_2", "tc"]] <- c("cyan_free_0", "log_k_cyan_free_bound",
    "f_JCZ38_qlogis", "f_JSE76_qlogis")
clusterExport(cl, "no_ranef")

f_saem_3 <- update(f_saem_2,
    no_random_effect = no_ranef,
    cluster = cl)

status(f_saem_3) |> kable()
```

	const	tc
fomc_path_2	E	Fth
dfop_path_2	Fth	Fth
sforb_path_2	Fth	Fth

With the exception of the FOMC pathway fit with constant variance, all updated fits completed successfully. However, the Fisher Information Matrix for the fixed effects (Fth) could not be inverted, so no confidence intervals for the optimised parameters are available.

```
illparms(f_saem_3) |> kable()
```

	const	tc
fomc_path_2	E	
dfop_path_2		
sforb_path_2		

```
anova(f_saem_3) |> kable(digits = 1)
```

	npar	AIC	BIC	Lik
fomc_path_2 tc	19	2250.9	2243.5	-1106.5
dfop_path_2 const	20	2281.7	2273.9	-1120.8
sforb_path_2 const	20	2279.5	2271.7	-1119.7
dfop_path_2 tc	20	2231.5	2223.7	-1095.8
sforb_path_2 tc	20	2235.7	2227.9	-1097.9

While the AIC and BIC values of the best fit (DFOP pathway fit with two-component error) are lower than in the previous fits with the alternative pathway, the practical value of these refined evaluations is limited as no confidence intervals are obtained.

Conclusion

It was demonstrated that a relatively complex transformation pathway with parallel formation of two primary metabolites and one secondary metabolite can be fitted even if the data in the individual datasets are quite different and partly only cover the formation phase.

The run times of the pathway fits were several hours, limiting the practical feasibility of iterative refinements based on ill-defined parameters and of alternative checks of parameter identifiability based on multistart runs.

Acknowledgements

The helpful comments by Janina Wöltjen of the German Environment Agency are gratefully acknowledged.

Appendix

Plots of fits that were not refined further

```
plot(f_saem_1[["sfo_path_1", "tc"]])
```

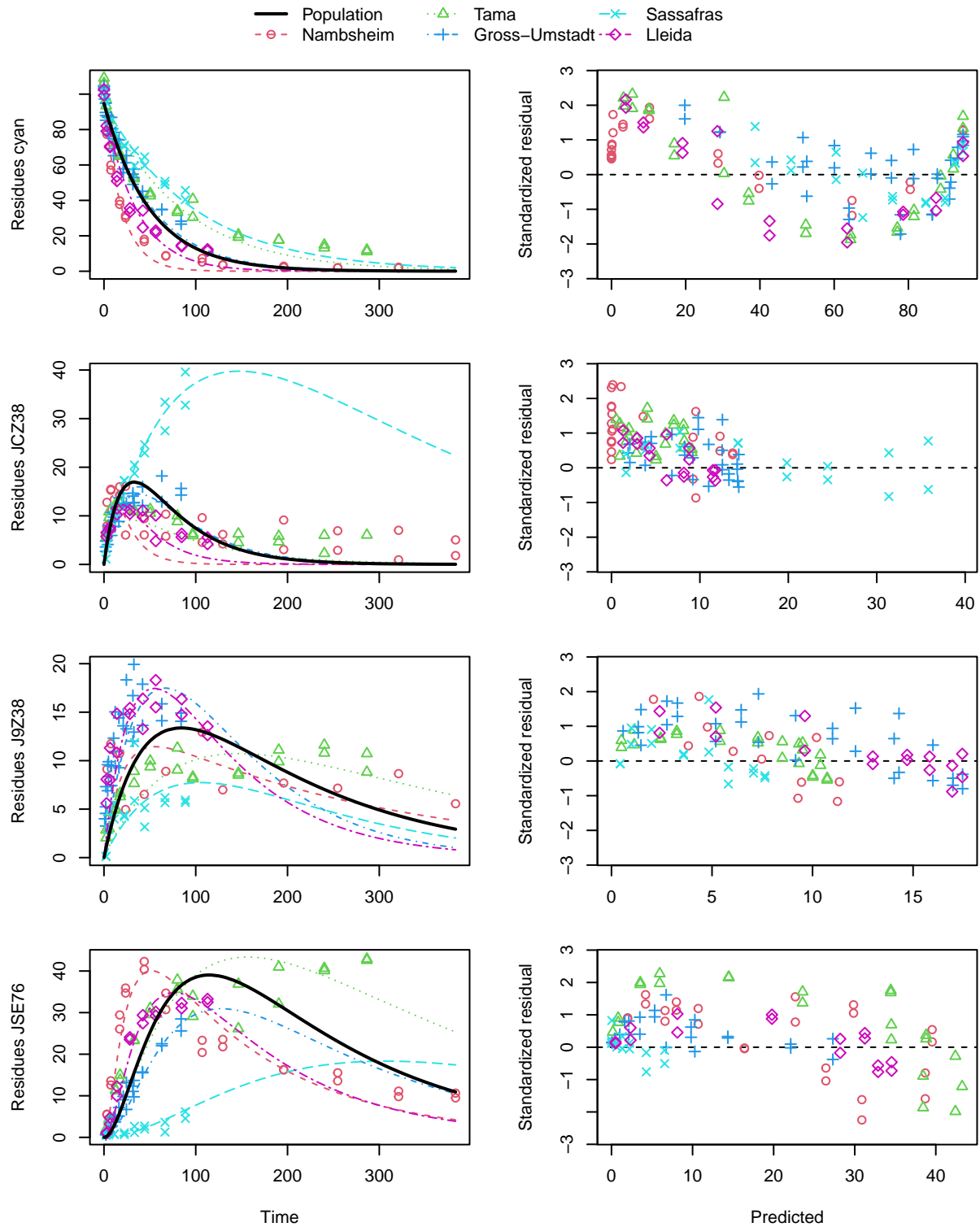


Figure 6: SFO pathway fit with two-component error

```
plot(f_saem_1[["fomc_path_1", "tc"]])
```

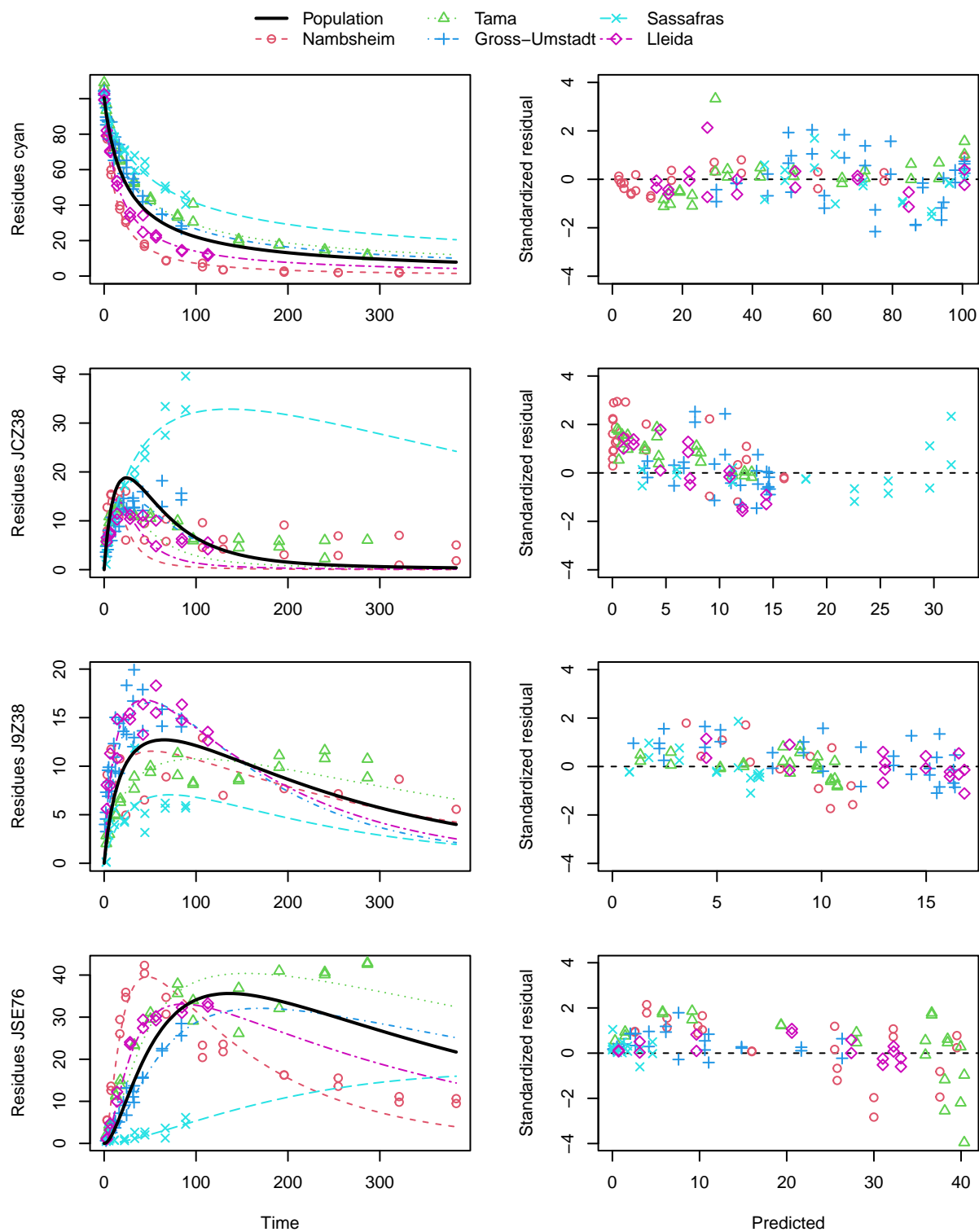


Figure 7: FOMC pathway fit with two-component error

```
plot(f_saem_1[["sforb_path_1", "tc"]])
```

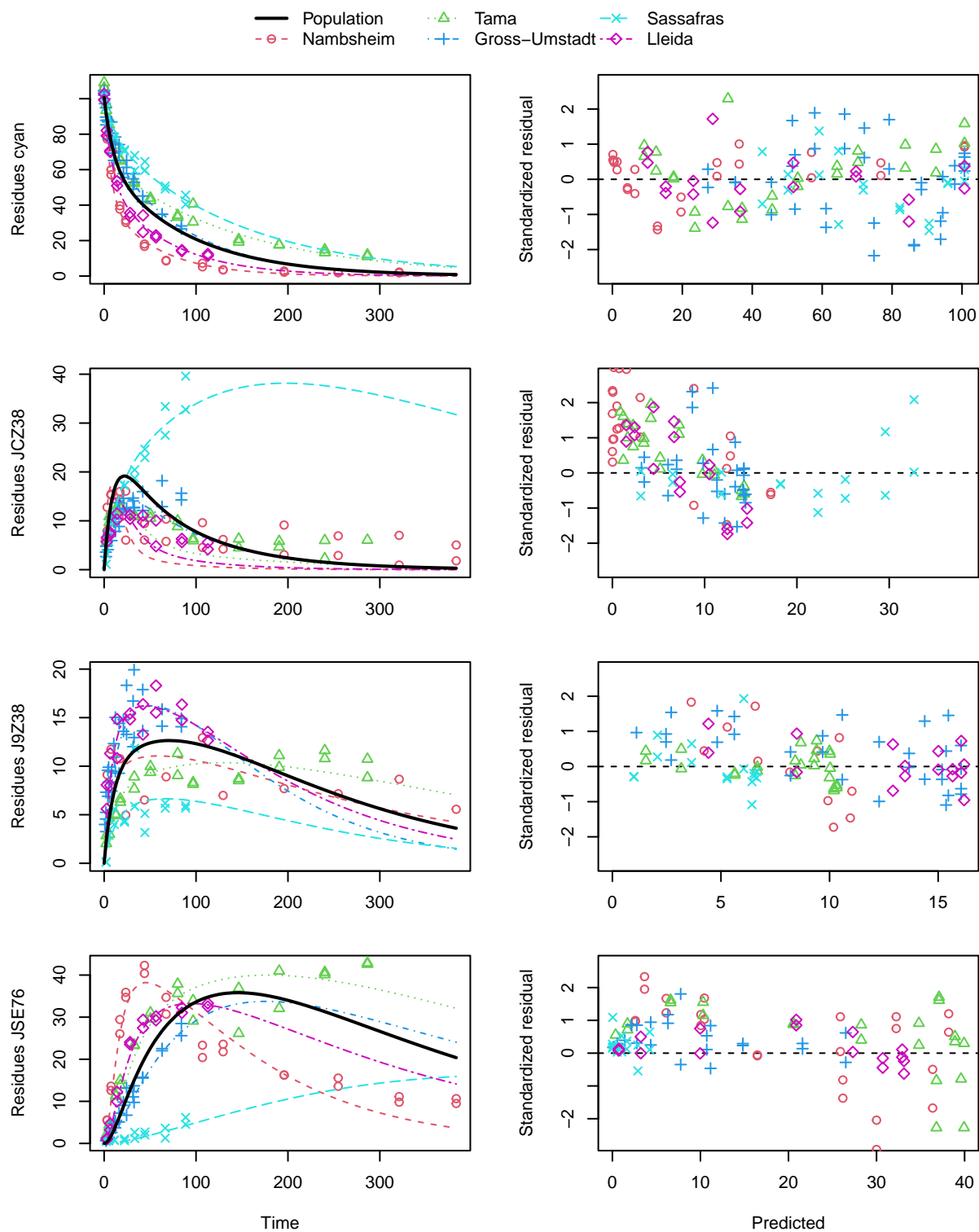


Figure 8: HS pathway fit with two-component error

Hierarchical fit listings

Pathway 1

Listing 1: Hierarchical SFO path 1 fit with constant variance

```
saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:55:16 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - k_cyan * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * k_cyan * cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * k_cyan * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 797.074 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0      log_k_cyan      log_k_JCZ38      log_k_J9Z38      log_k_JSE76
95.3304      -3.8459      -3.1305      -5.0678      -5.3196
f_cyan_ilr_1  f_cyan_ilr_2  f_JCZ38_qlogis
0.8158      22.5404      10.4289

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_cyan      log_k_JCZ38      log_k_J9Z38      log_k_JSE76
cyan_0      4.797      0.0000      0.000      0.000      0.000
log_k_cyan      0.000      0.9619      0.000      0.000      0.0000
log_k_JCZ38      0.000      0.0000      2.139      0.000      0.0000
log_k_J9Z38      0.000      0.0000      0.000      1.639      0.0000
log_k_JSE76      0.000      0.0000      0.000      0.000      0.7894
f_cyan_ilr_1      0.000      0.0000      0.000      0.000      0.0000
f_cyan_ilr_2      0.000      0.0000      0.000      0.000      0.0000
f_JCZ38_qlogis      0.000      0.0000      0.000      0.000      0.0000
      f_cyan_ilr_1  f_cyan_ilr_2  f_JCZ38_qlogis
cyan_0      0.0000      0.000      0.00
log_k_cyan      0.0000      0.000      0.00
log_k_JCZ38      0.0000      0.000      0.00
log_k_J9Z38      0.0000      0.000      0.00
log_k_JSE76      0.0000      0.000      0.00
f_cyan_ilr_1      0.7714      0.000      0.00
f_cyan_ilr_2      0.0000      8.684      0.00
f_JCZ38_qlogis      0.0000      0.000      13.48

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2693      2687      -1330

Optimised parameters:
      est.      lower      upper
cyan_0      95.0946      NA      NA
log_k_cyan      -3.8544      NA      NA
log_k_JCZ38      -3.0402      NA      NA
log_k_J9Z38      -5.0109      NA      NA
log_k_JSE76      -5.2857      NA      NA
f_cyan_ilr_1      0.8069      NA      NA
f_cyan_ilr_2      16.6623      NA      NA
f_JCZ38_qlogis      1.3602      NA      NA
a.1      4.8326      NA      NA
SD.log_k_cyan      0.5842      NA      NA
SD.log_k_JCZ38      1.2680      NA      NA
SD.log_k_J9Z38      0.3626      NA      NA
SD.log_k_JSE76      0.5244      NA      NA
SD.f_cyan_ilr_1      0.2752      NA      NA
```

SD.f_cyan_ilr_2	2.3556	NA	NA
SD.f_JCZ38_qlogis	0.2400	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_cyan	0.5842	NA	NA
SD.log_k_JCZ38	1.2680	NA	NA
SD.log_k_J9Z38	0.3626	NA	NA
SD.log_k_JSE76	0.5244	NA	NA
SD.f_cyan_ilr_1	0.2752	NA	NA
SD.f_cyan_ilr_2	2.3556	NA	NA
SD.f_JCZ38_qlogis	0.2400	NA	NA

Variance model:

	est.	lower	upper
a.1	4.833	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	95.094581	NA	NA
k_cyan	0.021186	NA	NA
k_JCZ38	0.047825	NA	NA
k_J9Z38	0.006665	NA	NA
k_JSE76	0.005063	NA	NA
f_cyan_to_JCZ38	0.757885	NA	NA
f_cyan_to_J9Z38	0.242115	NA	NA
f_JCZ38_to_JSE76	0.795792	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	7.579e-01
cyan_J9Z38	2.421e-01
cyan_sink	5.877e-10
JCZ38_JSE76	7.958e-01
JCZ38_sink	2.042e-01

Estimated disappearance times:

	DT50	DT90
cyan	32.72	108.68
JCZ38	14.49	48.15
J9Z38	103.99	345.46
JSE76	136.90	454.76

Listing 2: Hierarchical SFO path 1 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:56:15 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - k_cyan * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * k_cyan * cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * k_cyan * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 855.471 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0      log_k_cyan      log_k_JCZ38      log_k_J9Z38      log_k_JSE76
96.0039      -3.8907      -3.1276      -5.0069      -4.9367
f_cyan_ilr_1  f_cyan_ilr_2  f_JCZ38_qlogis
0.7937      20.0030      15.1336

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_cyan      log_k_JCZ38      log_k_J9Z38      log_k_JSE76
cyan_0      4.859      0.000      0.00      0.00      0.0000
log_k_cyan      0.000      0.962      0.00      0.00      0.0000
log_k_JCZ38      0.000      0.000      0.000      2.04      0.0000
log_k_J9Z38      0.000      0.000      0.00      1.72      0.0000
log_k_JSE76      0.000      0.000      0.00      0.00      0.9076
f_cyan_ilr_1      0.000      0.000      0.00      0.00      0.0000
f_cyan_ilr_2      0.000      0.000      0.00      0.00      0.0000
f_JCZ38_qlogis      0.000      0.000      0.00      0.00      0.0000
      f_cyan_ilr_1  f_cyan_ilr_2  f_JCZ38_qlogis
cyan_0      0.0000      0.000      0.00      0.00
log_k_cyan      0.0000      0.000      0.00
log_k_JCZ38      0.0000      0.000      0.00
log_k_J9Z38      0.0000      0.000      0.00
log_k_JSE76      0.0000      0.000      0.00
f_cyan_ilr_1      0.7598      0.000      0.00
f_cyan_ilr_2      0.0000      7.334      0.00
f_JCZ38_qlogis      0.0000      0.000      11.78

Starting values for error model parameters:
a.1 b.1
1 1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2658 2651 -1312

Optimised parameters:
      est.      lower      upper
cyan_0      94.72923      NA      NA
log_k_cyan      -3.91670      NA      NA
log_k_JCZ38      -3.12917      NA      NA
log_k_J9Z38      -5.06070      NA      NA
log_k_JSE76      -5.09254      NA      NA
f_cyan_ilr_1      0.81116      NA      NA
f_cyan_ilr_2      39.97850      NA      NA
f_JCZ38_qlogis      3.09728      NA      NA
a.1      3.95044      NA      NA
b.1      0.07998      NA      NA
SD.log_k_cyan      0.58855      NA      NA
SD.log_k_JCZ38      1.29753      NA      NA
SD.log_k_J9Z38      0.62851      NA      NA
SD.log_k_JSE76      0.37235      NA      NA
SD.f_cyan_ilr_1      0.37346      NA      NA
SD.f_cyan_ilr_2      1.41667      NA      NA
SD.f_JCZ38_qlogis      1.81467      NA      NA

Correlation is not available

```

```

Random effects:
      est. lower upper
SD.log_k_cyan    0.5886    NA    NA
SD.log_k_JCZ38   1.2975    NA    NA
SD.log_k_J9Z38   0.6285    NA    NA
SD.log_k_JSE76   0.3724    NA    NA
SD.f_cyan_ilr_1  0.3735    NA    NA
SD.f_cyan_ilr_2  1.4167    NA    NA
SD.f_JCZ38_qlogis 1.8147    NA    NA

Variance model:
      est. lower upper
a.1 3.95044    NA    NA
b.1 0.07998    NA    NA

Backtransformed parameters:
      est. lower upper
cyan_0      94.729229    NA    NA
k_cyan       0.019907    NA    NA
k_JCZ38      0.043754    NA    NA
k_J9Z38      0.006341    NA    NA
k_JSE76      0.006142    NA    NA
f_cyan_to_JCZ38 0.758991    NA    NA
f_cyan_to_J9Z38 0.241009    NA    NA
f_JCZ38_to_JSE76 0.956781    NA    NA

Resulting formation fractions:
      ff
cyan_JCZ38  0.75899
cyan_J9Z38  0.24101
cyan_sink   0.00000
JCZ38_JSE76 0.95678
JCZ38_sink  0.04322

Estimated disappearance times:
      DT50  DT90
cyan    34.82 115.67
JCZ38   15.84  52.63
J9Z38  109.31 363.12
JSE76  112.85 374.87

```

Listing 3: Hierarchical FOMC path 1 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:57:07 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - (alpha/beta) * 1/((time/beta) + 1) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 908.077 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
101.2314      -3.3680      -5.1108      -5.9416      0.7144
      f_cyan_ilr_2 f_JCZ38_qlogis      log_alpha      log_beta
       7.3870      15.7604      -0.1791      2.9811

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
5.416      0.000      0.000      0.000      0.0000
log_k_JCZ38      0.000      2.439      0.000      0.000      0.0000
log_k_J9Z38      0.000      0.000      1.700      0.000      0.0000
log_k_JSE76      0.000      0.000      0.000      1.856      0.0000
f_cyan_ilr_1      0.000      0.000      0.000      0.000      0.7164
f_cyan_ilr_2      0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis      0.000      0.000      0.000      0.000      0.0000
log_alpha      0.000      0.000      0.000      0.000      0.0000
log_beta      0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis      log_alpha      log_beta
cyan_0      0.00      0.00      0.0000      0.0000
log_k_JCZ38      0.00      0.00      0.0000      0.0000
log_k_J9Z38      0.00      0.00      0.0000      0.0000
log_k_JSE76      0.00      0.00      0.0000      0.0000
f_cyan_ilr_1      0.00      0.00      0.0000      0.0000
f_cyan_ilr_2      12.33      0.00      0.0000      0.0000
f_JCZ38_qlogis      0.00      20.42      0.0000      0.0000
log_alpha      0.00      0.00      0.4144      0.0000
log_beta      0.00      0.00      0.0000      0.5077

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2428 2421 -1196

Optimised parameters:
      est.      lower      upper
cyan_0      101.0225 98.306270 103.7387
log_k_JCZ38      -3.3786 -4.770657 -1.9866
log_k_J9Z38      -5.2603 -5.902085 -4.6186
log_k_JSE76      -6.1427 -7.318336 -4.9671
f_cyan_ilr_1      0.7437 0.421215 1.0663
f_cyan_ilr_2      0.9108 0.267977 1.5537
f_JCZ38_qlogis      2.0487 0.524897 3.5724
log_alpha      -0.2268 -0.618049 0.1644
log_beta      2.8986 2.700701 3.0964
a.1      3.4058 3.169913 3.6416
SD.cyan_0      2.5279 0.454190 4.6016
SD.log_k_JCZ38      1.5636 0.572824 2.5543
SD.log_k_J9Z38      0.5316 -0.004405 1.0677
SD.log_k_JSE76      0.9903 0.106325 1.8742
SD.f_cyan_ilr_1      0.3464 0.112066 0.5807

```

```

SD.f_cyan_ilr_2      0.2804 -0.393900  0.9546
SD.f_JCZ38_qlogis    0.9416 -0.152986  2.0362
SD.log_alpha         0.4273  0.161044  0.6936

Correlation:
      cyan_0  l__JCZ3  l__J9Z3  l__JSE7  f_cy__1  f_cy__2  f_JCZ38  log_lph
log_k_JCZ38    -0.0156
log_k_J9Z38    -0.0493  0.0073
log_k_JSE76    -0.0329  0.0018  0.0069
f_cyan_ilr_1   -0.0086  0.0180 -0.1406  0.0012
f_cyan_ilr_2   -0.2629  0.0779  0.2826  0.0274  0.0099
f_JCZ38_qlogis  0.0713 -0.0747 -0.0505  0.1169 -0.1022 -0.4893
log_alpha      -0.0556  0.0120  0.0336  0.0193  0.0036  0.0840 -0.0489
log_beta       -0.2898  0.0460  0.1305  0.0768  0.0190  0.4071 -0.1981  0.2772

Random effects:
      est.      lower  upper
SD.cyan_0      2.5279  0.454190 4.6016
SD.log_k_JCZ38 1.5636  0.572824 2.5543
SD.log_k_J9Z38 0.5316 -0.004405 1.0677
SD.log_k_JSE76 0.9903  0.106325 1.8742
SD.f_cyan_ilr_1 0.3464  0.112066 0.5807
SD.f_cyan_ilr_2 0.2804 -0.393900 0.9546
SD.f_JCZ38_qlogis 0.9416 -0.152986 2.0362
SD.log_alpha    0.4273  0.161044 0.6936

Variance model:
      est. lower upper
a.1 3.406  3.17 3.642

Backtransformed parameters:
      est.      lower  upper
cyan_0      1.010e+02 9.831e+01 1.037e+02
k_JCZ38      3.409e-02 8.475e-03 1.372e-01
k_J9Z38      5.194e-03 2.734e-03 9.867e-03
k_JSE76      2.149e-03 6.633e-04 6.963e-03
f_cyan_to_JCZ38 6.481e-01      NA      NA
f_cyan_to_J9Z38 2.264e-01      NA      NA
f_JCZ38_to_JSE76 8.858e-01 6.283e-01 9.727e-01
alpha        7.971e-01 5.390e-01 1.179e+00
beta         1.815e+01 1.489e+01 2.212e+01

Resulting formation fractions:
      ff
cyan_JCZ38  0.6481
cyan_J9Z38  0.2264
cyan_sink   0.1255
JCZ38_JSE76 0.8858
JCZ38_sink  0.1142

Estimated disappearance times:
      DT50  DT90 DT50back
cyan  25.15 308.01  92.72
JCZ38 20.33  67.54    NA
J9Z38 133.46 443.35    NA
JSE76 322.53 1071.42    NA

```

Listing 4: Hierarchical FOMC path 1 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:58:12 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - (alpha/beta) * 1/((time/beta) + 1) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 972.457 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0    log_k_JCZ38    log_k_J9Z38    log_k_JSE76    f_cyan_ilr_1
101.13827    -3.32493    -5.08921    -5.93478    0.71330
f_cyan_ilr_2 f_JCZ38_qlogis    log_alpha    log_beta
10.05989    12.79248    -0.09621    3.10646

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0    log_k_JCZ38    log_k_J9Z38    log_k_JSE76    f_cyan_ilr_1
5.643    0.000    0.000    0.000    0.00    0.0000
log_k_JCZ38    0.000    2.319    0.000    0.00    0.0000
log_k_J9Z38    0.000    0.000    1.731    0.00    0.0000
log_k_JSE76    0.000    0.000    0.000    1.86    0.0000
f_cyan_ilr_1    0.000    0.000    0.000    0.00    0.7186
f_cyan_ilr_2    0.000    0.000    0.000    0.00    0.0000
f_JCZ38_qlogis    0.000    0.000    0.000    0.00    0.0000
log_alpha    0.000    0.000    0.000    0.00    0.0000
log_beta    0.000    0.000    0.000    0.00    0.0000
      f_cyan_ilr_2    f_JCZ38_qlogis    log_alpha    log_beta
cyan_0    0.00    0.00    0.0000    0.0000
log_k_JCZ38    0.00    0.00    0.0000    0.0000
log_k_J9Z38    0.00    0.00    0.0000    0.0000
log_k_JSE76    0.00    0.00    0.0000    0.0000
f_cyan_ilr_1    0.00    0.00    0.0000    0.0000
f_cyan_ilr_2    12.49    0.00    0.0000    0.0000
f_JCZ38_qlogis    0.00    20.19    0.0000    0.0000
log_alpha    0.00    0.00    0.3142    0.0000
log_beta    0.00    0.00    0.0000    0.7331

Starting values for error model parameters:
a.1 b.1
1 1

Results:

Likelihood computed by importance sampling
      AIC    BIC    logLik
2423 2416 -1193

Optimised parameters:
      est.    lower    upper
cyan_0    100.57649    NA    NA
log_k_JCZ38    -3.46250    NA    NA
log_k_J9Z38    -5.24442    NA    NA
log_k_JSE76    -5.75229    NA    NA
f_cyan_ilr_1    0.68480    NA    NA
f_cyan_ilr_2    0.61670    NA    NA
f_JCZ38_qlogis    87.97407    NA    NA
log_alpha    -0.15699    NA    NA
log_beta    3.01540    NA    NA
a.1    3.11518    NA    NA
b.1    0.04445    NA    NA
SD.log_k_JCZ38    1.40732    NA    NA
SD.log_k_J9Z38    0.56510    NA    NA
SD.log_k_JSE76    0.72067    NA    NA
SD.f_cyan_ilr_1    0.31199    NA    NA

```

SD.f_cyan_ilr_2	0.36894	NA	NA
SD.f_JCZ38_qlogis	6.92892	NA	NA
SD.log_alpha	0.25662	NA	NA
SD.log_beta	0.35845	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.4073	NA	NA
SD.log_k_J9Z38	0.5651	NA	NA
SD.log_k_JSE76	0.7207	NA	NA
SD.f_cyan_ilr_1	0.3120	NA	NA
SD.f_cyan_ilr_2	0.3689	NA	NA
SD.f_JCZ38_qlogis	6.9289	NA	NA
SD.log_alpha	0.2566	NA	NA
SD.log_beta	0.3585	NA	NA

Variance model:

	est.	lower	upper
a.1	3.11518	NA	NA
b.1	0.04445	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.006e+02	NA	NA
k_JCZ38	3.135e-02	NA	NA
k_J9Z38	5.277e-03	NA	NA
k_JSE76	3.175e-03	NA	NA
f_cyan_to_JCZ38	5.991e-01	NA	NA
f_cyan_to_J9Z38	2.275e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
alpha	8.547e-01	NA	NA
beta	2.040e+01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.5991
cyan_J9Z38	0.2275
cyan_sink	0.1734
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000

Estimated disappearance times:

	DT50	DT90	DT50back
cyan	25.50	281.29	84.68
JCZ38	22.11	73.44	NA
J9Z38	131.36	436.35	NA
JSE76	218.28	725.11	NA

Listing 5: Hierarchical DFOP path 1 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:58:36 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 996.251 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
102.0644      -3.4008      -5.0024      -5.8613      0.6855
f_cyan_ilr_2 f_JCZ38_qlogis  log_k1      log_k2      g_qlogis
1.2365      13.7245      -1.8641      -4.5063      -0.6468

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      4.466      0.000      0.000      0.000      0.0000
log_k_JCZ38  0.000      2.382      0.000      0.000      0.0000
log_k_J9Z38  0.000      0.000      1.595      0.000      0.0000
log_k_JSE76  0.000      0.000      0.000      1.245      0.0000
f_cyan_ilr_1 0.000      0.000      0.000      0.000      0.6852
f_cyan_ilr_2 0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis 0.000      0.000      0.000      0.000      0.0000
log_k1      0.000      0.000      0.000      0.000      0.0000
log_k2      0.000      0.000      0.000      0.000      0.0000
g_qlogis     0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis log_k1 log_k2 g_qlogis
cyan_0      0.00      0.00 0.0000 0.0000 0.000
log_k_JCZ38  0.00      0.00 0.0000 0.0000 0.000
log_k_J9Z38  0.00      0.00 0.0000 0.0000 0.000
log_k_JSE76  0.00      0.00 0.0000 0.0000 0.000
f_cyan_ilr_1 0.00      0.00 0.0000 0.0000 0.000
f_cyan_ilr_2 1.28      0.00 0.0000 0.0000 0.000
f_JCZ38_qlogis 0.00      16.11 0.0000 0.0000 0.000
log_k1      0.00      0.00 0.9866 0.0000 0.000
log_k2      0.00      0.00 0.0000 0.5953 0.000
g_qlogis     0.00      0.00 0.0000 0.0000 1.583

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling
      AIC  BIC logLik
2403 2395 -1182

Optimised parameters:
      est. lower upper
cyan_0      102.6079  NA   NA
log_k_JCZ38  -3.4855  NA   NA
log_k_J9Z38  -5.1686  NA   NA
log_k_JSE76  -5.6697  NA   NA
f_cyan_ilr_1  0.6714  NA   NA
f_cyan_ilr_2  0.4986  NA   NA
f_JCZ38_qlogis 55.4760  NA   NA
log_k1      -1.8409  NA   NA
log_k2      -4.4915  NA   NA

```

g_qlogis	-0.6403	NA	NA
a.1	3.2387	NA	NA
SD.log_k_JCZ38	1.4524	NA	NA
SD.log_k_J9Z38	0.5151	NA	NA
SD.log_k_JSE76	0.6514	NA	NA
SD.f_cyan_ilr_1	0.3023	NA	NA
SD.f_cyan_ilr_2	0.2959	NA	NA
SD.f_JCZ38_qlogis	1.9984	NA	NA
SD.log_k1	0.5188	NA	NA
SD.log_k2	0.3894	NA	NA
SD.g_qlogis	0.8579	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.4524	NA	NA
SD.log_k_J9Z38	0.5151	NA	NA
SD.log_k_JSE76	0.6514	NA	NA
SD.f_cyan_ilr_1	0.3023	NA	NA
SD.f_cyan_ilr_2	0.2959	NA	NA
SD.f_JCZ38_qlogis	1.9984	NA	NA
SD.log_k1	0.5188	NA	NA
SD.log_k2	0.3894	NA	NA
SD.g_qlogis	0.8579	NA	NA

Variance model:

	est.	lower	upper
a.1	3.239	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.026e+02	NA	NA
k_JCZ38	3.064e-02	NA	NA
k_J9Z38	5.692e-03	NA	NA
k_JSE76	3.449e-03	NA	NA
f_cyan_to_JCZ38	5.798e-01	NA	NA
f_cyan_to_J9Z38	2.243e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
k1	1.587e-01	NA	NA
k2	1.120e-02	NA	NA
g	3.452e-01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.5798
cyan_J9Z38	0.2243
cyan_sink	0.1958
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	25.21	167.73	50.49	4.368	61.87
JCZ38	22.62	75.15	NA	NA	NA
J9Z38	121.77	404.50	NA	NA	NA
JSE76	200.98	667.64	NA	NA	NA

Listing 6: Hierarchical DFOP path 1 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:03:08 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1268.545 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
101.3964    -3.3626    -4.9792    -5.8727      0.6814
f_cyan_ilr_2 f_JCZ38_qlogis  log_k1      log_k2      g_qlogis
  6.7799    13.7245    -1.9222    -4.5035    -0.7172

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      5.317      0.000      0.000      0.000      0.0000
log_k_JCZ38  0.000      2.272      0.000      0.000      0.0000
log_k_J9Z38  0.000      0.000      1.633      0.000      0.0000
log_k_JSE76  0.000      0.000      0.000      1.271      0.0000
f_cyan_ilr_1 0.000      0.000      0.000      0.000      0.6838
f_cyan_ilr_2 0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis 0.000      0.000      0.000      0.000      0.0000
log_k1        0.000      0.000      0.000      0.000      0.0000
log_k2        0.000      0.000      0.000      0.000      0.0000
g_qlogis      0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis log_k1 log_k2 g_qlogis
cyan_0      0.00      0.00 0.0000 0.0000 0.000
log_k_JCZ38 0.00      0.00 0.0000 0.0000 0.000
log_k_J9Z38 0.00      0.00 0.0000 0.0000 0.000
log_k_JSE76 0.00      0.00 0.0000 0.0000 0.000
f_cyan_ilr_1 0.00      0.00 0.0000 0.0000 0.000
f_cyan_ilr_2 11.77     0.00 0.0000 0.0000 0.000
f_JCZ38_qlogis 0.00     16.11 0.0000 0.0000 0.000
log_k1       0.00      0.00 0.9496 0.0000 0.000
log_k2       0.00      0.00 0.0000 0.5846 0.000
g_qlogis     0.00      0.00 0.0000 0.0000 1.719

Starting values for error model parameters:
a.1 b.1
  1  1

Results:

Likelihood computed by importance sampling
      AIC  BIC logLik
2398 2390 -1179

Optimised parameters:
      est. lower upper
cyan_0      100.8076  NA   NA
log_k_JCZ38  -3.4684  NA   NA
log_k_J9Z38  -5.0844  NA   NA
log_k_JSE76  -5.5743  NA   NA
f_cyan_ilr_1   0.6669  NA   NA
f_cyan_ilr_2   0.7912  NA   NA
f_JCZ38_qlogis 84.1825  NA   NA
log_k1       -2.1671  NA   NA
log_k2       -4.5447  NA   NA

```

g_qlogis	-0.5631	NA	NA
a.1	2.9627	NA	NA
b.1	0.0444	NA	NA
SD.log_k_JCZ38	1.4044	NA	NA
SD.log_k_J9Z38	0.6410	NA	NA
SD.log_k_JSE76	0.5391	NA	NA
SD.f_cyan_ilr_1	0.3203	NA	NA
SD.f_cyan_ilr_2	0.5038	NA	NA
SD.f_JCZ38_qlogis	3.5865	NA	NA
SD.log_k2	0.3119	NA	NA
SD.g_qlogis	0.8276	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.4044	NA	NA
SD.log_k_J9Z38	0.6410	NA	NA
SD.log_k_JSE76	0.5391	NA	NA
SD.f_cyan_ilr_1	0.3203	NA	NA
SD.f_cyan_ilr_2	0.5038	NA	NA
SD.f_JCZ38_qlogis	3.5865	NA	NA
SD.log_k2	0.3119	NA	NA
SD.g_qlogis	0.8276	NA	NA

Variance model:

	est.	lower	upper
a.1	2.9627	NA	NA
b.1	0.0444	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.008e+02	NA	NA
k_JCZ38	3.117e-02	NA	NA
k_J9Z38	6.193e-03	NA	NA
k_JSE76	3.794e-03	NA	NA
f_cyan_to_JCZ38	6.149e-01	NA	NA
f_cyan_to_J9Z38	2.395e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
k1	1.145e-01	NA	NA
k2	1.062e-02	NA	NA
g	3.628e-01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.6149
cyan_J9Z38	0.2395
cyan_sink	0.1456
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	26.26	174.32	52.47	6.053	65.25
JCZ38	22.24	73.88	NA	NA	NA
J9Z38	111.93	371.82	NA	NA	NA
JSE76	182.69	606.88	NA	NA	NA

Listing 7: Hierarchical SFORB path 1 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:58:51 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
                cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
                cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
                * JCZ38
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
                * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1011.276 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      102.0643      -2.8987      -2.7077
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
      -3.4717      -3.4008      -5.0024
      log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
      -5.8613      0.6855      1.2366
      f_JCZ38_qlogis
      13.7418

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
cyan_free_0      4.466      0.0000      0.000
log_k_cyan_free      0.000      0.6158      0.000
log_k_cyan_free_bound      0.000      0.0000      1.463
log_k_cyan_bound_free      0.000      0.0000      0.000
log_k_JCZ38      0.000      0.0000      0.000
log_k_J9Z38      0.000      0.0000      0.000
log_k_JSE76      0.000      0.0000      0.000
f_cyan_ilr_1      0.000      0.0000      0.000
f_cyan_ilr_2      0.000      0.0000      0.000
f_JCZ38_qlogis      0.000      0.0000      0.000
      log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000      0.000      0.000      0.000
log_k_cyan_free      0.000      0.000      0.000      0.000
log_k_cyan_free_bound      0.000      0.000      0.000      0.000
log_k_cyan_bound_free      1.058      0.000      0.000      0.000
log_k_JCZ38      0.000      2.382      0.000      0.000
log_k_J9Z38      0.000      0.000      1.595      0.000
log_k_JSE76      0.000      0.000      0.000      1.245
f_cyan_ilr_1      0.000      0.000      0.000      0.000
f_cyan_ilr_2      0.000      0.000      0.000      0.000
f_JCZ38_qlogis      0.000      0.000      0.000      0.000
      f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis
cyan_free_0      0.0000      0.00      0.00
log_k_cyan_free      0.0000      0.00      0.00
log_k_cyan_free_bound      0.0000      0.00      0.00
log_k_cyan_bound_free      0.0000      0.00      0.00
log_k_JCZ38      0.0000      0.00      0.00
log_k_J9Z38      0.0000      0.00      0.00
log_k_JSE76      0.0000      0.00      0.00
f_cyan_ilr_1      0.6852      0.00      0.00
f_cyan_ilr_2      0.0000      1.28      0.00
f_JCZ38_qlogis      0.0000      0.00      16.14

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling

```

```

AIC BIC logLik
2401 2394 -1181

Optimised parameters:
      est. lower upper
cyan_free_0      102.7803 NA NA
log_k_cyan_free    -2.8068 NA NA
log_k_cyan_free_bound -2.5714 NA NA
log_k_cyan_bound_free -3.4426 NA NA
log_k_JCZ38       -3.4994 NA NA
log_k_J9Z38       -5.1148 NA NA
log_k_JSE76       -5.6335 NA NA
f_cyan_ilr_1       0.6597 NA NA
f_cyan_ilr_2       0.5132 NA NA
f_JCZ38_qlogis     37.2090 NA NA
a.1                3.2367 NA NA
SD.log_k_cyan_free  0.3161 NA NA
SD.log_k_cyan_free_bound 0.8103 NA NA
SD.log_k_cyan_bound_free 0.5554 NA NA
SD.log_k_JCZ38      1.4858 NA NA
SD.log_k_J9Z38      0.5859 NA NA
SD.log_k_JSE76      0.6195 NA NA
SD.f_cyan_ilr_1     0.3118 NA NA
SD.f_cyan_ilr_2     0.3344 NA NA
SD.f_JCZ38_qlogis   0.5518 NA NA

Correlation is not available

Random effects:
      est. lower upper
SD.log_k_cyan_free    0.3161 NA NA
SD.log_k_cyan_free_bound 0.8103 NA NA
SD.log_k_cyan_bound_free 0.5554 NA NA
SD.log_k_JCZ38        1.4858 NA NA
SD.log_k_J9Z38        0.5859 NA NA
SD.log_k_JSE76        0.6195 NA NA
SD.f_cyan_ilr_1       0.3118 NA NA
SD.f_cyan_ilr_2       0.3344 NA NA
SD.f_JCZ38_qlogis     0.5518 NA NA

Variance model:
      est. lower upper
a.1 3.237 NA NA

Backtransformed parameters:
      est. lower upper
cyan_free_0      1.028e+02 NA NA
k_cyan_free       6.040e-02 NA NA
k_cyan_free_bound  7.643e-02 NA NA
k_cyan_bound_free  3.198e-02 NA NA
k_JCZ38           3.022e-02 NA NA
k_J9Z38           6.007e-03 NA NA
k_JSE76           3.576e-03 NA NA
f_cyan_free_to_JCZ38 5.787e-01 NA NA
f_cyan_free_to_J9Z38 2.277e-01 NA NA
f_JCZ38_to_JSE76   1.000e+00 NA NA

Estimated Eigenvalues of SFORB model(s):
cyan_b1 cyan_b2 cyan_g
0.15646 0.01235 0.33341

Resulting formation fractions:
      ff
cyan_free_JCZ38 0.5787
cyan_free_J9Z38 0.2277
cyan_free_sink  0.1936
cyan_free       1.0000
JCZ38_JSE76     1.0000
JCZ38_sink      0.0000

Estimated disappearance times:
      DT50 DT90 DT50back DT50_cyan_b1 DT50_cyan_b2
cyan   24.48 153.7  46.26      4.43      56.15
JCZ38  22.94  76.2   NA      NA      NA
J9Z38 115.39 383.3   NA      NA      NA
JSE76 193.84 643.9   NA      NA      NA

```

Listing 8: Hierarchical SFORB path 1 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:03:05 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
               cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
               cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
               * JCZ38
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
               * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1265.016 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
               cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
               101.3964          -2.9881          -2.7949
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
               -3.4376          -3.3626          -4.9792
               log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
               -5.8727          0.6814          6.8139
               f_JCZ38_qlogis
               13.7419

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
               cyan_free_0 log_k_cyan_free log_k_cyan_free_bound
cyan_free_0      5.317      0.0000      0.000
log_k_cyan_free      0.000      0.7301      0.000
log_k_cyan_free_bound      0.000      0.0000      1.384
log_k_cyan_bound_free      0.000      0.0000      0.000
log_k_JCZ38      0.000      0.0000      0.000
log_k_J9Z38      0.000      0.0000      0.000
log_k_JSE76      0.000      0.0000      0.000
f_cyan_ilr_1      0.000      0.0000      0.000
f_cyan_ilr_2      0.000      0.0000      0.000
f_JCZ38_qlogis      0.000      0.0000      0.000
               log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000      0.000      0.000      0.000
log_k_cyan_free      0.000      0.000      0.000      0.000
log_k_cyan_free_bound      0.000      0.000      0.000      0.000
log_k_cyan_bound_free      1.109      0.000      0.000      0.000
log_k_JCZ38      0.000      2.272      0.000      0.000
log_k_J9Z38      0.000      0.000      1.633      0.000
log_k_JSE76      0.000      0.000      0.000      1.271
f_cyan_ilr_1      0.000      0.000      0.000      0.000
f_cyan_ilr_2      0.000      0.000      0.000      0.000
f_JCZ38_qlogis      0.000      0.000      0.000      0.000
               f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis
cyan_free_0      0.0000      0.00      0.00
log_k_cyan_free      0.0000      0.00      0.00
log_k_cyan_free_bound      0.0000      0.00      0.00
log_k_cyan_bound_free      0.0000      0.00      0.00
log_k_JCZ38      0.0000      0.00      0.00
log_k_J9Z38      0.0000      0.00      0.00
log_k_JSE76      0.0000      0.00      0.00
f_cyan_ilr_1      0.6838      0.00      0.00
f_cyan_ilr_2      0.0000      11.84      0.00
f_JCZ38_qlogis      0.0000      0.00      16.14

Starting values for error model parameters:
a.1 b.1
  1  1

Results:

Likelihood computed by importance sampling

```

```

AIC BIC logLik
2400 2392 -1180

Optimised parameters:
               est. lower upper
cyan_free_0    100.69983    NA    NA
log_k_cyan_free -3.11584    NA    NA
log_k_cyan_free_bound -3.15216    NA    NA
log_k_cyan_bound_free -3.65986    NA    NA
log_k_JCZ38    -3.47811    NA    NA
log_k_J9Z38    -5.08835    NA    NA
log_k_JSE76    -5.55514    NA    NA
f_cyan_ilr_1    0.66764    NA    NA
f_cyan_ilr_2    0.78329    NA    NA
f_JCZ38_qlogis  25.35245    NA    NA
a.1             2.99088    NA    NA
b.1             0.04346    NA    NA
SD.log_k_cyan_free 0.48797    NA    NA
SD.log_k_cyan_bound_free 0.27243    NA    NA
SD.log_k_JCZ38    1.42450    NA    NA
SD.log_k_J9Z38    0.63496    NA    NA
SD.log_k_JSE76    0.55951    NA    NA
SD.f_cyan_ilr_1    0.32687    NA    NA
SD.f_cyan_ilr_2    0.48056    NA    NA
SD.f_JCZ38_qlogis 0.43818    NA    NA

Correlation is not available

Random effects:
               est. lower upper
SD.log_k_cyan_free 0.4880    NA    NA
SD.log_k_cyan_bound_free 0.2724    NA    NA
SD.log_k_JCZ38    1.4245    NA    NA
SD.log_k_J9Z38    0.6350    NA    NA
SD.log_k_JSE76    0.5595    NA    NA
SD.f_cyan_ilr_1    0.3269    NA    NA
SD.f_cyan_ilr_2    0.4806    NA    NA
SD.f_JCZ38_qlogis 0.4382    NA    NA

Variance model:
               est. lower upper
a.1 2.99088    NA    NA
b.1 0.04346    NA    NA

Backtransformed parameters:
               est. lower upper
cyan_free_0    1.007e+02    NA    NA
k_cyan_free    4.434e-02    NA    NA
k_cyan_free_bound 4.276e-02    NA    NA
k_cyan_bound_free 2.574e-02    NA    NA
k_JCZ38        3.087e-02    NA    NA
k_J9Z38        6.168e-03    NA    NA
k_JSE76        3.868e-03    NA    NA
f_cyan_free_to_JCZ38 6.143e-01    NA    NA
f_cyan_free_to_J9Z38 2.389e-01    NA    NA
f_JCZ38_to_JSE76 1.000e+00    NA    NA

Estimated Eigenvalues of SFORB model(s):
cyan_b1 cyan_b2 cyan_g
0.10161 0.01123 0.36636

Resulting formation fractions:
               ff
cyan_free_JCZ38 6.143e-01
cyan_free_J9Z38 2.389e-01
cyan_free_sink 1.468e-01
cyan_free      1.000e+00
JCZ38_JSE76    1.000e+00
JCZ38_sink     9.763e-12

Estimated disappearance times:
DT50 DT90 DT50back DT50_cyan_b1 DT50_cyan_b2
cyan 25.91 164.4 49.49 6.822 61.72
JCZ38 22.46 74.6 NA NA NA
J9Z38 112.37 373.3 NA NA NA
JSE76 179.22 595.4 NA NA NA

```


Listing 9: Hierarchical HS path 1 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:58:45 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ifelse(time <= tb, k1, k2) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ifelse(time <= tb, k1, k2) * cyan -
             k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * ifelse(time <= tb, k1, k2) * cyan -
             k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1005.559 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
102.8738      -3.4490      -4.9348      -5.5989      0.6469
      f_cyan_ilr_2 f_JCZ38_qlogis      log_k1      log_k2      log_tb
1.2854      9.7193      -2.9084      -4.1810      1.7813

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
cyan_0      5.409      0.00      0.00      0.00      0.0000
log_k_JCZ38      0.000      2.33      0.00      0.000      0.0000
log_k_J9Z38      0.000      0.00      1.59      0.000      0.0000
log_k_JSE76      0.000      0.00      0.00      1.006      0.0000
f_cyan_ilr_1      0.000      0.00      0.00      0.000      0.6371
f_cyan_ilr_2      0.000      0.00      0.00      0.000      0.0000
f_JCZ38_qlogis      0.000      0.00      0.00      0.000      0.0000
log_k1      0.000      0.00      0.00      0.000      0.0000
log_k2      0.000      0.00      0.00      0.000      0.0000
log_tb      0.000      0.00      0.00      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis log_k1 log_k2 log_tb
cyan_0      0.000      0.00 0.0000 0.0000 0.0000
log_k_JCZ38      0.000      0.00 0.0000 0.0000 0.0000
log_k_J9Z38      0.000      0.00 0.0000 0.0000 0.0000
log_k_JSE76      0.000      0.00 0.0000 0.0000 0.0000
f_cyan_ilr_1      0.000      0.00 0.0000 0.0000 0.0000
f_cyan_ilr_2      2.167      0.00 0.0000 0.0000 0.0000
f_JCZ38_qlogis      0.000      10.22 0.0000 0.0000 0.0000
log_k1      0.000      0.00 0.7003 0.0000 0.0000
log_k2      0.000      0.00 0.0000 0.8928 0.0000
log_tb      0.000      0.00 0.0000 0.0000 0.6774

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2427      2420      -1194

Optimised parameters:
      est.      lower      upper
cyan_0      101.84849      NA      NA
log_k_JCZ38      -3.47365      NA      NA
log_k_J9Z38      -5.10562      NA      NA
log_k_JSE76      -5.60318      NA      NA
f_cyan_ilr_1      0.66127      NA      NA
f_cyan_ilr_2      0.60283      NA      NA
f_JCZ38_qlogis      45.06408      NA      NA
log_k1      -3.10124      NA      NA
log_k2      -4.39028      NA      NA
log_tb      2.32256      NA      NA
a.1      3.32683      NA      NA
SD.log_k_JCZ38      1.41427      NA      NA
SD.log_k_J9Z38      0.54767      NA      NA

```

SD.log_k_JSE76	0.62147	NA	NA
SD.f_cyan_ilr_1	0.30189	NA	NA
SD.f_cyan_ilr_2	0.34960	NA	NA
SD.f_JCZ38_qlogis	0.04644	NA	NA
SD.log_k1	0.39534	NA	NA
SD.log_k2	0.43468	NA	NA
SD.log_tb	0.60781	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.41427	NA	NA
SD.log_k_J9Z38	0.54767	NA	NA
SD.log_k_JSE76	0.62147	NA	NA
SD.f_cyan_ilr_1	0.30189	NA	NA
SD.f_cyan_ilr_2	0.34960	NA	NA
SD.f_JCZ38_qlogis	0.04644	NA	NA
SD.log_k1	0.39534	NA	NA
SD.log_k2	0.43468	NA	NA
SD.log_tb	0.60781	NA	NA

Variance model:

	est.	lower	upper
a.1	3.327	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.018e+02	NA	NA
k_JCZ38	3.100e-02	NA	NA
k_J9Z38	6.063e-03	NA	NA
k_JSE76	3.686e-03	NA	NA
f_cyan_to_JCZ38	5.910e-01	NA	NA
f_cyan_to_J9Z38	2.320e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
k1	4.499e-02	NA	NA
k2	1.240e-02	NA	NA
tb	1.020e+01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.591
cyan_J9Z38	0.232
cyan_sink	0.177
JCZ38_JSE76	1.000
JCZ38_sink	0.000

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	29.09	158.91	47.84	15.41	55.91
JCZ38	22.36	74.27	NA	NA	NA
J9Z38	114.33	379.80	NA	NA	NA
JSE76	188.04	624.66	NA	NA	NA

Listing 10: Hierarchical HS path 1 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 00:58:06 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ifelse(time <= tb, k1, k2) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ifelse(time <= tb, k1, k2) * cyan -
            k_JCZ38 * JCZ38
d_J9Z38/dt = + f_cyan_to_J9Z38 * ifelse(time <= tb, k1, k2) * cyan -
            k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 966.022 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
101.168         -3.358         -4.941         -5.794         0.676
f_cyan_ilr_2 f_JCZ38_qlogis      log_k1      log_k2      log_tb
5.740          13.863         -3.147         -4.262         2.173

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
5.79          0.000          0.000          0.000          0.000
log_k_JCZ38      0.00          2.271          0.000          0.000          0.000
log_k_J9Z38      0.00          0.000          1.614          0.000          0.000
log_k_JSE76      0.00          0.000          0.000          1.264          0.000
f_cyan_ilr_1      0.00          0.000          0.000          0.000          0.6761
f_cyan_ilr_2      0.00          0.000          0.000          0.000          0.000
f_JCZ38_qlogis    0.00          0.000          0.000          0.000          0.000
log_k1            0.00          0.000          0.000          0.000          0.000
log_k2            0.00          0.000          0.000          0.000          0.000
log_tb            0.00          0.000          0.000          0.000          0.000
f_cyan_ilr_2      0.000          0.00          0.000          0.000          0.000
log_k_JCZ38      0.000          0.00          0.000          0.000          0.000
log_k_J9Z38      0.000          0.00          0.000          0.000          0.000
log_k_JSE76      0.000          0.00          0.000          0.000          0.000
f_cyan_ilr_1      0.000          0.00          0.000          0.000          0.000
f_cyan_ilr_2      9.572          0.00          0.000          0.000          0.000
f_JCZ38_qlogis    0.000          19.19          0.000          0.000          0.000
log_k1            0.000          0.00          0.8705          0.000          0.000
log_k2            0.000          0.00          0.000          0.9288          0.000
log_tb            0.000          0.00          0.000          0.000          1.065

Starting values for error model parameters:
a.1 b.1
1 1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2422 2414 -1190

Optimised parameters:
      est.      lower      upper
cyan_0      100.9521      NA      NA
log_k_JCZ38      -3.4629      NA      NA
log_k_J9Z38      -5.0346      NA      NA
log_k_JSE76      -5.5722      NA      NA
f_cyan_ilr_1      0.6560      NA      NA
f_cyan_ilr_2      0.7983      NA      NA
f_JCZ38_qlogis    42.7949      NA      NA
log_k1         -3.1721      NA      NA
log_k2         -4.4039      NA      NA
log_tb          2.3994      NA      NA
a.1             3.0586      NA      NA
b.1             0.0380      NA      NA
SD.log_k_JCZ38    1.3754      NA      NA

```

SD.log_k_J9Z38	0.6703	NA	NA
SD.log_k_JSE76	0.5876	NA	NA
SD.f_cyan_ilr_1	0.3272	NA	NA
SD.f_cyan_ilr_2	0.5300	NA	NA
SD.f_JCZ38_qlogis	6.4465	NA	NA
SD.log_k1	0.4135	NA	NA
SD.log_k2	0.4182	NA	NA
SD.log_tb	0.6035	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.3754	NA	NA
SD.log_k_J9Z38	0.6703	NA	NA
SD.log_k_JSE76	0.5876	NA	NA
SD.f_cyan_ilr_1	0.3272	NA	NA
SD.f_cyan_ilr_2	0.5300	NA	NA
SD.f_JCZ38_qlogis	6.4465	NA	NA
SD.log_k1	0.4135	NA	NA
SD.log_k2	0.4182	NA	NA
SD.log_tb	0.6035	NA	NA

Variance model:

	est.	lower	upper
a.1	3.059	NA	NA
b.1	0.038	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.010e+02	NA	NA
k_JCZ38	3.134e-02	NA	NA
k_J9Z38	6.509e-03	NA	NA
k_JSE76	3.802e-03	NA	NA
f_cyan_to_JCZ38	6.127e-01	NA	NA
f_cyan_to_J9Z38	2.423e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
k1	4.191e-02	NA	NA
k2	1.223e-02	NA	NA
tb	1.102e+01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.6127
cyan_J9Z38	0.2423
cyan_sink	0.1449
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	29.94	161.54	48.63	16.54	56.68
JCZ38	22.12	73.47	NA	NA	NA
J9Z38	106.50	353.77	NA	NA	NA
JSE76	182.30	605.60	NA	NA	NA

Pathway 2

Listing 11: Hierarchical FOMC path 2 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:17:33 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - (alpha/beta) * 1/((time/beta) + 1) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_JCZ38 * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 851.145 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
101.8173    -1.8998    -5.1449    -2.5415    0.6705
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis  log_alpha  log_beta
  4.4669    16.1281    13.3327    -0.2314    2.8738

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      5.742      0.000      0.000      0.00      0.0000
log_k_JCZ38  0.000      1.402      0.000      0.00      0.0000
log_k_J9Z38  0.000      0.000      1.718      0.00      0.0000
log_k_JSE76  0.000      0.000      0.000      3.57      0.0000
f_cyan_ilr_1 0.000      0.000      0.000      0.00      0.5926
f_cyan_ilr_2 0.000      0.000      0.000      0.00      0.0000
f_JCZ38_qlogis 0.000      0.000      0.000      0.00      0.0000
f_JSE76_qlogis 0.000      0.000      0.000      0.00      0.0000
log_alpha     0.000      0.000      0.000      0.00      0.0000
log_beta      0.000      0.000      0.000      0.00      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_alpha log_beta
cyan_0      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JCZ38 0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_J9Z38 0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JSE76 0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_1 0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_2 10.56      0.00      0.00      0.00      0.0000      0.0000
f_JCZ38_qlogis 0.00      12.04      0.00      0.00      0.0000      0.0000
f_JSE76_qlogis 0.00      0.00      15.26      0.00      0.0000      0.0000
log_alpha     0.00      0.00      0.00      0.4708      0.0000
log_beta      0.00      0.00      0.00      0.0000      0.4432

Starting values for error model parameters:
a.1
1

Results:

Likelihood computed by importance sampling
      AIC  BIC  logLik
2308 2301 -1134

Optimised parameters:
      est.      lower      upper
cyan_0    101.9586  99.22024 104.69700
log_k_JCZ38 -2.4861 -3.17661 -1.79560
log_k_J9Z38 -5.3926 -6.08842 -4.69684
log_k_JSE76 -3.1193 -4.12904 -2.10962
f_cyan_ilr_1  0.7368  0.42085  1.05276
f_cyan_ilr_2  0.6196  0.06052  1.17861
f_JCZ38_qlogis 4.8970 -4.68003 14.47398
f_JSE76_qlogis 4.4066 -1.02087  9.83398
log_alpha   -0.3021 -0.68264  0.07838
log_beta     2.7438  2.57970  2.90786
a.1          2.9008  2.69920  3.10245

```

```

SD.cyan_0      2.7081  0.64216  4.77401
SD.log_k_JCZ38 0.7043  0.19951  1.20907
SD.log_k_J9Z38 0.6248  0.05790  1.19180
SD.log_k_JSE76 1.0750  0.33157  1.81839
SD.f_cyan_ilr_1 0.3429  0.11688  0.56892
SD.f_cyan_ilr_2 0.4774  0.09381  0.86097
SD.f_JCZ38_qlogis 1.5565 -7.83970 10.95279
SD.f_JSE76_qlogis 1.6871 -1.25577 4.63000
SD.log_alpha    0.4216  0.15913  0.68405

Correlation:
cyan_0  l__JCZ3  l__J9Z3  l__JSE7  f_cy__1  f_cy__2  f_JCZ38  f_JSE76
log_k_JCZ38 -0.0167
log_k_J9Z38 -0.0307  0.0057
log_k_JSE76 -0.0032  0.1358  0.0009
f_cyan_ilr_1 -0.0087  0.0206 -0.1158 -0.0009
f_cyan_ilr_2 -0.1598  0.0690  0.1770  0.0002 -0.0007
f_JCZ38_qlogis 0.0966 -0.1132 -0.0440  0.0182 -0.1385 -0.4583
f_JSE76_qlogis -0.0647  0.1157  0.0333 -0.0026  0.1110  0.3620 -0.8586
log_alpha    -0.0389  0.0113  0.0209  0.0021  0.0041  0.0451 -0.0605  0.0412
log_beta     -0.2508  0.0533  0.0977  0.0098  0.0220  0.2741 -0.2934  0.1999
log_lph
log_k_JCZ38
log_k_J9Z38
log_k_JSE76
f_cyan_ilr_1
f_cyan_ilr_2
f_JCZ38_qlogis
f_JSE76_qlogis
log_alpha
log_beta     0.2281

Random effects:
      est.      lower      upper
SD.cyan_0      2.7081  0.64216  4.7740
SD.log_k_JCZ38 0.7043  0.19951  1.2091
SD.log_k_J9Z38 0.6248  0.05790  1.1918
SD.log_k_JSE76 1.0750  0.33157  1.8184
SD.f_cyan_ilr_1 0.3429  0.11688  0.5689
SD.f_cyan_ilr_2 0.4774  0.09381  0.8610
SD.f_JCZ38_qlogis 1.5565 -7.83970 10.9528
SD.f_JSE76_qlogis 1.6871 -1.25577 4.6300
SD.log_alpha    0.4216  0.15913  0.6840

Variance model:
      est.      lower      upper
a.1  2.901  2.699  3.102

Backtransformed parameters:
      est.      lower      upper
cyan_0      101.95862  99.220240  1.047e+02
k_JCZ38      0.08323  0.041727  1.660e-01
k_J9Z38      0.00455  0.002269  9.124e-03
k_JSE76      0.04419  0.016098  1.213e-01
f_cyan_to_JCZ38 0.61318      NA      NA
f_cyan_to_J9Z38 0.21630      NA      NA
f_JCZ38_to_JSE76 0.99259  0.009193  1.000e+00
f_JSE76_to_JCZ38 0.98795  0.264857  9.999e-01
alpha        0.73924  0.505281  1.082e+00
beta         15.54568  13.193194  1.832e+01

Resulting formation fractions:
      ff
cyan_JCZ38 0.613182
cyan_J9Z38 0.216298
cyan_sink  0.170519
JCZ38_JSE76 0.992586
JCZ38_sink 0.007414
JSE76_JCZ38 0.987950
JSE76_sink 0.012050

Estimated disappearance times:
      DT50  DT90  DT50back
cyan      24.157 334.68  100.7
JCZ38      8.328 27.66   NA
J9Z38     152.341 506.06   NA
JSE76     15.687 52.11   NA

```

Listing 12: Hierarchical FOMC path 2 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:18:24 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - (alpha/beta) * 1/((time/beta) + 1) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_JCZ38 * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * (alpha/beta) * 1/((time/beta) + 1) *
              cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 901.733 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
101.9028      -1.9055      -5.0249      -2.5646      0.6807
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis      log_alpha      log_beta
      4.8883      16.0676      9.3923      -0.1346      3.0364

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
6.321      0.000      0.000      0.000      0.0000
log_k_JCZ38      0.000      1.392      0.000      0.000      0.0000
log_k_J9Z38      0.000      0.000      1.561      0.000      0.0000
log_k_JSE76      0.000      0.000      0.000      3.614      0.0000
f_cyan_ilr_1      0.000      0.000      0.000      0.000      0.6339
f_cyan_ilr_2      0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis      0.000      0.000      0.000      0.000      0.0000
f_JSE76_qlogis      0.000      0.000      0.000      0.000      0.0000
log_alpha      0.000      0.000      0.000      0.000      0.0000
log_beta      0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_alpha log_beta
cyan_0      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JCZ38      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_J9Z38      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JSE76      0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_1      0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_2      10.41      0.00      0.00      0.00      0.0000      0.0000
f_JCZ38_qlogis      0.00      12.24      0.00      0.00      0.0000      0.0000
f_JSE76_qlogis      0.00      0.00      15.13      0.0000      0.0000
log_alpha      0.00      0.00      0.00      0.3701      0.0000
log_beta      0.00      0.00      0.00      0.0000      0.5662

Starting values for error model parameters:
a.1 b.1
1 1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2248 2240 -1103

Optimised parameters:
      est.      lower      upper
cyan_0      101.55545      9.920e+01      1.039e+02
log_k_JCZ38      -2.37354      -2.928e+00      -1.819e+00
log_k_J9Z38      -5.14736      -5.960e+00      -4.335e+00
log_k_JSE76      -3.07802      -4.243e+00      -1.913e+00
f_cyan_ilr_1      0.71263      3.655e-01      1.060e+00
f_cyan_ilr_2      0.95202      2.701e-01      1.634e+00
f_JCZ38_qlogis      3.58473      1.251e+00      5.919e+00
f_JSE76_qlogis      19.03623      -1.037e+07      1.037e+07
log_alpha      -0.15297      -4.490e-01      1.431e-01
log_beta      2.99230      2.706e+00      3.278e+00
a.1      2.04816      NA      NA
b.1      0.06886      NA      NA
SD.log_k_JCZ38      0.56174      NA      NA

```

SD.log_k_J9Z38	0.86509	NA	NA
SD.log_k_JSE76	1.28450	NA	NA
SD.f_cyan_ilr_1	0.38705	NA	NA
SD.f_cyan_ilr_2	0.54153	NA	NA
SD.f_JCZ38_qlogis	1.65311	NA	NA
SD.f_JSE76_qlogis	7.51468	NA	NA
SD.log_alpha	0.31586	NA	NA
SD.log_beta	0.24696	NA	NA

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	0.5617	NA	NA
SD.log_k_J9Z38	0.8651	NA	NA
SD.log_k_JSE76	1.2845	NA	NA
SD.f_cyan_ilr_1	0.3870	NA	NA
SD.f_cyan_ilr_2	0.5415	NA	NA
SD.f_JCZ38_qlogis	1.6531	NA	NA
SD.f_JSE76_qlogis	7.5147	NA	NA
SD.log_alpha	0.3159	NA	NA
SD.log_beta	0.2470	NA	NA

Variance model:

	est.	lower	upper
a.1	2.04816	NA	NA
b.1	0.06886	NA	NA

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.016e+02	99.20301	103.9079
k_JCZ38	9.315e-02	0.05349	0.1622
k_J9Z38	5.815e-03	0.00258	0.0131
k_JSE76	4.605e-02	0.01436	0.1477
f_cyan_to_JCZ38	6.438e-01	NA	NA
f_cyan_to_J9Z38	2.350e-01	NA	NA
f_JCZ38_to_JSE76	9.730e-01	0.77745	0.9973
f_JSE76_to_JCZ38	1.000e+00	0.00000	1.0000
alpha	8.582e-01	0.63824	1.1538
beta	1.993e+01	14.97621	26.5262

Resulting formation fractions:

	ff
cyan_JCZ38	6.438e-01
cyan_J9Z38	2.350e-01
cyan_sink	1.212e-01
JCZ38_JSE76	9.730e-01
JCZ38_sink	2.700e-02
JSE76_JCZ38	1.000e+00
JSE76_sink	5.403e-09

Estimated disappearance times:

	DT50	DT90	DT50back
cyan	24.771	271.70	81.79
JCZ38	7.441	24.72	NA
J9Z38	119.205	395.99	NA
JSE76	15.052	50.00	NA

Listing 13: Hierarchical DFOP path 2 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:20:00 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38 +
f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 998.099 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
102.4358      -2.3107      -5.3123      -3.7120      0.6753
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis  log_k1      log_k2
1.1462      12.4095      12.3630      -1.9317      -4.4557
g_qlogis
-0.5648

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      4.594      0.0000      0.000      0.0      0.0000
log_k_JCZ38  0.000      0.7966      0.000      0.0      0.0000
log_k_J9Z38  0.000      0.0000      1.561      0.0      0.0000
log_k_JSE76  0.000      0.0000      0.000      0.8      0.0000
f_cyan_ilr_1 0.000      0.0000      0.000      0.0      0.6349
f_cyan_ilr_2 0.000      0.0000      0.000      0.0      0.0000
f_JCZ38_qlogis 0.000      0.0000      0.000      0.0      0.0000
f_JSE76_qlogis 0.000      0.0000      0.000      0.0      0.0000
log_k1      0.000      0.0000      0.000      0.0      0.0000
log_k2      0.000      0.0000      0.000      0.0      0.0000
g_qlogis     0.000      0.0000      0.000      0.0      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_k1 log_k2
cyan_0      0.000      0.00      0.0      0.0 0.000 0.0000
log_k_JCZ38  0.000      0.00      0.0      0.0 0.000 0.0000
log_k_J9Z38  0.000      0.00      0.0      0.0 0.000 0.0000
log_k_JSE76  0.000      0.00      0.0      0.0 0.000 0.0000
f_cyan_ilr_1 0.000      0.00      0.0      0.0 0.000 0.0000
f_cyan_ilr_2 0.000      1.797      0.0      0.0 0.000 0.0000
f_JCZ38_qlogis 0.000      13.85      0.0      0.0 0.000 0.0000
f_JSE76_qlogis 0.000      0.00      14.1      0.0 0.000 0.0000
log_k1      0.000      0.00      0.0      1.106 0.0000
log_k2      0.000      0.00      0.0      0.000 0.6141
g_qlogis     0.000      0.00      0.0      0.000 0.0000
      g_qlogis
cyan_0      0.000
log_k_JCZ38 0.000
log_k_J9Z38 0.000
log_k_JSE76 0.000
f_cyan_ilr_1 0.000
f_cyan_ilr_2 0.000
f_JCZ38_qlogis 0.000
f_JSE76_qlogis 0.000
log_k1      0.000
log_k2      0.000
g_qlogis     1.595

Starting values for error model parameters:
a.1
1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2290 2281 -1123

Optimised parameters:

	est.	lower	upper
cyan_0	102.6903	101.44420	103.9365
log_k_JCZ38	-2.4018	-2.98058	-1.8230
log_k_J9Z38	-5.1865	-5.92931	-4.4437
log_k_JSE76	-3.0784	-4.25226	-1.9045
f_cyan_ilr_1	0.7157	0.37625	1.0551
f_cyan_ilr_2	0.7073	0.20136	1.2132
f_JCZ38_qlogis	4.6797	0.43240	8.9269
f_JSE76_qlogis	5.0080	-1.01380	11.0299
log_k1	-1.9620	-2.62909	-1.2949
log_k2	-4.4894	-4.94958	-4.0292
g_qlogis	-0.4658	-1.34443	0.4129
a.1	2.7158	2.52576	2.9059
SD.log_k_JCZ38	0.5818	0.15679	1.0067
SD.log_k_J9Z38	0.7421	0.16751	1.3167
SD.log_k_JSE76	1.2841	0.43247	2.1356
SD.f_cyan_ilr_1	0.3748	0.13040	0.6192
SD.f_cyan_ilr_2	0.4550	0.08396	0.8261
SD.f_JCZ38_qlogis	2.0862	-0.73390	4.9062
SD.f_JSE76_qlogis	1.9585	-3.14773	7.0647
SD.log_k1	0.7389	0.25761	1.2201
SD.log_k2	0.5132	0.18143	0.8450
SD.g_qlogis	0.9870	0.35773	1.6164

Correlation:

	cyan_0	l__JCZ3	l__J9Z3	l__JSE7	f_cy__1	f_cy__2	f_JCZ38	f_JSE76
log_k_JCZ38	-0.0170							
log_k_J9Z38	-0.0457	0.0016						
log_k_JSE76	-0.0046	0.1183	0.0005					
f_cyan_ilr_1	0.0079	0.0072	-0.0909	0.0003				
f_cyan_ilr_2	-0.3114	0.0343	0.1542	0.0023	-0.0519			
f_JCZ38_qlogis	0.0777	-0.0601	-0.0152	0.0080	-0.0520	-0.2524		
f_JSE76_qlogis	-0.0356	0.0817	0.0073	0.0051	0.0388	0.1959	-0.6236	
log_k1	0.0848	-0.0028	0.0010	-0.0010	-0.0014	-0.0245	0.0121	-0.0177
log_k2	0.0274	-0.0001	0.0075	0.0000	-0.0023	-0.0060	0.0000	-0.0130
g_qlogis	0.0159	0.0002	-0.0095	0.0002	0.0029	-0.0140	-0.0001	0.0149
log_k1		log_k1	log_k2					
log_k_JCZ38								
log_k_J9Z38								
log_k_JSE76								
f_cyan_ilr_1								
f_cyan_ilr_2								
f_JCZ38_qlogis								
f_JSE76_qlogis								
log_k1								
log_k2		0.0280						
g_qlogis		-0.0278	-0.0310					

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	0.5818	0.15679	1.0067
SD.log_k_J9Z38	0.7421	0.16751	1.3167
SD.log_k_JSE76	1.2841	0.43247	2.1356
SD.f_cyan_ilr_1	0.3748	0.13040	0.6192
SD.f_cyan_ilr_2	0.4550	0.08396	0.8261
SD.f_JCZ38_qlogis	2.0862	-0.73390	4.9062
SD.f_JSE76_qlogis	1.9585	-3.14773	7.0647
SD.log_k1	0.7389	0.25761	1.2201
SD.log_k2	0.5132	0.18143	0.8450
SD.g_qlogis	0.9870	0.35773	1.6164

Variance model:

	est.	lower	upper
a.1	2.716	2.526	2.906

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.027e+02	1.014e+02	103.93649
k_JCZ38	9.056e-02	5.076e-02	0.16154
k_J9Z38	5.591e-03	2.660e-03	0.01175
k_JSE76	4.603e-02	1.423e-02	0.14890
f_cyan_to_JCZ38	6.184e-01	NA	NA
f_cyan_to_J9Z38	2.248e-01	NA	NA
f_JCZ38_to_JSE76	9.908e-01	6.064e-01	0.99987
f_JSE76_to_JCZ38	9.934e-01	2.662e-01	0.99998
k1	1.406e-01	7.214e-02	0.27393
k2	1.123e-02	7.086e-03	0.01779

```
g          3.856e-01 2.068e-01  0.60177
```

```
Resulting formation fractions:
```

```
      ff
cyan_JCZ38 0.618443
cyan_J9Z38 0.224770
cyan_sink  0.156787
JCZ38_JSE76 0.990803
JCZ38_sink 0.009197
JSE76_JCZ38 0.993360
JSE76_sink 0.006640
```

```
Estimated disappearance times:
```

```
      DT50  DT90 DT50back DT50_k1 DT50_k2
cyan    21.674 161.70   48.68   4.931   61.74
JCZ38    7.654  25.43      NA      NA      NA
J9Z38   123.966 411.81      NA      NA      NA
JSE76    15.057  50.02      NA      NA      NA
```

Listing 14: Hierarchical DFOP path 2 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:25:26 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38 +
f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1324.061 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
      101.7523      -1.5948      -5.0119      -2.2723      0.6719
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis  log_k1      log_k2
      5.1681      12.8238      12.4130      -2.0057      -4.5526
g_qlogis
      -0.5805

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      5.627      0.000      0.000      0.000      0.0000
log_k_JCZ38  0.000      2.327      0.000      0.000      0.0000
log_k_J9Z38  0.000      0.000      1.664      0.000      0.0000
log_k_JSE76  0.000      0.000      0.000      4.566      0.0000
f_cyan_ilr_1 0.000      0.000      0.000      0.000      0.6519
f_cyan_ilr_2 0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis 0.000      0.000      0.000      0.000      0.0000
f_JSE76_qlogis 0.000      0.000      0.000      0.000      0.0000
log_k1      0.000      0.000      0.000      0.000      0.0000
log_k2      0.000      0.000      0.000      0.000      0.0000
g_qlogis     0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_k1 log_k2
cyan_0      0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_JCZ38  0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_J9Z38  0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_JSE76  0.0      0.00      0.00      0.00 0.0000 0.0000
f_cyan_ilr_1 0.0      0.00      0.00      0.00 0.0000 0.0000
f_cyan_ilr_2 10.1      0.00      0.00      0.00 0.0000 0.0000
f_JCZ38_qlogis 0.0      13.99      0.00 0.0000 0.0000
f_JSE76_qlogis 0.0      0.00      14.15 0.0000 0.0000
log_k1      0.0      0.00      0.00 0.00 0.8452 0.0000
log_k2      0.0      0.00      0.00 0.00 0.0000 0.5968
g_qlogis     0.0      0.00      0.00 0.00 0.0000 0.0000
      g_qlogis
cyan_0      0.000
log_k_JCZ38 0.000
log_k_J9Z38 0.000
log_k_JSE76 0.000
f_cyan_ilr_1 0.000
f_cyan_ilr_2 0.000
f_JCZ38_qlogis 0.000
f_JSE76_qlogis 0.000
log_k1      0.000
log_k2      0.000
g_qlogis     1.691

Starting values for error model parameters:
a.1 b.1
1 1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2234 2226 -1095

Optimised parameters:

	est.	lower	upper
cyan_0	101.10667	9.903e+01	103.18265
log_k_JCZ38	-2.49437	-3.297e+00	-1.69221
log_k_J9Z38	-5.08171	-5.875e+00	-4.28846
log_k_JSE76	-3.20072	-4.180e+00	-2.22163
f_cyan_ilr_1	0.71059	3.639e-01	1.05727
f_cyan_ilr_2	1.15398	2.981e-01	2.00984
f_JCZ38_qlogis	3.18027	1.056e+00	5.30452
f_JSE76_qlogis	5.61578	-2.505e+01	36.28077
log_k1	-2.38875	-2.517e+00	-2.26045
log_k2	-4.67246	-4.928e+00	-4.41715
g_qlogis	-0.28231	-1.135e+00	0.57058
a.1	2.08190	1.856e+00	2.30785
b.1	0.06114	5.015e-02	0.07214
SD.log_k_JCZ38	0.84622	2.637e-01	1.42873
SD.log_k_J9Z38	0.84564	2.566e-01	1.43464
SD.log_k_JSE76	1.04385	3.242e-01	1.76351
SD.f_cyan_ilr_1	0.38568	1.362e-01	0.63514
SD.f_cyan_ilr_2	0.68046	7.166e-02	1.28925
SD.f_JCZ38_qlogis	1.25244	-4.213e-02	2.54700
SD.f_JSE76_qlogis	0.28202	-1.515e+03	1515.87968
SD.log_k2	0.25749	7.655e-02	0.43843
SD.g_qlogis	0.94535	3.490e-01	1.54174

Correlation:

	cyan_0	l__JCZ3	l__J9Z3	l__JSE7	f_cy__1	f_cy__2	f_JCZ38	f_JSE76
log_k_JCZ38	-0.0086							
log_k_J9Z38	-0.0363	-0.0007						
log_k_JSE76	0.0015	0.1210	-0.0017					
f_cyan_ilr_1	-0.0048	0.0095	-0.0572	0.0030				
f_cyan_ilr_2	-0.4788	0.0328	0.1143	0.0027	-0.0316			
f_JCZ38_qlogis	0.0736	-0.0664	-0.0137	0.0145	-0.0444	-0.2175		
f_JSE76_qlogis	-0.0137	0.0971	0.0035	0.0009	0.0293	0.1333	-0.6767	
log_k1	0.2345	-0.0350	-0.0099	-0.0113	-0.0126	-0.1652	0.1756	-0.2161
log_k2	0.0440	-0.0133	0.0199	-0.0040	-0.0097	-0.0119	0.0604	-0.1306
g_qlogis	0.0438	0.0078	-0.0123	0.0029	0.0046	-0.0363	-0.0318	0.0736
log_k1								
log_k_JCZ38								
log_k_J9Z38								
log_k_JSE76								
f_cyan_ilr_1								
f_cyan_ilr_2								
f_JCZ38_qlogis								
f_JSE76_qlogis								
log_k1								
log_k2	0.3198							
g_qlogis	-0.1666	-0.0954						

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	0.8462	2.637e-01	1.4287
SD.log_k_J9Z38	0.8456	2.566e-01	1.4346
SD.log_k_JSE76	1.0439	3.242e-01	1.7635
SD.f_cyan_ilr_1	0.3857	1.362e-01	0.6351
SD.f_cyan_ilr_2	0.6805	7.166e-02	1.2893
SD.f_JCZ38_qlogis	1.2524	-4.213e-02	2.5470
SD.f_JSE76_qlogis	0.2820	-1.515e+03	1515.8797
SD.log_k2	0.2575	7.655e-02	0.4384
SD.g_qlogis	0.9453	3.490e-01	1.5417

Variance model:

	est.	lower	upper
a.1	2.08190	1.85595	2.30785
b.1	0.06114	0.05015	0.07214

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.011e+02	9.903e+01	103.18265
k_JCZ38	8.255e-02	3.701e-02	0.18411
k_J9Z38	6.209e-03	2.809e-03	0.01373
k_JSE76	4.073e-02	1.530e-02	0.10843
f_cyan_to_JCZ38	6.608e-01	NA	NA
f_cyan_to_J9Z38	2.419e-01	NA	NA
f_JCZ38_to_JSE76	9.601e-01	7.419e-01	0.99506
f_JSE76_to_JCZ38	9.964e-01	1.322e-11	1.00000
k1	9.174e-02	8.070e-02	0.10430
k2	9.349e-03	7.243e-03	0.01207

g 4.299e-01 2.432e-01 0.63890

Resulting formation fractions:

ff
cyan_JCZ38 0.660808
cyan_J9Z38 0.241904
cyan_sink 0.097288
JCZ38_JSE76 0.960085
JCZ38_sink 0.039915
JSE76_JCZ38 0.996373
JSE76_sink 0.003627

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	24.359	186.18	56.05	7.555	74.14
JCZ38	8.397	27.89	NA	NA	NA
J9Z38	111.631	370.83	NA	NA	NA
JSE76	17.017	56.53	NA	NA	NA

Listing 15: Hierarchical SFORB path 2 fit with constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:19:53 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
                 cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
                 cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
              * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
              * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 990.789 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      102.4394         -2.7673         -2.8942
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
      -3.6201         -2.3107         -5.3123
      log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
      -3.7120         0.6754         1.1448
      f_JCZ38_qlogis      f_JSE76_qlogis
      13.2672         13.3538

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
cyan_free_0      4.589      0.0000      0.00      0.00
log_k_cyan_free      0.000      0.4849      0.00      0.00
log_k_cyan_free_bound      0.000      0.0000      0.0000      1.62
log_k_cyan_bound_free      0.000      0.0000      0.0000      0.00
log_k_JCZ38      0.000      0.0000      0.0000      0.00
log_k_J9Z38      0.000      0.0000      0.0000      0.00
log_k_JSE76      0.000      0.0000      0.0000      0.00
f_cyan_ilr_1      0.000      0.0000      0.0000      0.00
f_cyan_ilr_2      0.000      0.0000      0.0000      0.00
f_JCZ38_qlogis      0.000      0.0000      0.0000      0.00
f_JSE76_qlogis      0.000      0.0000      0.0000      0.00
      log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000      0.0000      0.000      0.0
log_k_cyan_free      0.000      0.0000      0.000      0.0
log_k_cyan_free_bound      0.000      0.0000      0.000      0.0
log_k_cyan_bound_free      1.197      0.0000      0.000      0.0
log_k_JCZ38      0.000      0.7966      0.000      0.0
log_k_J9Z38      0.000      0.0000      1.561      0.0
log_k_JSE76      0.000      0.0000      0.000      0.8
f_cyan_ilr_1      0.000      0.0000      0.000      0.0
f_cyan_ilr_2      0.000      0.0000      0.000      0.0
f_JCZ38_qlogis      0.000      0.0000      0.000      0.0
f_JSE76_qlogis      0.000      0.0000      0.000      0.0
      f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis
cyan_free_0      0.0000      0.000      0.00      0.00
log_k_cyan_free      0.0000      0.000      0.00      0.00
log_k_cyan_free_bound      0.0000      0.000      0.00      0.00
log_k_cyan_bound_free      0.0000      0.000      0.00      0.00
log_k_JCZ38      0.0000      0.000      0.00      0.00
log_k_J9Z38      0.0000      0.000      0.00      0.00
log_k_JSE76      0.0000      0.000      0.00      0.00
f_cyan_ilr_1      0.6349      0.000      0.00      0.00
f_cyan_ilr_2      0.0000      1.797      0.00      0.00
f_JCZ38_qlogis      0.0000      0.000      13.84      0.00
f_JSE76_qlogis      0.0000      0.000      0.00      14.66

Starting values for error model parameters:
a.1
1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2284 2275 -1120

Optimised parameters:

	est.	lower	upper
cyan_free_0	102.7730	1.015e+02	1.041e+02
log_k_cyan_free	-2.8530	-3.167e+00	-2.539e+00
log_k_cyan_free_bound	-2.7326	-3.543e+00	-1.922e+00
log_k_cyan_bound_free	-3.5582	-4.126e+00	-2.990e+00
log_k_JCZ38	-2.3810	-2.921e+00	-1.841e+00
log_k_J9Z38	-5.2301	-5.963e+00	-4.497e+00
log_k_JSE76	-3.0286	-4.286e+00	-1.771e+00
f_cyan_ilr_1	0.7081	3.733e-01	1.043e+00
f_cyan_ilr_2	0.5847	7.846e-03	1.162e+00
f_JCZ38_qlogis	9.5676	-1.323e+03	1.342e+03
f_JSE76_qlogis	3.7042	7.254e-02	7.336e+00
a.1	2.7222	2.532e+00	2.913e+00
SD.log_k_cyan_free	0.3338	1.086e-01	5.589e-01
SD.log_k_cyan_free_bound	0.8888	3.023e-01	1.475e+00
SD.log_k_cyan_bound_free	0.6220	2.063e-01	1.038e+00
SD.log_k_JCZ38	0.5221	1.334e-01	9.108e-01
SD.log_k_J9Z38	0.7104	1.371e-01	1.284e+00
SD.log_k_JSE76	1.3837	4.753e-01	2.292e+00
SD.f_cyan_ilr_1	0.3620	1.248e-01	5.992e-01
SD.f_cyan_ilr_2	0.4259	8.145e-02	7.704e-01
SD.f_JCZ38_qlogis	3.5332	-1.037e+05	1.037e+05
SD.f_JSE76_qlogis	1.6990	-2.771e-01	3.675e+00

Correlation:

	cyn_f_0	lg_k_c_	lg_k_cyn_f_	lg_k_cyn_b_	l__JCZ3	l__J9Z3
log_k_cyan_free	0.2126					
log_k_cyan_free_bound	0.0894	0.0871				
log_k_cyan_bound_free	0.0033	0.0410	0.0583			
log_k_JCZ38	-0.0708	-0.0280	-0.0147	0.0019		
log_k_J9Z38	-0.0535	-0.0138	0.0012	0.0148	0.0085	
log_k_JSE76	-0.0066	-0.0030	-0.0021	-0.0005	0.1090	0.0010
f_cyan_ilr_1	-0.0364	-0.0157	-0.0095	-0.0015	0.0458	-0.0960
f_cyan_ilr_2	-0.3814	-0.1104	-0.0423	0.0146	0.1540	0.1526
f_JCZ38_qlogis	0.2507	0.0969	0.0482	-0.0097	-0.2282	-0.0363
f_JSE76_qlogis	-0.1648	-0.0710	-0.0443	-0.0087	0.2002	0.0226
	l__JSE7	f_cy__1	f_cy__2	f_JCZ38		
log_k_cyan_free						
log_k_cyan_free_bound						
log_k_cyan_bound_free						
log_k_JCZ38						
log_k_J9Z38						
log_k_JSE76						
f_cyan_ilr_1	0.0001					
f_cyan_ilr_2	0.0031	0.0586				
f_JCZ38_qlogis	0.0023	-0.1867	-0.6255			
f_JSE76_qlogis	0.0082	0.1356	0.4519	-0.7951		

Random effects:

	est.	lower	upper
SD.log_k_cyan_free	0.3338	1.086e-01	5.589e-01
SD.log_k_cyan_free_bound	0.8888	3.023e-01	1.475e+00
SD.log_k_cyan_bound_free	0.6220	2.063e-01	1.038e+00
SD.log_k_JCZ38	0.5221	1.334e-01	9.108e-01
SD.log_k_J9Z38	0.7104	1.371e-01	1.284e+00
SD.log_k_JSE76	1.3837	4.753e-01	2.292e+00
SD.f_cyan_ilr_1	0.3620	1.248e-01	5.992e-01
SD.f_cyan_ilr_2	0.4259	8.145e-02	7.704e-01
SD.f_JCZ38_qlogis	3.5332	-1.037e+05	1.037e+05
SD.f_JSE76_qlogis	1.6990	-2.771e-01	3.675e+00

Variance model:

est. lower upper
a.1 2.722 2.532 2.913

Backtransformed parameters:

	est.	lower	upper
cyan_free_0	1.028e+02	1.015e+02	104.06475
k_cyan_free	5.767e-02	4.213e-02	0.07894
k_cyan_free_bound	6.505e-02	2.892e-02	0.14633
k_cyan_bound_free	2.849e-02	1.614e-02	0.05028
k_JCZ38	9.246e-02	5.390e-02	0.15859
k_J9Z38	5.353e-03	2.572e-03	0.01114
k_JSE76	4.838e-02	1.376e-02	0.17009
f_cyan_free_to_JCZ38	6.011e-01	5.028e-01	0.83792
f_cyan_free_to_J9Z38	2.208e-01	5.028e-01	0.83792
f_JCZ38_to_JSE76	9.999e-01	0.000e+00	1.00000


```
f_JSE76_to_JCZ38      9.760e-01 5.181e-01  0.99935
```

Estimated Eigenvalues of SFORB model(s):

```
cyan_b1 cyan_b2  cyan_g  
0.13942 0.01178 0.35948
```

Resulting formation fractions:

```
ff  
cyan_free_JCZ38 6.011e-01  
cyan_free_J9Z38 2.208e-01  
cyan_free_sink  1.780e-01  
cyan_free       1.000e+00  
JCZ38_JSE76     9.999e-01  
JCZ38_sink      6.996e-05  
JSE76_JCZ38     9.760e-01  
JSE76_sink      2.403e-02
```

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_cyan_b1	DT50_cyan_b2
cyan	23.390	157.60	47.44	4.971	58.82
JCZ38	7.497	24.90	NA	NA	NA
J9Z38	129.482	430.13	NA	NA	NA
JSE76	14.326	47.59	NA	NA	NA

Listing 16: Hierarchical SFORB path 2 fit with two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:25:49 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
               cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
               cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
               * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
               * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1347.327 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      101.751         -2.837         -3.016
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
      -3.660         -2.299         -5.313
      log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
      -3.699         0.672         5.873
      f_JCZ38_qlogis      f_JSE76_qlogis
      13.216         13.338

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      5.629         0.000         0.000
log_k_cyan_free      0.000         0.446         0.000
log_k_cyan_free_bound      0.000         0.000         1.449
log_k_cyan_bound_free      0.000         0.000         0.000
log_k_JCZ38      0.000         0.000         0.000
log_k_J9Z38      0.000         0.000         0.000
log_k_JSE76      0.000         0.000         0.000
f_cyan_ilr_1      0.000         0.000         0.000
f_cyan_ilr_2      0.000         0.000         0.000
f_JCZ38_qlogis      0.000         0.000         0.000
f_JSE76_qlogis      0.000         0.000         0.000
      log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000         0.0000         0.000         0.0000
log_k_cyan_free      0.000         0.0000         0.000         0.0000
log_k_cyan_free_bound      0.000         0.0000         0.000         0.0000
log_k_cyan_bound_free      1.213         0.0000         0.000         0.0000
log_k_JCZ38      0.000         0.7801         0.000         0.0000
log_k_J9Z38      0.000         0.0000         1.575         0.0000
log_k_JSE76      0.000         0.0000         0.000         0.8078
f_cyan_ilr_1      0.000         0.0000         0.000         0.0000
f_cyan_ilr_2      0.000         0.0000         0.000         0.0000
f_JCZ38_qlogis      0.000         0.0000         0.000         0.0000
f_JSE76_qlogis      0.000         0.0000         0.000         0.0000
      f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis
cyan_free_0      0.0000         0.00         0.00         0.00
log_k_cyan_free      0.0000         0.00         0.00         0.00
log_k_cyan_free_bound      0.0000         0.00         0.00         0.00
log_k_cyan_bound_free      0.0000         0.00         0.00         0.00
log_k_JCZ38      0.0000         0.00         0.00         0.00
log_k_J9Z38      0.0000         0.00         0.00         0.00
log_k_JSE76      0.0000         0.00         0.00         0.00
f_cyan_ilr_1      0.6519         0.00         0.00         0.00
f_cyan_ilr_2      0.0000         10.78         0.00         0.00
f_JCZ38_qlogis      0.0000         0.00         13.96         0.00
f_JSE76_qlogis      0.0000         0.00         0.00         14.69

Starting values for error model parameters:
a.1 b.1
1 1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2240 2232 -1098

Optimised parameters:

	est.	lower	upper
cyan_free_0	101.10205	98.99221	103.2119
log_k_cyan_free	-3.16929	-3.61395	-2.7246
log_k_cyan_free_bound	-3.38259	-3.63022	-3.1350
log_k_cyan_bound_free	-3.81075	-4.13888	-3.4826
log_k_JCZ38	-2.42057	-3.00756	-1.8336
log_k_J9Z38	-5.07501	-5.85138	-4.2986
log_k_JSE76	-3.12442	-4.21277	-2.0361
f_cyan_ilr_1	0.70577	0.35788	1.0537
f_cyan_ilr_2	1.14824	0.15810	2.1384
f_JCZ38_qlogis	3.52245	0.43257	6.6123
f_JSE76_qlogis	5.65140	-21.22295	32.5257
a.1	2.07062	1.84329	2.2980
b.1	0.06227	0.05124	0.0733
SD.log_k_cyan_free	0.49468	0.18566	0.8037
SD.log_k_cyan_bound_free	0.28972	0.07188	0.5076
SD.log_k_JCZ38	0.58852	0.16800	1.0090
SD.log_k_J9Z38	0.82500	0.24730	1.4027
SD.log_k_JSE76	1.19201	0.40313	1.9809
SD.f_cyan_ilr_1	0.38534	0.13640	0.6343
SD.f_cyan_ilr_2	0.72463	0.10076	1.3485
SD.f_JCZ38_qlogis	1.38223	-0.20997	2.9744
SD.f_JSE76_qlogis	2.07989	-72.53027	76.6901

Correlation:

	cyn_f_0	lg_k_c_	lg_k_cyn_f_	lg_k_cyn_b_	l__JCZ3	l__J9Z3
log_k_cyan_free	0.1117					
log_k_cyan_free_bound	0.1763	0.1828				
log_k_cyan_bound_free	0.0120	0.0593	0.5030			
log_k_JCZ38	-0.0459	-0.0230	-0.0931	-0.0337		
log_k_J9Z38	-0.0381	-0.0123	-0.0139	0.0237	0.0063	
log_k_JSE76	-0.0044	-0.0038	-0.0175	-0.0072	0.1120	0.0003
f_cyan_ilr_1	-0.0199	-0.0087	-0.0407	-0.0233	0.0268	-0.0552
f_cyan_ilr_2	-0.4806	-0.1015	-0.2291	-0.0269	0.1156	0.1113
f_JCZ38_qlogis	0.1805	0.0825	0.3085	0.0963	-0.1674	-0.0314
f_JSE76_qlogis	-0.1586	-0.0810	-0.3560	-0.1563	0.2025	0.0278
	l__JSE7	f_cy__1	f_cy__2	f_JCZ38		
log_k_cyan_free						
log_k_cyan_free_bound						
log_k_cyan_bound_free						
log_k_JCZ38						
log_k_J9Z38						
log_k_JSE76						
f_cyan_ilr_1	0.0024					
f_cyan_ilr_2	0.0087	0.0172				
f_JCZ38_qlogis	-0.0016	-0.1047	-0.4656			
f_JSE76_qlogis	0.0119	0.1034	0.4584	-0.8137		

Random effects:

	est.	lower	upper
SD.log_k_cyan_free	0.4947	0.18566	0.8037
SD.log_k_cyan_bound_free	0.2897	0.07188	0.5076
SD.log_k_JCZ38	0.5885	0.16800	1.0090
SD.log_k_J9Z38	0.8250	0.24730	1.4027
SD.log_k_JSE76	1.1920	0.40313	1.9809
SD.f_cyan_ilr_1	0.3853	0.13640	0.6343
SD.f_cyan_ilr_2	0.7246	0.10076	1.3485
SD.f_JCZ38_qlogis	1.3822	-0.20997	2.9744
SD.f_JSE76_qlogis	2.0799	-72.53027	76.6901

Variance model:

	est.	lower	upper
a.1	2.07062	1.84329	2.2980
b.1	0.06227	0.05124	0.0733

Backtransformed parameters:

	est.	lower	upper
cyan_free_0	1.011e+02	9.899e+01	103.21190
k_cyan_free	4.203e-02	2.695e-02	0.06557
k_cyan_free_bound	3.396e-02	2.651e-02	0.04350
k_cyan_bound_free	2.213e-02	1.594e-02	0.03073
k_JCZ38	8.887e-02	4.941e-02	0.15984
k_J9Z38	6.251e-03	2.876e-03	0.01359
k_JSE76	4.396e-02	1.481e-02	0.13054
f_cyan_free_to_JCZ38	6.590e-01	5.557e-01	0.95365
f_cyan_free_to_J9Z38	2.429e-01	5.557e-01	0.95365
f_JCZ38_to_JSE76	9.713e-01	6.065e-01	0.99866

```
f_JSE76_to_JCZ38      9.965e-01 6.067e-10  1.00000
```

Estimated Eigenvalues of SFORB model(s):

```
cyan_b1 cyan_b2  cyan_g
0.08749 0.01063 0.40855
```

Resulting formation fractions:

```
ff
cyan_free_JCZ38 0.65905
cyan_free_J9Z38 0.24291
cyan_free_sink  0.09805
cyan_free       1.00000
JCZ38_JSE76     0.97132
JCZ38_sink      0.02868
JSE76_JCZ38     0.99650
JSE76_sink      0.00350
```

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_cyan_b1	DT50_cyan_b2
cyan	24.91	167.16	50.32	7.922	65.19
JCZ38	7.80	25.91	NA	NA	NA
J9Z38	110.89	368.36	NA	NA	NA
JSE76	15.77	52.38	NA	NA	NA

Pathway 2, refined fits

Listing 17: Hierarchical FOMC path 2 fit with reduced random effects, two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:51:36 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - (alpha/beta) * 1/((time/beta) + 1) * cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * (alpha/beta) * 1/((time/beta) + 1) *
cyan - k_JCZ38 * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * (alpha/beta) * 1/((time/beta) + 1) *
cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1545.442 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
101.9028      -1.9055      -5.0249      -2.5646      0.6807
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis      log_alpha      log_beta
  4.8883      16.0676      9.3923      -0.1346      3.0364

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0      log_k_JCZ38      log_k_J9Z38      log_k_JSE76      f_cyan_ilr_1
cyan_0      6.321      0.000      0.000      0.000      0.0000
log_k_JCZ38      0.000      1.392      0.000      0.000      0.0000
log_k_J9Z38      0.000      0.000      1.561      0.000      0.0000
log_k_JSE76      0.000      0.000      0.000      3.614      0.0000
f_cyan_ilr_1      0.000      0.000      0.000      0.000      0.6339
f_cyan_ilr_2      0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis      0.000      0.000      0.000      0.000      0.0000
f_JSE76_qlogis      0.000      0.000      0.000      0.000      0.0000
log_alpha      0.000      0.000      0.000      0.000      0.0000
log_beta      0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_alpha log_beta
cyan_0      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JCZ38      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_J9Z38      0.00      0.00      0.00      0.00      0.0000      0.0000
log_k_JSE76      0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_1      0.00      0.00      0.00      0.00      0.0000      0.0000
f_cyan_ilr_2      10.41      0.00      0.00      0.00      0.0000      0.0000
f_JCZ38_qlogis      0.00      12.24      0.00      0.00      0.0000      0.0000
f_JSE76_qlogis      0.00      0.00      15.13      0.0000      0.0000
log_alpha      0.00      0.00      0.00      0.3701      0.0000
log_beta      0.00      0.00      0.00      0.0000      0.5662

Starting values for error model parameters:
a.1 b.1
1 1

Results:

Likelihood computed by importance sampling
      AIC      BIC      logLik
2251 2244 -1106

Optimised parameters:
      est.      lower      upper
cyan_0      101.05768      NA      NA
log_k_JCZ38      -2.73252      NA      NA
log_k_J9Z38      -5.07399      NA      NA
log_k_JSE76      -3.52863      NA      NA
f_cyan_ilr_1      0.72176      NA      NA
f_cyan_ilr_2      1.34610      NA      NA
f_JCZ38_qlogis      2.08337      NA      NA
f_JSE76_qlogis      1590.31880      NA      NA
log_alpha      -0.09336      NA      NA
log_beta      3.10191      NA      NA
a.1      2.08557      1.85439      2.31675

```

b.1	0.06998	0.05800	0.08197
SD.log_k_JCZ38	1.20053	0.43329	1.96777
SD.log_k_J9Z38	0.85854	0.26708	1.45000
SD.log_k_JSE76	0.62528	0.16061	1.08995
SD.f_cyan_ilr_1	0.35190	0.12340	0.58039
SD.f_cyan_ilr_2	0.85385	0.15391	1.55378
SD.log_alpha	0.28971	0.08718	0.49225
SD.log_beta	0.31614	0.05938	0.57290

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.2005	0.43329	1.9678
SD.log_k_J9Z38	0.8585	0.26708	1.4500
SD.log_k_JSE76	0.6253	0.16061	1.0900
SD.f_cyan_ilr_1	0.3519	0.12340	0.5804
SD.f_cyan_ilr_2	0.8538	0.15391	1.5538
SD.log_alpha	0.2897	0.08718	0.4923
SD.log_beta	0.3161	0.05938	0.5729

Variance model:

	est.	lower	upper
a.1	2.08557	1.854	2.31675
b.1	0.06998	0.058	0.08197

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.011e+02	NA	NA
k_JCZ38	6.506e-02	NA	NA
k_J9Z38	6.257e-03	NA	NA
k_JSE76	2.935e-02	NA	NA
f_cyan_to_JCZ38	6.776e-01	NA	NA
f_cyan_to_J9Z38	2.442e-01	NA	NA
f_JCZ38_to_JSE76	8.893e-01	NA	NA
f_JSE76_to_JCZ38	1.000e+00	NA	NA
alpha	9.109e-01	NA	NA
beta	2.224e+01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.67761
cyan_J9Z38	0.24417
cyan_sink	0.07822
JCZ38_JSE76	0.88928
JCZ38_sink	0.11072
JSE76_JCZ38	1.00000
JSE76_sink	0.00000

Estimated disappearance times:

	DT50	DT90	DT50back
cyan	25.36	256.37	77.18
JCZ38	10.65	35.39	NA
J9Z38	110.77	367.98	NA
JSE76	23.62	78.47	NA

Listing 18: Hierarchical DFOP path 2 fit with reduced random effects, constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:           4.2.2
Date of fit:      Fri Jan  6 01:52:20 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38 +
f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1588.988 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
102.4358      -2.3107      -5.3123      -3.7120      0.6753
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis  log_k1      log_k2
1.1462      12.4095      12.3630      -1.9317      -4.4557
g_qlogis
-0.5648

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      4.594      0.0000      0.000      0.0      0.0000
log_k_JCZ38  0.000      0.7966      0.000      0.0      0.0000
log_k_J9Z38  0.000      0.0000      1.561      0.0      0.0000
log_k_JSE76  0.000      0.0000      0.000      0.8      0.0000
f_cyan_ilr_1 0.000      0.0000      0.000      0.0      0.6349
f_cyan_ilr_2 0.000      0.0000      0.000      0.0      0.0000
f_JCZ38_qlogis 0.000      0.0000      0.000      0.0      0.0000
f_JSE76_qlogis 0.000      0.0000      0.000      0.0      0.0000
log_k1      0.000      0.0000      0.000      0.0      0.0000
log_k2      0.000      0.0000      0.000      0.0      0.0000
g_qlogis      0.000      0.0000      0.000      0.0      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_k1 log_k2
cyan_0      0.000      0.00      0.0      0.0 0.000 0.0000
log_k_JCZ38  0.000      0.00      0.0      0.0 0.000 0.0000
log_k_J9Z38  0.000      0.00      0.0      0.0 0.000 0.0000
log_k_JSE76  0.000      0.00      0.0      0.0 0.000 0.0000
f_cyan_ilr_1 0.000      0.00      0.0      0.0 0.000 0.0000
f_cyan_ilr_2 1.797      0.00      0.0      0.0 0.000 0.0000
f_JCZ38_qlogis 0.000      13.85      0.0      0.0 0.000 0.0000
f_JSE76_qlogis 0.000      0.00      14.1      0.0 0.000 0.0000
log_k1      0.000      0.00      0.0      1.106 0.0000
log_k2      0.000      0.00      0.0      0.000 0.6141
g_qlogis      0.000      0.00      0.0      0.000 0.0000
      g_qlogis
cyan_0      0.000
log_k_JCZ38 0.000
log_k_J9Z38 0.000
log_k_JSE76 0.000
f_cyan_ilr_1 0.000
f_cyan_ilr_2 0.000
f_JCZ38_qlogis 0.000
f_JSE76_qlogis 0.000
log_k1      0.000
log_k2      0.000
g_qlogis      1.595

Starting values for error model parameters:
a.1
1

```

Results:

Likelihood computed by importance sampling

AIC	BIC	logLik
2282	2274	-1121

Optimised parameters:

	est.	lower	upper
cyan_0	102.5254	NA	NA
log_k_JCZ38	-2.9358	NA	NA
log_k_J9Z38	-5.1424	NA	NA
log_k_JSE76	-3.6458	NA	NA
f_cyan_ilr_1	0.6957	NA	NA
f_cyan_ilr_2	0.6635	NA	NA
f_JCZ38_qlogis	4984.8163	NA	NA
f_JSE76_qlogis	1.9415	NA	NA
log_k1	-1.9456	NA	NA
log_k2	-4.4705	NA	NA
g_qlogis	-0.5117	NA	NA
a.1	2.7455	2.55392	2.9370
SD.log_k_JCZ38	1.3163	0.47635	2.1563
SD.log_k_J9Z38	0.7162	0.16133	1.2711
SD.log_k_JSE76	0.6457	0.15249	1.1390
SD.f_cyan_ilr_1	0.3424	0.11714	0.5677
SD.f_cyan_ilr_2	0.4524	0.09709	0.8077
SD.log_k1	0.7353	0.25445	1.2161
SD.log_k2	0.5137	0.18206	0.8453
SD.g_qlogis	0.9857	0.35651	1.6148

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.3163	0.47635	2.1563
SD.log_k_J9Z38	0.7162	0.16133	1.2711
SD.log_k_JSE76	0.6457	0.15249	1.1390
SD.f_cyan_ilr_1	0.3424	0.11714	0.5677
SD.f_cyan_ilr_2	0.4524	0.09709	0.8077
SD.log_k1	0.7353	0.25445	1.2161
SD.log_k2	0.5137	0.18206	0.8453
SD.g_qlogis	0.9857	0.35651	1.6148

Variance model:

	est.	lower	upper
a.1	2.745	2.554	2.937

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.025e+02	NA	NA
k_JCZ38	5.309e-02	NA	NA
k_J9Z38	5.844e-03	NA	NA
k_JSE76	2.610e-02	NA	NA
f_cyan_to_JCZ38	6.079e-01	NA	NA
f_cyan_to_J9Z38	2.272e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
f_JSE76_to_JCZ38	8.745e-01	NA	NA
k1	1.429e-01	NA	NA
k2	1.144e-02	NA	NA
g	3.748e-01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.6079
cyan_J9Z38	0.2272
cyan_sink	0.1649
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000
JSE76_JCZ38	0.8745
JSE76_sink	0.1255

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	22.29	160.20	48.22	4.85	60.58
JCZ38	13.06	43.37	NA	NA	NA
J9Z38	118.61	394.02	NA	NA	NA
JSE76	26.56	88.22	NA	NA	NA

Listing 19: Hierarchical DFOP path 2 fit with reduced random effects, two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:54:49 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan/dt = - ((k1 * g * exp(-k1 * time) + k2 * (1 - g) * exp(-k2 *
time)) / (g * exp(-k1 * time) + (1 - g) * exp(-k2 * time)))
* cyan
d_JCZ38/dt = + f_cyan_to_JCZ38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_JCZ38 * JCZ38 +
f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_to_J9Z38 * ((k1 * g * exp(-k1 * time) + k2 * (1 -
g) * exp(-k2 * time)) / (g * exp(-k1 * time) + (1 - g) *
exp(-k2 * time))) * cyan - k_J9Z38 * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1737.73 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
      101.7523      -1.5948      -5.0119      -2.2723      0.6719
f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis  log_k1      log_k2
      5.1681      12.8238      12.4130      -2.0057      -4.5526
g_qlogis
      -0.5805

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_0  log_k_JCZ38  log_k_J9Z38  log_k_JSE76  f_cyan_ilr_1
cyan_0      5.627      0.000      0.000      0.000      0.0000
log_k_JCZ38  0.000      2.327      0.000      0.000      0.0000
log_k_J9Z38  0.000      0.000      1.664      0.000      0.0000
log_k_JSE76  0.000      0.000      0.000      4.566      0.0000
f_cyan_ilr_1 0.000      0.000      0.000      0.000      0.6519
f_cyan_ilr_2 0.000      0.000      0.000      0.000      0.0000
f_JCZ38_qlogis 0.000      0.000      0.000      0.000      0.0000
f_JSE76_qlogis 0.000      0.000      0.000      0.000      0.0000
log_k1      0.000      0.000      0.000      0.000      0.0000
log_k2      0.000      0.000      0.000      0.000      0.0000
g_qlogis     0.000      0.000      0.000      0.000      0.0000
      f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis log_k1 log_k2
cyan_0      0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_JCZ38 0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_J9Z38 0.0      0.00      0.00      0.00 0.0000 0.0000
log_k_JSE76 0.0      0.00      0.00      0.00 0.0000 0.0000
f_cyan_ilr_1 0.0      0.00      0.00      0.00 0.0000 0.0000
f_cyan_ilr_2 10.1     0.00      0.00      0.00 0.0000 0.0000
f_JCZ38_qlogis 0.0     13.99     0.00      0.00 0.0000 0.0000
f_JSE76_qlogis 0.0     0.00      14.15     0.00 0.0000 0.0000
log_k1      0.0      0.00      0.00      0.00 0.8452 0.0000
log_k2      0.0      0.00      0.00      0.00 0.0000 0.5968
g_qlogis     0.0      0.00      0.00      0.00 0.0000 0.0000
      g_qlogis
cyan_0      0.000
log_k_JCZ38 0.000
log_k_J9Z38 0.000
log_k_JSE76 0.000
f_cyan_ilr_1 0.000
f_cyan_ilr_2 0.000
f_JCZ38_qlogis 0.000
f_JSE76_qlogis 0.000
log_k1      0.000
log_k2      0.000
g_qlogis     1.691

Starting values for error model parameters:
a.1 b.1
1 1

```

Results:

Likelihood computed by importance sampling

AIC	BIC	logLik
2232	2224	-1096

Optimised parameters:

	est.	lower	upper
cyan_0	101.20051	NA	NA
log_k_JCZ38	-2.93542	NA	NA
log_k_J9Z38	-5.03151	NA	NA
log_k_JSE76	-3.67679	NA	NA
f_cyan_ilr_1	0.67290	NA	NA
f_cyan_ilr_2	0.99787	NA	NA
f_JCZ38_qlogis	348.32484	NA	NA
f_JSE76_qlogis	1.87846	NA	NA
log_k1	-2.32738	NA	NA
log_k2	-4.61295	NA	NA
g_qlogis	-0.38342	NA	NA
a.1	2.06184	1.83746	2.28622
b.1	0.06329	0.05211	0.07447
SD.log_k_JCZ38	1.29042	0.47468	2.10617
SD.log_k_J9Z38	0.84235	0.25903	1.42566
SD.log_k_JSE76	0.56930	0.13934	0.99926
SD.f_cyan_ilr_1	0.35183	0.12298	0.58068
SD.f_cyan_ilr_2	0.77269	0.17908	1.36631
SD.log_k2	0.28549	0.09210	0.47888
SD.g_qlogis	0.93830	0.34568	1.53093

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_JCZ38	1.2904	0.4747	2.1062
SD.log_k_J9Z38	0.8423	0.2590	1.4257
SD.log_k_JSE76	0.5693	0.1393	0.9993
SD.f_cyan_ilr_1	0.3518	0.1230	0.5807
SD.f_cyan_ilr_2	0.7727	0.1791	1.3663
SD.log_k2	0.2855	0.0921	0.4789
SD.g_qlogis	0.9383	0.3457	1.5309

Variance model:

	est.	lower	upper
a.1	2.06184	1.83746	2.28622
b.1	0.06329	0.05211	0.07447

Backtransformed parameters:

	est.	lower	upper
cyan_0	1.012e+02	NA	NA
k_JCZ38	5.311e-02	NA	NA
k_J9Z38	6.529e-03	NA	NA
k_JSE76	2.530e-02	NA	NA
f_cyan_to_JCZ38	6.373e-01	NA	NA
f_cyan_to_J9Z38	2.461e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
f_JSE76_to_JCZ38	8.674e-01	NA	NA
k1	9.755e-02	NA	NA
k2	9.922e-03	NA	NA
g	4.053e-01	NA	NA

Resulting formation fractions:

	ff
cyan_JCZ38	0.6373
cyan_J9Z38	0.2461
cyan_sink	0.1167
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000
JSE76_JCZ38	0.8674
JSE76_sink	0.1326

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_k1	DT50_k2
cyan	24.93	179.68	54.09	7.105	69.86
JCZ38	13.05	43.36	NA	NA	NA
J9Z38	106.16	352.67	NA	NA	NA
JSE76	27.39	91.00	NA	NA	NA

Listing 20: Hierarchical SFORB path 2 fit with reduced random effects, constant variance

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:51:51 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
                cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
                cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
            * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
            * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1560.438 s
Using 300, 100 iterations and 10 chains

Variance model: Constant variance

Starting values for degradation parameters:
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      102.4394         -2.7673         -2.8942
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
      -3.6201         -2.3107         -5.3123
      log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
      -3.7120         0.6754         1.1448
      f_JCZ38_qlogis      f_JSE76_qlogis
      13.2672         13.3538

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
cyan_free_0      4.589      0.0000      0.00      0.00
log_k_cyan_free      0.000      0.4849      0.00      0.00
log_k_cyan_free_bound      0.000      0.0000      0.0000      1.62
log_k_cyan_bound_free      0.000      0.0000      0.00      0.00
log_k_JCZ38      0.000      0.0000      0.00      0.00
log_k_J9Z38      0.000      0.0000      0.0000      0.00
log_k_JSE76      0.000      0.0000      0.00      0.00
f_cyan_ilr_1      0.000      0.0000      0.00      0.00
f_cyan_ilr_2      0.000      0.0000      0.0000      0.00
f_JCZ38_qlogis      0.000      0.0000      0.00      0.00
f_JSE76_qlogis      0.000      0.0000      0.00      0.00
      log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000      0.0000      0.000      0.00      0.0
log_k_cyan_free      0.000      0.0000      0.000      0.00      0.0
log_k_cyan_free_bound      0.000      0.0000      0.000      0.00      0.0
log_k_cyan_bound_free      1.197      0.0000      0.000      0.00      0.0
log_k_JCZ38      0.000      0.7966      0.000      0.00      0.0
log_k_J9Z38      0.000      0.0000      1.561      0.00      0.0
log_k_JSE76      0.000      0.0000      0.000      0.00      0.8
f_cyan_ilr_1      0.000      0.0000      0.000      0.00      0.0
f_cyan_ilr_2      0.000      0.0000      0.000      0.00      0.0
f_JCZ38_qlogis      0.000      0.0000      0.000      0.00      0.0
f_JSE76_qlogis      0.000      0.0000      0.000      0.00      0.0
      f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis
cyan_free_0      0.0000      0.000      0.00      0.00      0.00
log_k_cyan_free      0.0000      0.000      0.00      0.00      0.00
log_k_cyan_free_bound      0.0000      0.000      0.00      0.00      0.00
log_k_cyan_bound_free      0.0000      0.000      0.00      0.00      0.00
log_k_JCZ38      0.0000      0.000      0.00      0.00      0.00
log_k_J9Z38      0.0000      0.000      0.00      0.00      0.00
log_k_JSE76      0.0000      0.000      0.00      0.00      0.00
f_cyan_ilr_1      0.6349      0.000      0.00      0.00      0.00
f_cyan_ilr_2      0.0000      1.797      0.00      0.00      0.00
f_JCZ38_qlogis      0.0000      0.000      13.84      0.00      0.00
f_JSE76_qlogis      0.0000      0.000      0.00      14.66

Starting values for error model parameters:
a.1
1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2279 2272 -1120

Optimised parameters:

	est.	lower	upper
cyan_free_0	102.5621	NA	NA
log_k_cyan_free	-2.8531	NA	NA
log_k_cyan_free_bound	-2.6916	NA	NA
log_k_cyan_bound_free	-3.5032	NA	NA
log_k_JCZ38	-2.9436	NA	NA
log_k_J9Z38	-5.1140	NA	NA
log_k_JSE76	-3.6472	NA	NA
f_cyan_ilr_1	0.6887	NA	NA
f_cyan_ilr_2	0.6874	NA	NA
f_JCZ38_qlogis	4063.6389	NA	NA
f_JSE76_qlogis	1.9556	NA	NA
a.1	2.7460	2.55451	2.9376
SD.log_k_cyan_free	0.3131	0.09841	0.5277
SD.log_k_cyan_free_bound	0.8850	0.29909	1.4710
SD.log_k_cyan_bound_free	0.6167	0.20391	1.0295
SD.log_k_JCZ38	1.3555	0.49101	2.2200
SD.log_k_J9Z38	0.7200	0.16166	1.2783
SD.log_k_JSE76	0.6252	0.14619	1.1042
SD.f_cyan_ilr_1	0.3386	0.11447	0.5627
SD.f_cyan_ilr_2	0.4699	0.09810	0.8417

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_cyan_free	0.3131	0.09841	0.5277
SD.log_k_cyan_free_bound	0.8850	0.29909	1.4710
SD.log_k_cyan_bound_free	0.6167	0.20391	1.0295
SD.log_k_JCZ38	1.3555	0.49101	2.2200
SD.log_k_J9Z38	0.7200	0.16166	1.2783
SD.log_k_JSE76	0.6252	0.14619	1.1042
SD.f_cyan_ilr_1	0.3386	0.11447	0.5627
SD.f_cyan_ilr_2	0.4699	0.09810	0.8417

Variance model:

	est.	lower	upper
a.1	2.746	2.555	2.938

Backtransformed parameters:

	est.	lower	upper
cyan_free_0	1.026e+02	NA	NA
k_cyan_free	5.767e-02	NA	NA
k_cyan_free_bound	6.777e-02	NA	NA
k_cyan_bound_free	3.010e-02	NA	NA
k_JCZ38	5.267e-02	NA	NA
k_J9Z38	6.012e-03	NA	NA
k_JSE76	2.606e-02	NA	NA
f_cyan_free_to_JCZ38	6.089e-01	NA	NA
f_cyan_free_to_J9Z38	2.299e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
f_JSE76_to_JCZ38	8.761e-01	NA	NA

Estimated Eigenvalues of SFORB model(s):

	cyan_b1	cyan_b2	cyan_g
	0.1434	0.0121	0.3469

Resulting formation fractions:

	ff
cyan_free_JCZ38	0.6089
cyan_free_J9Z38	0.2299
cyan_free_sink	0.1612
cyan_free	1.0000
JCZ38_JSE76	1.0000
JCZ38_sink	0.0000
JSE76_JCZ38	0.8761
JSE76_sink	0.1239

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_cyan_b1	DT50_cyan_b2
cyan	23.94	155.06	46.68	4.832	57.28
JCZ38	13.16	43.71	NA	NA	NA
J9Z38	115.30	383.02	NA	NA	NA
JSE76	26.59	88.35	NA	NA	NA

Listing 21: Hierarchical SFORB path 2 fit with reduced random effects, two-component error

```

saemix version used for fitting:      3.2
mkin version used for pre-fitting:    1.2.2
R version used for fitting:          4.2.2
Date of fit:      Fri Jan  6 01:54:31 2023
Date of summary:  Fri Jan  6 01:54:50 2023

Equations:
d_cyan_free/dt = - k_cyan_free * cyan_free - k_cyan_free_bound *
               cyan_free + k_cyan_bound_free * cyan_bound
d_cyan_bound/dt = + k_cyan_free_bound * cyan_free - k_cyan_bound_free *
               cyan_bound
d_JCZ38/dt = + f_cyan_free_to_JCZ38 * k_cyan_free * cyan_free - k_JCZ38
               * JCZ38 + f_JSE76_to_JCZ38 * k_JSE76 * JSE76
d_J9Z38/dt = + f_cyan_free_to_J9Z38 * k_cyan_free * cyan_free - k_J9Z38
               * J9Z38
d_JSE76/dt = + f_JCZ38_to_JSE76 * k_JCZ38 * JCZ38 - k_JSE76 * JSE76

Data:
433 observations of 4 variable(s) grouped in 5 datasets

Model predictions using solution type deSolve

Fitted in 1719.72 s
Using 300, 100 iterations and 10 chains

Variance model: Two-component variance function

Starting values for degradation parameters:
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      101.751         -2.837         -3.016
log_k_cyan_bound_free      log_k_JCZ38      log_k_J9Z38
      -3.660         -2.299         -5.313
      log_k_JSE76      f_cyan_ilr_1      f_cyan_ilr_2
      -3.699         0.672         5.873
      f_JCZ38_qlogis      f_JSE76_qlogis
      13.216         13.338

Fixed degradation parameter values:
None

Starting values for random effects (square root of initial entries in omega):
      cyan_free_0      log_k_cyan_free log_k_cyan_free_bound
      5.629         0.000         0.000
log_k_cyan_free      0.000         0.446         0.000
log_k_cyan_free_bound      0.000         0.000         1.449
log_k_cyan_bound_free      0.000         0.000         0.000
log_k_JCZ38      0.000         0.000         0.000
log_k_J9Z38      0.000         0.000         0.000
log_k_JSE76      0.000         0.000         0.000
f_cyan_ilr_1      0.000         0.000         0.000
f_cyan_ilr_2      0.000         0.000         0.000
f_JCZ38_qlogis      0.000         0.000         0.000
f_JSE76_qlogis      0.000         0.000         0.000
      log_k_cyan_bound_free log_k_JCZ38 log_k_J9Z38 log_k_JSE76
cyan_free_0      0.000         0.0000         0.000         0.0000
log_k_cyan_free      0.000         0.0000         0.000         0.0000
log_k_cyan_free_bound      0.000         0.0000         0.000         0.0000
log_k_cyan_bound_free      1.213         0.0000         0.000         0.0000
log_k_JCZ38      0.000         0.7801         0.000         0.0000
log_k_J9Z38      0.000         0.0000         1.575         0.0000
log_k_JSE76      0.000         0.0000         0.000         0.8078
f_cyan_ilr_1      0.000         0.0000         0.000         0.0000
f_cyan_ilr_2      0.000         0.0000         0.000         0.0000
f_JCZ38_qlogis      0.000         0.0000         0.000         0.0000
f_JSE76_qlogis      0.000         0.0000         0.000         0.0000
      f_cyan_ilr_1 f_cyan_ilr_2 f_JCZ38_qlogis f_JSE76_qlogis
cyan_free_0      0.0000         0.00         0.00         0.00
log_k_cyan_free      0.0000         0.00         0.00         0.00
log_k_cyan_free_bound      0.0000         0.00         0.00         0.00
log_k_cyan_bound_free      0.0000         0.00         0.00         0.00
log_k_JCZ38      0.0000         0.00         0.00         0.00
log_k_J9Z38      0.0000         0.00         0.00         0.00
log_k_JSE76      0.0000         0.00         0.00         0.00
f_cyan_ilr_1      0.6519         0.00         0.00         0.00
f_cyan_ilr_2      0.0000         10.78         0.00         0.00
f_JCZ38_qlogis      0.0000         0.00         13.96         0.00
f_JSE76_qlogis      0.0000         0.00         0.00         14.69

Starting values for error model parameters:
a.1 b.1
1 1

```

Results:

Likelihood computed by importance sampling

AIC BIC logLik
2236 2228 -1098

Optimised parameters:

	est.	lower	upper
cyan_free_0	100.72760	NA	NA
log_k_cyan_free	-3.18281	NA	NA
log_k_cyan_free_bound	-3.37924	NA	NA
log_k_cyan_bound_free	-3.77107	NA	NA
log_k_JCZ38	-2.92811	NA	NA
log_k_J9Z38	-5.02759	NA	NA
log_k_JSE76	-3.65835	NA	NA
f_cyan_ilr_1	0.67390	NA	NA
f_cyan_ilr_2	1.15106	NA	NA
f_JCZ38_qlogis	827.82299	NA	NA
f_JSE76_qlogis	1.83064	NA	NA
a.1	2.06921	1.84443	2.29399
b.1	0.06391	0.05267	0.07515
SD.log_k_cyan_free	0.50518	0.18962	0.82075
SD.log_k_cyan_bound_free	0.30991	0.08170	0.53813
SD.log_k_JCZ38	1.26661	0.46578	2.06744
SD.log_k_J9Z38	0.88272	0.27813	1.48730
SD.log_k_JSE76	0.53050	0.12561	0.93538
SD.f_cyan_ilr_1	0.35547	0.12461	0.58633
SD.f_cyan_ilr_2	0.91446	0.20131	1.62761

Correlation is not available

Random effects:

	est.	lower	upper
SD.log_k_cyan_free	0.5052	0.1896	0.8207
SD.log_k_cyan_bound_free	0.3099	0.0817	0.5381
SD.log_k_JCZ38	1.2666	0.4658	2.0674
SD.log_k_J9Z38	0.8827	0.2781	1.4873
SD.log_k_JSE76	0.5305	0.1256	0.9354
SD.f_cyan_ilr_1	0.3555	0.1246	0.5863
SD.f_cyan_ilr_2	0.9145	0.2013	1.6276

Variance model:

	est.	lower	upper
a.1	2.06921	1.84443	2.29399
b.1	0.06391	0.05267	0.07515

Backtransformed parameters:

	est.	lower	upper
cyan_free_0	1.007e+02	NA	NA
k_cyan_free	4.147e-02	NA	NA
k_cyan_free_bound	3.407e-02	NA	NA
k_cyan_bound_free	2.303e-02	NA	NA
k_JCZ38	5.350e-02	NA	NA
k_J9Z38	6.555e-03	NA	NA
k_JSE76	2.578e-02	NA	NA
f_cyan_free_to_JCZ38	6.505e-01	NA	NA
f_cyan_free_to_J9Z38	2.508e-01	NA	NA
f_JCZ38_to_JSE76	1.000e+00	NA	NA
f_JSE76_to_JCZ38	8.618e-01	NA	NA

Estimated Eigenvalues of SFORB model(s):

	cyan_b1	cyan_b2	cyan_g
	0.08768	0.01089	0.39821

Resulting formation fractions:

	ff
cyan_free_JCZ38	0.65053
cyan_free_J9Z38	0.25082
cyan_free_sink	0.09864
cyan_free	1.00000
JCZ38_JSE76	1.00000
JCZ38_sink	0.00000
JSE76_JCZ38	0.86184
JSE76_sink	0.13816

Estimated disappearance times:

	DT50	DT90	DT50back	DT50_cyan_b1	DT50_cyan_b2
cyan	25.32	164.79	49.61	7.906	63.64
JCZ38	12.96	43.04	NA	NA	NA
J9Z38	105.75	351.29	NA	NA	NA
JSE76	26.89	89.33	NA	NA	NA

Session info

R version 4.2.2 Patched (2022-11-10 r83330)
Platform: x86_64-pc-linux-gnu (64-bit)
Running under: Debian GNU/Linux bookworm/sid

Matrix products: default

BLAS: /usr/lib/x86_64-linux-gnu/openblas-serial/libblas.so.3

LAPACK: /usr/lib/x86_64-linux-gnu/openblas-serial/libopenblas-r0.3.21.so

locale:

```
[1] LC_CTYPE=de_DE.UTF-8      LC_NUMERIC=C
[3] LC_TIME=de_DE.UTF-8      LC_COLLATE=de_DE.UTF-8
[5] LC_MONETARY=de_DE.UTF-8  LC_MESSAGES=de_DE.UTF-8
[7] LC_PAPER=de_DE.UTF-8     LC_NAME=C
[9] LC_ADDRESS=C             LC_TELEPHONE=C
[11] LC_MEASUREMENT=de_DE.UTF-8 LC_IDENTIFICATION=C
```

attached base packages:

```
[1] parallel stats graphics grDevices utils datasets methods
[8] base
```

other attached packages:

```
[1] saemix_3.2 npde_3.3 knitr_1.41 mkin_1.2.2
```

loaded via a namespace (and not attached):

```
[1] highr_0.9 compiler_4.2.2 pillar_1.8.1 prettyunits_1.1.1
[5] tools_4.2.2 pkgbuild_1.4.0 mclust_6.0.0 digest_0.6.31
[9] evaluate_0.19 lifecycle_1.0.3 tibble_3.1.8 gtable_0.3.1
[13] nlme_3.1-161 lattice_0.20-45 pkgconfig_2.0.3 rlang_1.0.6
[17] DBI_1.1.3 cli_3.5.0 yaml_2.3.6 xfun_0.35
[21] fastmap_1.1.0 gridExtra_2.3 stringr_1.5.0 dplyr_1.0.10
[25] generics_0.1.3 vctrs_0.5.1 lmtest_0.9-40 grid_4.2.2
[29] tidyselect_1.2.0 inline_0.3.19 deSolve_1.34 glue_1.6.2
[33] R6_2.5.1 processx_3.8.0 fansi_1.0.3 rmarkdown_2.19
[37] callr_3.7.3 ggplot2_3.4.0 magrittr_2.0.3 codetools_0.2-18
[41] ps_1.7.2 scales_1.2.1 htmltools_0.5.4 assertthat_0.2.1
[45] colorspace_2.0-3 utf8_1.2.2 stringi_1.7.8 munsell_0.5.0
[49] crayon_1.5.2 zoo_1.8-11
```

Hardware info

CPU model: AMD Ryzen 9 7950X 16-Core Processor

MemTotal: 64940452 kB